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Auxiliary-field quantum Monte Carlo calculations of the molybdenum dimer

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Chemical accuracy is difficult to achieve for systems with transition metal atoms. Third row transition metal atoms are particularly challenging due to strong electron-electron correlation in localized d-orbitals. The Cr₂ molecule is an outstanding example, which we previously treated with highly accurate auxiliary-field quantum Monte Carlo (AFQMC) calculations [W. Purwanto et al., J. Chem. Phys. 142, 064302 (2015)]. Somewhat surprisingly, computational description of the isoelectronic Mo₂ dimer has also, to date, been scattered and less than satisfactory. We present high-level theoretical benchmarks of the Mo₂ singlet ground state (X¹Σ⁺) and first triplet excited state (a³Σ⁺), using the phaseless AFQMC calculations. Extrapolation to the complete basis set limit is performed. Excellent agreement with experimental spectroscopic constants is obtained. We also present a comparison of the correlation effects in Cr₂ and Mo₂. Published by AIP Publishing.

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I. INTRODUCTION

Transition metal (TM) dimers are of special interest theoretically and computationally. They fully exhibit the complexity of more complex TM materials (such as the formation of high-order bonds), but their relatively small sizes make them amenable to systematic and rigorous theoretical studies. Group VIB dimers are especially interesting, because the atom fragments are in the high-spin state (⁷S), and they form a closed shell (¹Σ) configuration in the molecular ground state. This results in a many-body spectrum with many nearly degenerate states, with strong electronic correlation effects. The Mo₂ molecule is similar to Cr₂ in that both are highly multiconfigurational in nature and require accurate treatment of both static and dynamic electron correlation. Because the 4d orbitals are not as localized as 3d, the severity of electronic correlation is significantly reduced for Mo₂. For example, a complete active space self-consistent field (CASSCF) treatment in Mo₂ recovers about 30% of the experimental binding energy, while with the same wave function, Cr₂ is not even bound. Nevertheless, the best quantum chemistry calculations for Mo₂ give widely varying predictions.¹–³

In this work, we present accurate theoretical calculations of Mo₂ potential energy curves (PECs) near the equilibrium geometry. We consider both the singlet ground state (X¹Σ⁺) and triplet first excited state (a³Σ⁺), and calculate their spectroscopic properties. We employ the phaseless auxiliary-field quantum Monte Carlo (AFQMC) method⁴–⁷ in our calculations. Select benchmark calculations were also performed with exact free-projection (FP) AFQMC⁷–⁹ to help establish the accuracy of our calculations. A high-quality quadruple zeta (QZ) basis set is used for the majority of our calculations. Extrapolation to the complete basis set (CBS) limit is performed in combination with the triple zeta (TZ) basis results, following standard approaches. As shown below, the AFQMC results for the spectroscopic constants are in excellent agreement with experiment. We compare our results with those from other quantum chemistry approaches. The similarities and differences in electron-electron correlation between Mo₂ and Cr₂ are also examined.

The remainder of the paper proceeds as follows. The methodology is discussed in Section II. Results of our Mo₂ calculations are presented in Section III. Section IV presents comparisons with previous many-body quantum chemistry results and an analysis of the relative sizes of the correlation energy contributions in Mo₂ and Cr₂, as well as the effect of the trial wave function in the AFQMC calculations. We summarize our results in Section V.

II. METHODOLOGY

The AFQMC method projects the many-body ground state wave function from a given trial wave function.¹⁰–¹² It is implemented as random walks of Slater determinants, with orbitals expressed in a chosen single-particle basis. A phaseless approximation⁴ has been introduced to control the phase problem introduced by complex auxiliary-field sampling, resulting in a practical computational method that scales modestly with the system size [e.g., O(N³) or O(N⁴)]. Its high accuracy has been demonstrated in many molecular and solid systems⁵,⁸,¹³–¹⁶ as well as model electronic systems.⁷,¹⁷

As an orbitally based wave function method, the AFQMC theoretical framework has close relationships to many-body quantum chemistry methods. When expressed in a one-particle gaussian type orbital (GTO) basis, both approaches use exactly the same Hamiltonian. Thus, many efficient techniques developed for correlated quantum chemistry methods can be directly imported. This was done, for example, by using Cholesky decomposition to remove a
bottleneck in the handling of two-body interaction matrix elements for large basis sets \(^{18}\) and introducing frozen-core type of approaches to seamlessly embed the highly correlated AFQMC treatment within a larger mean-field environment.\(^{14,16}\)

Since static correlation is important in \(\text{Mo}_2\), it is desirable that the trial wave function accounts for this effect well. We perform CASSCF\((12e,12o)\) calculations, which correlate 12 electrons in 12 active orbitals derived from 4d and 5s atomic states. The resulting multideterminant expansion is then truncated to retain about 93%–95% of the total weight, yielding a multi-determinant wave function which is used without further optimization as our trial wave function. Typically this gives a trial wave function with 90–240 determinants for the ground state, and 30 – 290 for the excited state. Since the number of determinants grows rapidly with bond stretching, we have to use a shorter cutoff \((86\%–92\%)\) at larger bond lengths \((\geq 2.2 \, \text{Å})\) in order to keep the number of determinants in a range that is easy to handle with the current state of our code.

We perform our AFQMC calculations using the all-electron atomic natural orbital relativistic correlation consistent (ANO RCC) GTO basis.\(^{19}\) Scalar relativity is treated with the Douglas-Kroll-Hess Hamiltonian. Spin-orbit effects on the dissociation energy were assessed with density functional theory calculations, using NWChem, with a cc-pwCVTZ-PP basis, and Dolg’s energy-consistent spin-orbit relativistic effective core potential (ECP). There was essentially no effect on the dissociation energy (with the spin-orbit generalized gradient approximation PBE functional), so this was not pursued further. The Ar+3d\(^{10}\) atom-like core orbitals are frozen at the mean-field (CASSCF) level. The calculated results were obtained using basis sets up to the realistic QZ \((8s7p5d3f2g1h contraction)\) basis,\(^3\) denoted ANO-QZ hereafter. As shown below, this basis provides excellent results for many quantities. The exception is the binding energy, which needs to be extrapolated to the CBS limit in order to make reliable comparisons with experiment.

### III. RESULTS

We first present \(\text{Mo}_2\) AFQMC results obtained with the ANO-QZ basis, before discussing the CBS-extrapolated results. Previously reported many-body calculations\(^1\)–\(^3\) largely used multireference perturbative methods. The ANO-QZ CASPT2 (complete active space second-order perturbation theory) results of Borin et al.\(^3\) are among the most accurate. The exact and approximate AFQMC results, using the same basis, will provide a useful benchmark to those results.

Figure 1 shows the \(\text{Mo}_2\) AFQMC binding-energy curves of the ground (singlet \(X\)) and excited (triplet \(a\)) states in the ANO-QZ basis. (The binding energy is defined as the difference between the molecular total energy and that of the two isolated atoms. It is shown as a function of \(R_{\text{Mo-Mo}}\), the distance between the two \(\text{Mo}_2\) nuclei.) AFQMC calculations of the Mo atoms were done using the ROHF trial wave function. For the ground state of the molecule, phaseless AFQMC calculations are performed using both UHF (AFQMC/UHF) and truncated CASSCF (AFQMC/CASSCF) trial wave functions. The computed binding energy curves are shown; also shown is the exact free projection AFQMC (FP-AFQMC) binding energy for a geometry near equilibrium. For the excited state, only AFQMC/CASSCF results are shown. Morse curves are fitted to these results and are shown as color bands whose width represents the combined stochastic and fitting uncertainties. The ground state appears to exhibit stronger correlations, as evidenced by the larger statistical error bar for similar quality of trial wave functions and roughly comparable amounts of AFQMC computation. This is also consistent with the observation that the Hartree-Fock energy for the singlet state is higher than the triplet and that a larger number of determinants are in the trial wave function for the ground state even though the same cutoff is applied when truncating both the ground- and excited-state CASSCF wave functions (see Sec. II).

While AFQMC/UHF overestimates the binding energy by \(\sim 0.25\) eV compared to the exact FP-AFQMC, AFQMC/CASSCF shows excellent agreement. This establishes the high accuracy of the truncated CASSCF trial wave function for \(\text{Mo}_2\). Similar behavior was found in our previous work on \(\text{Cr}_2\),\(^{15}\) where a multi-determinant truncated CASSCF trial wave function was also required. In the more strongly correlated \(\text{Cr}_2\) molecule, however, AFQMC/UHF overestimated the binding by \(\sim 0.9\) eV near the equilibrium bond length for a TZ basis.\(^{15}\) For comparison, the CASPT2 results\(^1\) in the same basis set are also shown in Fig. 1. We see that both the ground and excited states appear to be overbound by \(\sim 0.3\) eV. In the ground state of \(\text{Cr}_2\), CASPT2 results showed the same trend, resulting in overbinding by \(\sim 0.8\) eV.\(^{15,20}\)

The CBS-extrapolated AFQMC/CASSCF PECs are shown in Figure 2. As in our previous work,\(^{15}\) the QS \(\rightarrow\) CBS correction was obtained from AFQMC/UHF calculations.
using the ANO-TZ (7s6p4d1f) and ANO-QZ basis sets. Extrapolation with only these two available basis sets is less than ideal and could potentially cause uncertainties. In Cr$_2$, we were able to validate the TZ-QZ extrapolation with explicit calculations using the 5Z basis set. Cross comparison of the results here with those from Cr$_2$ is valuable and helps to improve confidence in the procedure. We use a two-part scheme to extrapolate the many-body energies to the CBS limit, as the exponential ansatz for the HF energies (with exponent $c = 1.63$) and the inverse cubic form for the correlation energies. The QZ $\rightarrow$ CBS correction increases the magnitude of the AFQMC binding energy by about 0.3 eV and 0.2 eV at the shortest and longest bond distances ($R_{\text{Mo-Mo}} = 1.7$ and 2.2 Å, respectively). In this geometry range, the correction is well approximated by a linear function of $R_{\text{Mo-Mo}}$. This correction was applied to ANO-QZ AFQMC/CASSCF PECs to obtain the CBS limit. Test calculations showed that the excited state CBS correction was within error bars of the ground state CBS value, so we used the ground state correction for both.

Spectroscopic constants corresponding to Figs. 1 and 2 are given in Tables I and II for the ground and excited states, respectively. The tables also show results from experiment and from other high-level quantum chemistry many-body calculations. Our coupled cluster singles and doubles with perturbative triples [CCSD(T)] results were extrapolated to the CBS limit following the same procedure as described above, using CCSD(T) calculations for all basis sets; the CBS correction obtained this way was slightly smaller than, but consistent with, AFQMC/UHF CBS correction. For multi-reference perturbative calculations, the CBS extrapolation is less straightforward, since their correlation energies do not fit the inverse-cubic ansatz well, as discussed further below. Consequently, we made no attempt to apply the same CBS corrections to the perturbative results in Tables I and II; the values are listed in a separate column and correspond to the specified basis set.

As discussed in connection with Fig. 1, AFQMC/CASSCF is essentially exact near equilibrium. Thus, the AFQMC/CASSCF results in Tables I and II provide a benchmark for assessing the other quantum chemistry methods. At the CBS limit AFQMC/CASSCF is seen to be in excellent agreement with the experiment. In contrast, other quantum chemistry results show considerable variance, especially for the molecular dissociation energy $D_c$. This is discussed further in Sec. IV.

### Table I. Ground state ($X^1\Sigma^+$) spectroscopic properties of Mo$_2$ computed using phaseless AFQMC and other quantum chemistry methods. $D_c$ is the molecular dissociation energy, in units of eV (where the zero-point energy $\sim 0.03$ eV has been removed from the experimental value); $R_0$ is the equilibrium bond length (in Å); and $\omega_e$ is the harmonic vibrational frequency (in cm$^{-1}$). Unless otherwise indicated, the ANO-QZ basis (see text) is used. CBS extrapolation of $D_c$ is shown also, when applicable.

<table>
<thead>
<tr>
<th>Method</th>
<th>$D_c$</th>
<th>$D_c$ (CBS)</th>
<th>$R_0$</th>
<th>$\omega_e$</th>
</tr>
</thead>
<tbody>
<tr>
<td>PT2–NEV (larger basis)</td>
<td>4.8845</td>
<td>...</td>
<td>1.9187</td>
<td>507.64</td>
</tr>
<tr>
<td>PT2–NEV$^{a,b,c}$</td>
<td>5.055</td>
<td>...</td>
<td>1.9198</td>
<td>506.09</td>
</tr>
<tr>
<td>PT3–NEV$^{a,d,e}$</td>
<td>3.9685</td>
<td>...</td>
<td>1.9500</td>
<td>461.54</td>
</tr>
<tr>
<td>PT2$^{c,g}$</td>
<td>4.41</td>
<td>...</td>
<td>1.950</td>
<td>459</td>
</tr>
<tr>
<td>MRSDCI+Q$^b$</td>
<td>3.9</td>
<td>...</td>
<td>1.993</td>
<td>447.5</td>
</tr>
<tr>
<td>CCSD(T)</td>
<td>3.85</td>
<td>4.06</td>
<td>1.913</td>
<td>549</td>
</tr>
<tr>
<td>AFQMC/UHF</td>
<td>4.45(1)</td>
<td>4.66(1)</td>
<td>1.955(4)</td>
<td>428(5)</td>
</tr>
<tr>
<td>AFQMC/CASSCF</td>
<td>4.20(5)</td>
<td>4.46(5)</td>
<td>1.95(2)</td>
<td>467(24)</td>
</tr>
<tr>
<td>Experiment</td>
<td>4.51(1)$^d$</td>
<td>1.940(9)$^d$</td>
<td>477.1$^d$</td>
<td></td>
</tr>
</tbody>
</table>

$^a$Ref. 2.
$^b$Strongly contracted NEVPT2(12e,12o) method.
$^c$Strongly contracted NEVPT3(12e,12o) method.
$^d$CASPT2(12e,12o) method.
$^e$Ref. 1. Calculations use an ECP with 5s5p4d1f basis (see cited article for detail).
$^f$Ref. 25.
$^g$Ref. 26.
$^h$Ref. 27.
TABLE II. Excited state \((\alpha^{2}\Sigma_{u}^{+})\) spectroscopic properties of Mo\(_2\) computed using phaseless AFQMC and other quantum chemistry methods. \(T_e\) is the excitation energy from the ground state (in units of eV); \(R_0\) is the bond length at the PEC minimum (in Å); and \(\omega_c\) is the harmonic vibrational frequency (in cm\(^{-1}\)). Unless otherwise indicated, the ANO-QZ basis (see text) is used. CBS extrapolation of \(T_e\) is shown also, when applicable.

<table>
<thead>
<tr>
<th>Method</th>
<th>(T_e)</th>
<th>(T_e) (CBS)</th>
<th>(R_0)</th>
<th>(\omega_c)</th>
</tr>
</thead>
<tbody>
<tr>
<td>PT2(^{a,b})</td>
<td>1.105</td>
<td>...</td>
<td>2.063</td>
<td>393</td>
</tr>
<tr>
<td>AFQMC/CASSCF</td>
<td>1.15(6)</td>
<td>1.15(6)</td>
<td>2.05(1)</td>
<td>399(20)</td>
</tr>
<tr>
<td>Experiment</td>
<td>0.994(^{c})</td>
<td>...</td>
<td>393.7(^{c})</td>
<td></td>
</tr>
</tbody>
</table>

\(^{a}\)Ref. 3.  
\(^{b}\)CASPT2(12e,12o) method.  
\(^{c}\)Ref. 28.

IV. DISCUSSION

In this section, we analyze in more detail both the comparison of AFQMC with other methods and the comparison of the correlation effects in Mo\(_2\) with Cr\(_2\). Correlation effects are greatly reduced in Mo\(_2\) compared to Cr\(_2\). While the CASSCF result is not bound for Cr\(_2\) for an active space as large as (12e,28o), in Mo\(_2\) CASSCF(12e,12o) already recovers 30% of the binding energy. For systems with strong static correlation, multireference perturbation theory has often been the method of choice. As shown in Table I, however, the results depend rather sensitively on the perturbative implementation. Given that Mo\(_2\) is considerably more benign than Cr\(_2\), it is perhaps somewhat surprising that it turns out to be rather challenging to the best quantum chemistry methods.

A. Comparison with other theoretical results

The CASPT2 calculation of Borin et al.,\(^3\) using the ANO-QZ basis and a CASSCF(12e,12o) active space zero-order wave function, overestimates \(D_e\) by ~0.2 eV. In Cr\(_2\), CASPT2(12,12) shows much larger overbinding of ~1.0 eV, based on direct comparisons with the exact FP-AFQMC.\(^{15}\) This trend has been attributed to the inadequacy of the active space chosen for the zeroth-order wave function.\(^{2,20}\) In Cr\(_2\), an improved zeroth-order wave function was obtained for a larger active space of 12 electrons and 28 orbitals, using a self-consistent density matrix renormalization group (DMRG) calculation.\(^{28}\) The subsequent CASPT2 calculation\(^{20}\) reduces, but does not eliminate, the discrepancy with exact FP-AFQMC, resulting in underbinding by ~0.4 eV.\(^{15}\) (See also Ref. 23 for a treatment of Cr\(_2\) with a split partitioning of the active space.) Multireference perturbative methods are also sensitive to the perturbative implementation. Results from an alternative perturbation treatment, using \(n\)-electron valence perturbation theory (NEVPT)\(^{24}\) are also shown in Table I. The second-order PT2-NEV results show larger overbinding, while third-order PT3-NEV is underbound by ~0.2 eV. The \(D_e\) of PT2-NEV is reduced by 0.2 eV upon increasing the ANO basis size. This is opposite to AFQMC and CCSD(T), which show \(D_e\) increasing with basis size. The basis convergence of the perturbative calculations does not follow the empirical \(x^{-3}\) behavior, where \(x\) is the (correlation consistent) basis cardinal number. (Hence no CBS extrapolation is performed on the results, as mentioned earlier.) In view of these considerations, the agreement of the CASPT2 Mo\(_2\) ANO-QZ calculation with the experimental binding energy is likely somewhat fortuitous.

Table I also presents results from multireference singles and doubles configuration interaction (MRSDCI) calculations,\(^{1}\) with \(Q\) correction applied, and from CCSD(T). The MRSDCI+\(Q\) used an ECP and a smaller basis. Single-reference CCSD(T), with restricted HF reference wave function, performs much better in Mo\(_2\) than in Cr\(_2\). While CCSD(T) underestimates the triplet excited state (Table II), we find that the AFQMC and CASPT2 results agree very well with each other and with the experiment.

B. Comparing Cr\(_2\) and Mo\(_2\)

In this section, we quantitatively compare the effect of electron-electron correlation in Cr\(_2\) and Mo\(_2\). Under the frozen-core Hamiltonian, these molecules have the same number of correlated electrons, so that the correlation energies are directly comparable. We use the exact FP-AFQMC to benchmark the relative effects between the two molecules. Figure 3 compares the magnitude of electron-electron correlation effects in the Cr\(_2\) and Mo\(_2\) molecules. Results for Cr\(_2\) were obtained using the cc-pwCVTZ-DK basis at the experimental bond length \(R = 1.6788\) Å (see Ref. 15); the Cr\(_2\) RHF energy is ~2098.533 662 \(E_h\). Results for Mo\(_2\) were obtained using the ANO-QZ basis near the experimental bond length \(R = 1.9\) Å; the Mo\(_2\) RHF energy is ~8091.069 911 \(E_h\). Although the correlation energy is ~0.5 \(E_h\) larger in Cr\(_2\) than in Mo\(_2\), the Cr\(_2\) UHF wave function recovers a larger fraction of the correlation energy, 32%, versus 15% in Mo\(_2\). The CASSCF wave function shows a similar but less pronounced trend, recovering 39% and 28% in Cr\(_2\) and Mo\(_2\), respectively.

The stronger correlation effects in Cr\(_2\), however, are evident in the top panel of Fig. 3(b): achieving 95% of the CASSCF total wave function weight requires retaining 559 determinants in Cr\(_2\) but only 168 in Mo\(_2\). This is also evident in the larger CCSD(T) discrepancy in Cr\(_2\) than in Mo\(_2\), ~40 \(mE_h\) and ~7 \(mE_h\), respectively. The dependence of the AFQMC/CASSCF energies on the quality of the trial wave function is shown in the bottom panel of Fig. 3(b). The dependence is significantly stronger in Cr\(_2\), where at 95% cutoff, the total energy is still ~13 \(mE_h\) higher than the exact value (this error is ~5 \(mE_h\) for Mo\(_2\)). At the variational level, although the truncated wave function recovers more correlation energy in Cr\(_2\) than in Mo\(_2\) for the same weight cut, its performance is worse in AFQMC/CASSCF. We attribute this to the larger dynamic correlation energy that must be recovered in Cr\(_2\). Cancellation of errors between the molecule and atom AFQMC energies leads to better agreement in binding energy, however. For the best truncated CASSCF
FIG. 3. The correlation energy in the Cr\(_2\) and Mo\(_2\) molecules. All energies are reported relative to the restricted HF (RHF) energy. Note that the energy offset in the lower panels of (a) and (b) aligns the (exact) FP-AFQMC correlation energies of Cr\(_2\) and Mo\(_2\). (a) Upper panels: RHF (dotted zero baseline), UHF (dashed line), and CASSCF (solid line) energies. Lower panels: CCSD(T) (dashed line), AFQMC/CASSCF at 95% weight cutoff (triangle and square), FP-AFQMC (diamond), AFQMC/UHF (circle); the AFQMC statistical uncertainties are indicated by the shading. (b) Correlation energy as a function of the retained weight in the multi-determinant CASSCF wave function. Solid squares and open triangles denote the Mo\(_2\) and Cr\(_2\) results, respectively. Upper panel: variational energy of the truncated CASSCF wave function; numbers adjacent to the symbols give the number of determinants in the truncated wave function. Lower panel: the corresponding AFQMC/CASSCF correlation energies; statistical uncertainties indicated by the error bars. The exact FP-AFQMC energy from (a) is also shown. See the text for additional details.

wave function, the error in the binding energy is \(~5\) m\(E_h\) (~0.14 eV) for Cr\(_2\), and virtually exact for Mo\(_2\). Basis set errors will modify the correlation energy recovered by the different methods. The mean-field HF energies are quite well converged for the basis sets used here. For the many-body calculations, we estimate (using AFQMC/UHF) the CBS shifts to be \(~100\) m\(E_h\) and \(~70\) m\(E_h\) for Cr\(_2\) and Mo\(_2\), respectively. For the purpose of the above comparisons, however, the relative error between the various approximate and exact methods should not change significantly.

V. SUMMARY

We have presented an accurate calculation of the Mo\(_2\) ground state (\(X^1\Sigma^+_g\)) and first triplet excited state (\(a^3\Sigma^+\)). We use the phaseless AFQMC method with the truncated CASSCF trial wave function (AFQMC/CASSCF). Calculations were done using high-quality, realistic basis sets, and extrapolation to the CBS limit is performed. The resulting PECs and spectroscopic constants are in excellent agreement with experiment. Comparisons are made with other high-level quantum chemistry methods. We have also quantified the extent of strong electron correlations in both Cr\(_2\) and Mo\(_2\) molecules. Molybdenum is important in a variety of systems which can potentially exhibit exotic properties from strong correlation and topological effects. Our results can serve as a benchmark as theoretical and computational methods are developed and employed to treat such systems reliably.

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