New Measurements of the Transverse Beam Asymmetry for Elastic Electron Scattering from Selected Nuclei

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We have measured the beam-normal single-spin asymmetry $A_n$ in the elastic scattering of 1–3 GeV transversely polarized electrons from $^1$H and for the first time from $^4$He, $^{12}$C, and $^{208}$Pb. For $^1$H, $^4$He, and $^{12}$C, the measurements are in agreement with calculations that relate $A_n$ to the imaginary part of the two-photon exchange amplitude including inelastic intermediate states. Surprisingly, the $^{208}$Pb result is significantly smaller than the corresponding prediction using the same formalism. These results suggest that a systematic set of new $A_n$ measurements might emerge as a new and sensitive probe of the structure of heavy nuclei.

Traditionally, fixed-target electron scattering has been analyzed in terms of the one-boson (photon or $Z$) exchange approximation. For scattering off heavy nuclei, distorted waves, based on solutions to the Dirac equation in the strong electric field of the nucleus, are also required to describe the data. Recently, the inclusion of the exchange of one or more additional photons has been necessary for the interpretation of precision data. The electric form factors $G_F$ extracted in elastic electron-proton scattering using two different techniques, Rosenbluth separation and polarization observables, were inconsistent [1–3]. The latter should be less sensitive to higher-order electromagnetic effects, and calculations including two-photon exchange provide a plausible explanation for the difference [4–8]. Another example is corrections to the parity-violating asymmetry $A_{PV}$ in the same process, which provides a measurement of the weak charge of the proton and serves as a sensitive test of the electroweak theory. For interpreting $A_{PV}$, $\gamma$-$Z$ box diagrams are important [9], as well as two-photon exchange [10]. Theoretical calculations of two-photon exchange processes are difficult, because an integral over all off-shell proton intermediate state contributions must be made.

The effect of the extra boson is relatively small on the measured cross section or asymmetry for the above examples. On the other hand, the beam-normal spin asymmetry $A_n$ for elastic electron scattering at GeV energies is dominated by two (or more) $\gamma$ exchange. Several measurements of $A_n$ at GeV energies for the proton have been reported [11–14]. Several theoretical papers report computed values of $A_n$ that are in qualitative agreement with the data when they include the effects of inelastic intermediate hadronic states [15–18].

The beam-normal, or transverse asymmetry, $A_n$ is a direct probe of higher-order photon exchange as time-reversal symmetry dictates that $A_n$ is zero at first Born approximation. Afanasev et al. [4] and Gorchtein and Horowitz [19] have calculated $A_n$, in a two-photon exchange approximation, but including a full range of intermediate excited states. Gorchtein and Horowitz predict that $A_n$ scales roughly as the ratio of mass number $A$ to $Z$ and is not strongly $Z$-dependent. In contrast, Cooper and Horowitz [20] calculate Coulomb distortion effects and work to all orders in photon exchanges by numerically solving the Dirac equation. However, they consider only the elastic intermediate state. They find that elastic
intermediate state contributions, while in general small, increase strongly with $Z$.

To predict $A_n$ for nuclear targets, Afanasev used a unitarity-based model [18] with the total photoproduction cross section and the Compton slope as input; his prediction for $^4$He is consistent with the value of $A_n$ reported in this Letter. However, there is not yet a calculation of $A_n$ that includes both Coulomb distortion effects and a full range of excited intermediate states. Measuring $A_n$ as a function of $Z$ might reveal the role of dispersion effects relative to Coulomb distortions and motivate more detailed calculations. To this end, in this Letter, we report data on the beam-normal spin asymmetry $A_n$ on the targets $^1$H, $^4$He, $^{12}$C, and $^{208}$Pb.

To observe the beam-normal single-spin asymmetry, the electron beam-spin vector $\vec{P}_e$ must have a component normal to the scattering plane defined by the unit vector $\vec{k}$ perpendicular to the plane, where $\vec{k} = k/k; \vec{k} = \vec{k}_x \times \vec{k}_y$, where $\vec{k}_x$ and $\vec{k}_y$ are, respectively, the incident and scattered electron momenta. The measured beam-normal single-spin asymmetry is then defined as $A_{m1} = (\sigma_1 - \sigma_2)/(\sigma_1 + \sigma_2)$, where $\sigma_{1(2)}$ is the cross section for beam electron spin parallel (antiparallel) to $\vec{k}$. The measured asymmetry $A_{m1}$ is related to $A_n$ by

$$A_{m1} = A_n \vec{P}_e \cdot \vec{k},$$

where $\phi$ is the angle between $\vec{k}$ and $\vec{P}_e$: $\cos\phi = \vec{P}_e \cdot \vec{k}/|P_e|$.

The measurements were carried out in Hall A at the Thomas Jefferson National Accelerator Facility. The data were obtained as a part of a study of systematic uncertainties for three experiments designed to measure $A_{PV}$ in elastic electron scattering, since $A_n$ can contribute to the extracted $A_{PV}$ if the beam polarization has a transverse component and the apparatus lacks perfect symmetry.

The data were obtained in 2004 for the $^1$H and $^4$He targets where the primary goal was to measure $A_{PV}$ in order to determine the strange form factors in the nucleon [21,22]. The $^{12}$C and $^{208}$Pb data were obtained in 2010 where the goal was to determine the radius of the distribution of neutrons [23,24]. The kinematics for each target is given in Table I: the central acceptance angle of the spectrometers $\theta$, the beam energy $E_b$, the acceptance-averaged 4-momentum transfer $Q^2$, and the average accepted $\cos\phi$ [Eq. (1)]. The uncertainties in $Q^2$ were 1% for the $^1$H and $^4$He data and 1.5% for the $^{12}$C and $^{208}$Pb data [21–23].

All of the targets except $^{12}$C were cooled with helium gas at about 20 K. The LH$_2$ and high pressure He targets featured rapid vertical flow of the fluid. In addition, the beam was rastered over a 4 mm $\times$ 4 mm square for all targets. The 0.55 mm thick isotopically pure $^{208}$Pb target was sandwiched between two 150 $\mu$m diamond foils, and the edges were cooled with the cold helium. Electrons elastically scattered from the targets were focused onto detectors in the focal plane of the Hall A high resolution spectrometers [25]. The transverse asymmetry is modulated by the sine of the azimuthal electron scattering angle, and so the electron polarization was set vertical. This ensured that the acceptance of the two spectrometers, which are symmetrically placed to accept horizontally scattered events, contained the maximum and minimum of the asymmetry. The momentum resolution of the spectrometers ensured that essentially only elastic events were accepted.

To measure the asymmetry, Cherenkov light was produced in a radiator and collected by a photomultiplier tube (PMT), whose output sent to an analog-to-digital converter and integrated over a fixed time period of constant helicity. These detectors had to withstand the radiation damage caused by the high signal flux and also provide a uniform response to the electrons so that integrating the signals did not increase fluctuations. For the $^{208}$Pb and $^{12}$C data, each spectrometer had two 3.5 cm by 14 cm quartz detectors oriented at 45° to the direction of the electrons in the spectrometer, one in front that was 5 mm thick and one behind that was 1 cm thick. For the $^1$H and $^4$He data, a five-layer sandwich of quartz and brass provided sufficient energy resolution.

The electron beam originated from a GaAs photocathode illuminated by circularly polarized light [26]. By reversing the sign of the laser circular polarization, the direction of the spin at the target could be reversed rapidly [27]. A half-wave ($\lambda/2$) plate was periodically inserted into the laser optical path which passively reversed the sign of the electron beam polarization. Roughly equal statistics were thus accumulated with opposite signs for the measured asymmetry, which suppressed many systematic effects. The direction of the polarization could be controlled by a Wien filter and solenoidal lenses near the injector [28]. The accelerated beam was directed into Hall A, where its intensity, energy, and trajectory on target were inferred from the response of several monitoring devices.

Each period of constant spin direction is referred to as a “window.” The beam monitors, target, detector components, and electronics were designed so that the fluctuations in the fractional difference in the PMT response between a pair of successive windows were dominated by scattered electron counting statistics. To keep spurious beam-induced asymmetries under control at well below the parts per million level, careful attention was given to the design and configuration of the laser optics leading to the photocathode [27].

<table>
<thead>
<tr>
<th>Target</th>
<th>$^1$H</th>
<th>$^4$He</th>
<th>$^{12}$C</th>
<th>$^{208}$Pb</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\theta$ (°)</td>
<td>6°</td>
<td>6°</td>
<td>5°</td>
<td>5°</td>
</tr>
<tr>
<td>$Q^2$ (GeV$^2$)</td>
<td>0.0989</td>
<td>0.0773</td>
<td>0.00984</td>
<td>0.00881</td>
</tr>
<tr>
<td>$E_b$ (GeV)</td>
<td>3.026</td>
<td>2.750</td>
<td>1.063</td>
<td>1.063</td>
</tr>
<tr>
<td>$\langle \cos\phi \rangle$</td>
<td>0.968</td>
<td>0.967</td>
<td>0.963</td>
<td>0.967</td>
</tr>
</tbody>
</table>
The spin-reversal rate was 30 Hz for the $^1$H and $^4$He data and 240 Hz for the $^{12}$C and $^{208}$Pb data. The integrated response of each detector PMT and beam monitor was digitized and recorded for each window. In the 30 Hz case, the raw spin-direction asymmetry $A_{\text{raw}}$ in each spectrometer arm was computed from the detector response normalized to the beam intensity for each window pair. At the faster reversal, quadruplets of windows with either of the patterns $++--$ or $+-+-$ were used to suppress the significant 60 Hz line noise. In either case, the sequence of these patterns was chosen with a pseudorandom number generator.

Loose requirements were imposed on beam quality, removing periods of beam intensity, position, or energy instability, removing about 25% of the total data sample. No spin-direction-dependent cuts were applied. Since we measure the difference between two horizontal detectors, the dominant source of noise due to the beam arose from position fluctuations in the horizontal direction, which change the acceptance of the spectrometers in opposite directions. Noise in the beam energy or current largely cancels. In contrast, a measurement of the sum of the detectors in each arm were of opposite sign as expected [Eq. (1) reverses sign]. After correcting for the $\lambda/2$ reversals, the magnitudes of $A_{\text{raw}}$ are consistent within statistical uncertainties. The reduced $\chi^2$ for a constant fit to the $A_{\text{raw}}$ runs is close to 1 for each target type. The average $A_{\text{beam}}$ corrections were negligible. The physics asymmetry $A_n$ is calculated from $A_{\text{raw}}$ by correcting for the beam polarization $P_e$, the average value of $\cos\phi$ as given in Table I, and the background subtractions from the Al windows in the LH$_2$ and $^4$He targets and the diamond surrounding the lead foil.

Nonlinearity in the PMT response was limited to 1% in bench tests that mimicked running conditions. The total relative nonlinearity between the PMT response and those of the beam intensity monitors was limited to 1.5% by studies. An acceptance correction accounted for the nonlinear dependence of the asymmetry with $Q^2$. A significant systematic uncertainty in $\langle Q^2 \rangle$ is in the determination of the absolute scale of $\theta_{\text{lab}}$. A nuclear recoil technique with a dedicated calibration run using a water cell target [22] was used to set a scale uncertainty on $\langle Q^2 \rangle$ of $<0.2\%$.

Beam polarization measurements $|P_x|$ in Eq. (1) were made during the runs for the four nuclei. The beam polarization was inferred from longitudinal polarization

FIG. 1. Plots of the asymmetries for carbon and lead. The top row shows for the $^{12}$C target the left high resolution spectrometer (HRS) and right HRS asymmetries in the left and right panels, respectively. The bottom row shows the same sequence for the $^{208}$Pb target. The data have been sign-corrected for the $\lambda/2$ plate insertions.
møller polarimeter gave $P_e$. For the $^1\text{H}$ beam/$^6\text{C}$ Accelerator Facility has been studied and determined to $\sim 3$ GeV (for $^4\text{He}$ and $^8\text{Pb}$) and $\sim 1$ GeV (for $^{12}\text{C}$ and $^{208}\text{Pb}$). In the last two rows of Table III, we see that the extracted $\hat{A}_n$ from the three lower $Z$ nuclei are consistent with this empirical trend, while the $^{208}\text{Pb}$ result is consistent with zero. The $^{208}\text{Pb}$ result is in strong disagreement with the theoretical prediction as shown in Fig. 2, which plots the measurement results and their predictions [19].

Motivated by this large observed disagreement, we initiate a discussion of the potential dynamics by first noting that the scattering angle for all four measurements was roughly the same (Table I). If dispersion corrections play a bigger role than predicted, one might expect larger disagreements for $A_n$ measurements taken at lower beam energy, as is the case for $^{12}\text{C}$ and $^{208}\text{Pb}$. However, the measured $A_n$ for $^{12}\text{C}$ is quite consistent with theoretical expectations. In Fig. 3, we plot the fractional difference between the measured values and the predictions of Ref. [19] as a function of $Z$. The trend suggests that Coulomb distortions are playing a very significant role at large $Z$, underscoring the potential interest in additional $A_n$ measurements with intermediate $Z$ nuclei.

In conclusion, we have measured the beam-normal single-spin asymmetry $A_n$ for $^1\text{H}$, $^4\text{He}$, $^{12}\text{C}$, and $^{208}\text{Pb}$ and find good agreement for $^1\text{H}$, $^4\text{He}$, and $^{12}\text{C}$ with the calculations in Ref. [19], which include a dispersion integral over intermediate excited states. However, they

We now discuss the observed trends of the first ever measurements of $A_n$ for target nuclei with $A > 2$. In our kinematic range, the calculations in Ref. [19] scale approximately with $Z, A,$ and $\sqrt{Q^2}$ as

$$A_n = \frac{\hat{A}_n Q A}{Z},$$

where $\hat{A}_n$ is approximately constant, with a small additional dependence on the incident beam energy $E_{\text{beam}}$: $\sim -25 \text{ ppm/GeV}$ for $E_{\text{beam}} \sim 3$ GeV (for $^1\text{H}$ and $^4\text{He}$) and $\sim -30 \text{ ppm/GeV}$ for $E_{\text{beam}} \sim 1$ GeV (for $^{12}\text{C}$ and $^{208}\text{Pb}$).

TABLE II. $A_{PV}$ uncertainty contributions in units of $10^{-6}$ or parts per million.

<table>
<thead>
<tr>
<th>Target</th>
<th>$^1\text{H}$</th>
<th>$^4\text{He}$</th>
<th>$^{12}\text{C}$</th>
<th>$^{208}\text{Pb}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>False asymmetry</td>
<td>0.14</td>
<td>0.11</td>
<td>0.02</td>
<td>0.12</td>
</tr>
<tr>
<td>Beam polarization</td>
<td>0.21</td>
<td>0.33</td>
<td>0.08</td>
<td>0.003</td>
</tr>
<tr>
<td>Linearity</td>
<td>0.07</td>
<td>0.15</td>
<td>0.06</td>
<td>0.004</td>
</tr>
<tr>
<td>Target windows</td>
<td>0.06</td>
<td>0.12</td>
<td>0.00</td>
<td>0.062</td>
</tr>
<tr>
<td>Total systematic</td>
<td>0.27</td>
<td>0.41</td>
<td>0.10</td>
<td>0.14</td>
</tr>
<tr>
<td>Statistical</td>
<td>1.52</td>
<td>1.39</td>
<td>0.36</td>
<td>0.21</td>
</tr>
</tbody>
</table>

A summary of the systematic and statistical uncertainties is shown in Table II. The central values of $A_n$ for each nucleus and the total combined statistical and systematic uncertainties added in quadrature are displayed in the first two rows of Table III. For $^1\text{H}$, our result is consistent with a previously reported measurement [12] for the same $Q^2$ but at a lower beam energy (0.85 GeV).

TABLE III. The measured $A_n$ and derived $\hat{A}_n$ values [Eq. (2)] for the four nuclei along with the corresponding total uncertainties $A/Z$ and $Q$.

<table>
<thead>
<tr>
<th>Target</th>
<th>$^1\text{H}$</th>
<th>$^4\text{He}$</th>
<th>$^{12}\text{C}$</th>
<th>$^{208}\text{Pb}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>$A_n$ (ppm)</td>
<td>$-6.80$</td>
<td>$-13.97$</td>
<td>$-6.49$</td>
<td>$0.28$</td>
</tr>
<tr>
<td>$\sigma(A_n)$ (ppm)</td>
<td>$\pm 1.54$</td>
<td>$\pm 1.45$</td>
<td>$\pm 0.38$</td>
<td>$\pm 0.25$</td>
</tr>
<tr>
<td>$\sqrt{Q^2}$ (GeV)</td>
<td>$0.31$</td>
<td>$0.28$</td>
<td>$0.099$</td>
<td>$0.094$</td>
</tr>
<tr>
<td>$A/Z$</td>
<td>1.0</td>
<td>2.0</td>
<td>2.0</td>
<td>2.53</td>
</tr>
<tr>
<td>$\hat{A}_n$ (ppm/GeV)</td>
<td>$-21.9$</td>
<td>$-24.9$</td>
<td>$-32.8$</td>
<td>$+1.2$</td>
</tr>
<tr>
<td>$\sigma(\hat{A}_n)$ (ppm/GeV)</td>
<td>$\pm 5.0$</td>
<td>$\pm 2.6$</td>
<td>$\pm 1.9$</td>
<td>$\pm 1.1$</td>
</tr>
</tbody>
</table>

FIG. 2 (color). Extracted physics asymmetries $A_n$ vs $Q$. Each curve, specific to a particular nucleus as indicated, is a theoretical calculation from Ref. [19].
are only to order $\alpha^2$ (two-photon exchange) and neglect Coulomb distortions. On the other hand, $A_n$ for $^{208}$Pb is measured to be very small and disagrees completely with theoretical calculations. Coulomb distortions were shown in Ref. [20] to grow rapidly with $Z$. On the other hand, the weight of dispersion corrections varies with the incident beam energy. Thus, new theoretical calculations that treat dispersion corrections and Coulomb distortions simultaneously as well as a systematic set of $A_n$ measurements for a range of $Z$ at various beam energies might lead to new insights into the structure of heavy nuclei.

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