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Observation of Electron-Antineutrino Disappearance at Daya Bay


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The Daya Bay Reactor Neutrino Experiment has measured a nonzero value for the neutrino mixing angle $\theta_{13}$ with a significance of 5.2 standard deviations. Antineutrinos from six 2.9 GWth reactors were detected in six antineutrino detectors deployed in two near (flux-weighted baseline 470 m and 576 m) and one far (1648 m) underground experimental halls. With a 43 000 ton–GWth–day live-time exposure in 55 days, 10 416 (80 376) electron-antineutrino candidates were detected at the far hall (near halls). The ratio of the observed to expected number of antineutrinos at the far hall is $R = 0.940 \pm 0.011^{(\text{stat})} \pm 0.004^{(\text{syst})}$. A rate-only analysis finds $\sin^2 2\theta_{13} = 0.092 \pm 0.016^{(\text{stat})} \pm 0.005^{(\text{syst})}$ in a three-neutrino framework.

It is well established that the flavor of a neutrino oscillates with time. Neutrino oscillations can be described by the three mixing angles ($\theta_{12}$, $\theta_{23}$, and $\theta_{13}$) and a phase of the Pontecorvo-Maki-Nakagawa-Sakata matrix, and two mass-squared differences ($\Delta m_{32}^2$ and $\Delta m_{21}^2$) [1,2]. Of these mixing angles, $\theta_{13}$ is the least known. The CHOOZ neutrino oscillation experiment obtained a 90%-confidence-level upper limit of 0.17 for $\sin^2 2\theta_{13}$ [3]. Recently, results from T2K (Tokai to Kamioka, Japan) [4], MINOS (Main Injector Neutrino Oscillation Search) [5], and Double Chooz [6] experiments have indicated that $\theta_{13}$ could be nonzero. In this Letter, we present the observation of a nonzero value for $\theta_{13}$.

For reactor-based experiments, an unambiguous determination of $\theta_{13}$ can be extracted via the survival probability of the electron-antineutrino $\bar{\nu}_e$ at short distances from the reactors,

$$P_{\text{sur}} = 1 - \sin^2 2\theta_{13} \sin^2(1.267 \Delta m_{31}^2 L/E),$$

where $\Delta m_{31}^2 = \Delta m_{32}^2 \pm \Delta m_{21}^2$, $E$ is the $\bar{\nu}_e$ energy in MeV and $L$ is the distance in meters between the $\bar{\nu}_e$ source and the detector (baseline).

The near-far arrangement of antineutrino detectors (ADs), as illustrated in Fig. 1, allows for a relative measurement by comparing the observed $\bar{\nu}_e$ rates at various baselines. With functionally identical ADs, the relative rate is independent of correlated uncertainties and uncorrelated reactor uncertainties are minimized.

A detailed description of the Daya Bay experiment can be found in Refs. [7,8]. Here, only the apparatus relevant to this analysis will be highlighted. The six pressurized water reactors are grouped into three pairs with each pair referred to as a nuclear power plant (NPP). The maximum thermal power of each reactor is 2.9 GW. Three underground experimental halls (EHs) are connected with horizontal tunnels. Two ADs are located in EH1 and one in EH2 (the near halls). Three ADs are positioned near the oscillation maximum in the far hall, EH3. The vertical overburden in equivalent meters of water (m.w.e.), the

![FIG. 1 (color online). Layout of the Daya Bay experiment. The dots represent reactors, labeled as D1, D2, L1, L2, L3, and L4. Six ADs, AD1–AD6, are installed in three EHs.](image)
simulated muon rate and average muon energy, and average distance to the reactor pairs are listed in Table I.

As shown in Fig. 2, the ADs in each EH are shielded with >2.5 m of high-purity water against ambient radiation in all directions. Each water pool is segmented into inner and outer water shields (IWS and OWS) and instrumented with photomultiplier tubes (PMTs) to function as Cherenkov-radiation detectors whose data were used by offline software to remove spallation neutrons and other cosmogenic backgrounds. The detection efficiency for long-track muons is >99.7% [7]. The water pool is covered with an array of resistive plate chambers (RPC).

The $\bar{\nu}_e$ is detected via the inverse $\beta$-decay (IBD) reaction, $\bar{\nu}_e + p \rightarrow e^+ + n$, in a gadolinium-doped liquid scintillator (Gd-LS) [9,10]. The coincidence of the prompt scintillation from the $e^+$ and the delayed neutron capture on Gd provides a distinctive $\bar{\nu}_e$ signature.

Each AD consists of a cylindrical, 5 m diameter stainless steel vessel (SSV) that houses two nested, UV-transparent acrylic cylindrical vessels. A 3.1 m diameter inner acrylic vessel (IAV) holds 20 t of liquid scintillator (LS) inside a 4 m diameter outer acrylic vessel (OAV). Between the SSV and OAV, 37 t of mineral oil (MO) shields the LS and Gd-LS from radioactivity. IBD interactions are detected by 192 Hamamatsu R5912 PMTs. A black radial shield and specular reflectors are installed on the vertical detector walls and above and below the LS volume, respectively. Gd-LS and LS are prepared and filled into ADs systematically to ensure all ADs are functionally identical [7]. Three automated calibration units (ACUs) mounted on the SSV lid allow for remote deployment of a light-emitting diode, a $^{68}$Ge source, and a combined source of $^{241}$Am - $^{13}$C and $^{60}$Co into the Gd-LS and LS liquid volumes along three vertical axes.

The results are based on data taken from 24 December 2011 to 17 February 2012. A blind analysis strategy was adopted, with the baselines, the thermal-power histories of the cores, and the target masses of the ADs hidden until the analyses were frozen. Triggers were formed from the number of PMTs with signals above a ~0.25 photoelectron (pe) threshold (NHIT) or the charge sum of the over-threshold PMTs (ESUM). The AD triggers were NHIT > 45 or ESUM ≥ 65 pe. The trigger rate per AD was <280 Hz with a negligible trigger inefficiency for IBD candidates. The data consist of charge and timing information for each PMT, and were accumulated independently for each detector. To remove systematic effects due to reactor flux fluctuations, only data sets with all detectors in operation were used.

The energy of each trigger in an AD was reconstructed based on the total photoelectrons collected by the PMTs. The energy calibration constant, ~163 pe/MeV for all ADs and stable throughout the data collection period, was determined by setting the energy peak of the $^{60}$Co source deployed at each AD center to 2.506 MeV. Vertex reconstruction was based on center-of-charge, defined as the charge-weighted-mean of the coordinates of all PMTs. The mapping from center-of-charge to vertex was done by analytic corrections determined using data collected with $^{60}$Co sources deployed at various points within the AD. A vertex-dependent correction to energy (<10%) and a constant factor (0.988) were applied equally to all ADs to correct for geometrical effects and energy nonlinearity between the $^{60}$Co and the neutron capture on Gd ($\mu_{\text{Gd}}$), determined by the $^{60}$Co and Am-C sources at the detector center. An independent energy calibration that utilized the peak of the nGd from spallation neutron to set the energy scale and templates derived from Monte Carlo simulations (MC) for vertex reconstruction, gave consistent performance [7]. The energy resolution was (7.5/$\sqrt{E(\text{MeV})}$ + 0.9)% for all 6 ADs.

IBD events were selected with the following criteria: $0.7 < E_p < 12.0$ MeV, $6.0 < E_d < 12.0$ MeV, $1 < \Delta t < 200$ μs, the prompt-delayed pair was vetoed by preceding

<table>
<thead>
<tr>
<th>Overburden</th>
<th>$R_\mu$</th>
<th>$E_\mu$</th>
<th>D1,2</th>
<th>L1,2</th>
<th>L3,4</th>
</tr>
</thead>
<tbody>
<tr>
<td>EH1</td>
<td>250</td>
<td>1.27</td>
<td>57</td>
<td>364</td>
<td>857</td>
</tr>
<tr>
<td>EH2</td>
<td>265</td>
<td>0.95</td>
<td>58</td>
<td>1348</td>
<td>480</td>
</tr>
<tr>
<td>EH3</td>
<td>860</td>
<td>0.056</td>
<td>137</td>
<td>1912</td>
<td>1540</td>
</tr>
</tbody>
</table>

**TABLE I.** Vertical overburden (m.w.e.), muon rate $R_\mu$ (Hz/m²), and average muon energy $E_\mu$ (GeV) of the three EHs, and the distances (m) to the reactor pairs.
muons if $t_d - t_{\mu ws} < 600 \mu s$, $t_d - t_{\mu AD} < 1000 \mu s$, or $t_d - t_{\mu sh} < 1 \text{ s}$, and a multiplicity cut that requires no additional $>0.7$ MeV trigger in the time range ($t_p - 200 \mu s, t_d + 200 \mu s$), where $E_p$ ($E_d$) is the prompt (delayed) energy and $\Delta t = t_d - t_p$ is the time difference between the prompt and delayed signals. Statistically consistent performance was achieved by an independent analysis that used different energy reconstruction, muon veto, and multiplicity cuts.

The inefficiency of the muon veto for selecting IBD events $(1 - \epsilon_\mu)$ was calculated by integrating the vetoed time of each muon with temporal overlaps taken into account. Inefficiency due to the multiplicity selection $(1 - \epsilon_m)$ was calculated by considering the probability that a random signal occurred near an IBD in time. The average values of $\epsilon_\mu \epsilon_m$ are given for each AD in Table II.

We considered the following kinds of background: accidental correlation of two unrelated signals, $\beta$-$n$ decay of $^9$Li-$^8$He produced by muons in the ADs, fast-neutron backgrounds produced by muons outside the ADs, $^13$C($\alpha, n$)$^{16}$O interactions, and correlated events due to the retracted Am-C neutron source in the ACUs. The estimated background rates per AD are summarized in Table II.

The accidental background was determined by measuring the rate of both prompt- and delayed-type signals, and then estimating the probability that two signals randomly satisfied the $\Delta t$ required for IBD selection. Additional estimates using prompt and delayed candidates separated by more than 1 ms or 2 m provided consistent results. The uncertainty in the measured accidental rate was dominated by the statistical uncertainty in the rate of delayed candidates.

The rate of correlated background from the $\beta$-$n$ cascade of $^9$Li-$^8$He decays was evaluated from the distribution of the time since the last muon using the known decay times for these isotopes [11]. The $^9$Li-$^8$He background rate as a function of the muon energy deposited in the AD was estimated by preparing samples with and without detected neutrons 10 $\mu$s to 200 $\mu$s after the muon. A 50% systematic uncertainty was assigned to account for the extrapolation to zero deposited muon energy.

An energetic neutron entering an AD can form a fast-neutron background by recoiling off a proton before being captured on Gd. By relaxing the $E_p < 12$ MeV criterion in the IBD selection, a flat distribution in $E_p$ was observed up to 100 MeV. Extrapolation into the IBD energy region gave an estimate for the residual fast-neutron background. A similar flat $E_p$ distribution was found in the muon-tagged fast-neutron sample produced by inverting the muon veto cut. Consistent results were obtained by scaling the muon-tagged fast-neutron rate with muon inefficiency, and by MC.

The $^{13}$C($\alpha, n$)$^{16}$O background was determined using MC after estimating the amount of $^{238}$U, $^{232}$Th, $^{227}$Ac, and $^{210}$Po in the Gd-LS from their cascade decays, or by fitting their $\alpha$-particle energy peaks in the data.

A neutron emitted from the 0.5 Hz Am-C neutron source in an ACU could generate a $\gamma$-ray via inelastic scattering in the SSV before subsequently being captured on Fe-Cr-Mn-Ni. An IBD was mimicked if both $\gamma$ rays from the scattering and capture processes entered the scintillating region. This correlated background was estimated using MC. The normalization was constrained by the measured rate of single delayed-type candidates from this source.

Table III is a summary of the absolute efficiencies and the systematic uncertainties. The uncertainties of the absolute efficiencies are correlated among the ADs. No relative efficiency, except $\epsilon_\mu \epsilon_m$, was corrected. All differences between the functionally identical ADs were taken as uncorrelated uncertainties.

The spill-in enhancement resulted when neutrons from IBD outside the target drift into the target, and was evaluated using MC. The spillout deficit (\~2.2\%) was included in the absolute Gd capture ratio. The Gd capture

| TABLE II. Signal and background summary. The background and IBD rates were corrected for the $\epsilon_\mu \epsilon_m$ efficiency. The no-oscillation predictions based on reactor flux analyses and detector simulation have been corrected with the best-fit normalization parameter in determining $\sin^2 2\theta_{13}$. |
|---------------------------------|---------|---------|---------|---------|---------|---------|
|                                | AD1     | AD2     | AD3     | AD4     | AD5     | AD6     |
| IBD candidates                 | 28935   | 28975   | 22466   | 3528    | 3436    | 3452    |
| No-oscillation prediction for IBD | 28647   | 29996   | 22335   | 3566.5  | 3573.0  | 3535.9  |
| Data acquisition live time (days) | 49.5530 | 49.6971 | 70.3899 | 0.8785  | 0.8800  | 0.8952  |
| $\epsilon_\mu \epsilon_m$     | 0.8019  | 0.7989  | 0.8363  | 0.9547  | 0.9543  | 0.9538  |
| Accidental signals (per day)   | 9.82 $\pm$ 0.06 | 9.88 $\pm$ 0.06 | 7.67 $\pm$ 0.05 | 3.29 $\pm$ 0.03 | 3.33 $\pm$ 0.03 | 3.12 $\pm$ 0.03 |
| Fast-neutron (per day)         | 0.84 $\pm$ 0.02 | 0.84 $\pm$ 0.28 | 0.74 $\pm$ 0.44 | 0.04 $\pm$ 0.04 | 0.04 $\pm$ 0.04 | 0.04 $\pm$ 0.04 |
| $^9$Li-$^8$He (per AD per day) | 3.1 $\pm$ 1.6 | 1.8 $\pm$ 1.1 | 0.16 $\pm$ 0.11 |
| Am-C correlated (per AD per day) | 0.2 $\pm$ 0.2 | 0.2 $\pm$ 0.2 | 0.2 $\pm$ 0.2 | 0.2 $\pm$ 0.2 | 0.2 $\pm$ 0.2 | 0.2 $\pm$ 0.2 |
| $^{13}$C($\alpha, n$)$^{16}$O background (per day) | 0.04 $\pm$ 0.02 | 0.04 $\pm$ 0.02 | 0.035 $\pm$ 0.02 | 0.03 $\pm$ 0.02 | 0.03 $\pm$ 0.02 | 0.03 $\pm$ 0.02 |
| IBD rate (per day)             | 714.17 $\pm$ 4.58 | 717.86 $\pm$ 4.60 | 532.29 $\pm$ 3.82 | 71.78 $\pm$ 1.29 | 69.80 $\pm$ 1.28 | 70.39 $\pm$ 1.28 |
The uncertainties obtained similar results on the background and relative recently calculated fluxes [17,18] (3.1% uncertainty) had little impact on the results. The thermal energy released per fission is given in Ref. [19]. Nonequilibrium corrections for long-lived isotopes were applied following Ref. [17]. Contributions from spent fuel [20,21] (~0.3%) were included as an uncertainty.

Thermal-power data provided by the power plant carry an uncertainty of 0.5% per core [22–24] that we conservatively treat as uncorrelated. The fission fractions were also provided for each fuel cycle as a function of burn-up, with a ~5% uncertainty from validation of the simulation [25,26]. A DRAGON [27] model was constructed to study the correlation among the fission rates of isotopes. The uncertainties of the fission fraction simulation resulted in a 0.6% uncorrelated uncertainty of the $\bar{v}_e$ yield per core. The baselines have been surveyed with a Global Positioning System and modern theodolites to a precision of 28 mm. The uncertainties in the baseline and the spatial distribution of the fission fractions in the core had a negligible effect to the results. Figure 3 presents the background-subtracted and efficiency-corrected IBD rates in the three EHs. Relative reactor flux predictions are shown for comparison.

The $\bar{v}_e$ rate in the far hall was predicted with a weighted combination of the two near-hall measurements assuming no oscillation. The weights were determined by the thermal power of each reactor and its baseline to each AD. We observed a deficit in the far hall, expressed as a ratio of observed to expected events,

$$R = 0.940 \pm 0.011(\text{stat.}) \pm 0.004(\text{syst.}).$$

In addition, the residual reactor-related uncertainties were found to be 5% of the uncorrelated uncertainty of a single core.

This analysis was independent of reactor flux models. The $\bar{v}_e$ yield per fission [12] was not fixed when determining $\sin^2 2\theta_{13}$. Whether we used the conventional Institut Laue-Langevin fluxes [13–16] (2.7% uncertainty) or the recently calculated fluxes [17,18] (3.1% uncertainty) had little impact on the results. The thermal energy released per fission is given in Ref. [19]. Nonequilibrium corrections for long-lived isotopes were applied following Ref. [17].

Table: Summary of absolute efficiencies, and correlated and uncorrelated systematic uncertainties.

<table>
<thead>
<tr>
<th>Detector</th>
<th>Efficiency</th>
<th>Correlated</th>
<th>Uncorrelated</th>
</tr>
</thead>
<tbody>
<tr>
<td>Target Protons</td>
<td>99.98%</td>
<td>0.01%</td>
<td>0.01%</td>
</tr>
<tr>
<td>Flasher cut</td>
<td>90.9%</td>
<td>0.6%</td>
<td>0.12%</td>
</tr>
<tr>
<td>Delayed-energy cut</td>
<td>99.88%</td>
<td>0.10%</td>
<td>0.01%</td>
</tr>
<tr>
<td>Multiplicity cut</td>
<td>98.6%</td>
<td>0.12%</td>
<td>0.01%</td>
</tr>
<tr>
<td>Capture-time cut</td>
<td>96.8%</td>
<td>0.02%</td>
<td>&lt;0.01%</td>
</tr>
<tr>
<td>Gd capture ratio</td>
<td>83.8%</td>
<td>0.8%</td>
<td>&lt;0.1%</td>
</tr>
<tr>
<td>Spill in</td>
<td>105.0%</td>
<td>1.5%</td>
<td>0.02%</td>
</tr>
<tr>
<td>Live time</td>
<td>100.0%</td>
<td>0.002%</td>
<td>&lt;0.01%</td>
</tr>
<tr>
<td>Combined</td>
<td>78.8%</td>
<td>1.9%</td>
<td>0.2%</td>
</tr>
</tbody>
</table>

Energy per fission:
- Correlated: 0.2%
- Uncorrelated: 0.5%

IBD reaction per fission:
- Correlated: 3%
- Fission fraction: 0.6%
- Uncorrelated: 0.3%

Combined:
- Correlated: 3%
- Uncorrelated: 0.8%

Graph: Daily average measured IBD rates per AD in the three experimental halls as a function of time. Data between the two vertical dashed lines were used in this analysis. The solid curves represent no-oscillation predictions based on reactor flux analyses and detector simulation for comparison. The predictions have been corrected with the best-fit normalization parameter in determining $\sin^2 2\theta_{13}$. The predictions are shown for comparison.
The value of $\sin^2 2\theta_{13}$ was determined with a $\chi^2$ constructed with pull terms accounting for the correlation of the systematic errors [28],

$$\chi^2 = \frac{\sum_{d=1}^{6} [M_d - T_d(1 + \varepsilon + \sum_r \omega^r_d \alpha_r + \varepsilon_d) + \eta_d]^2}{M_d + B_d}$$

$$+ \sum_r \frac{\alpha^2_r}{\sigma^2_r} + \frac{6}{\sum_{d=1}^{6} \left( \frac{\varepsilon^2_d}{\sigma^2_d} + \frac{\eta^2_d}{\sigma^2_d} \right)}$$

(2)

where $M_d$ are the measured IBD events of the $d$th AD with backgrounds subtracted, $B_d$ is the corresponding background, $T_d$ is the prediction from neutrino flux, MC, and neutrino oscillations [29], $\omega^r_d$ is the fraction of IBD contribution of the $r$th reactor to the $d$th AD determined by baselines and reactor fluxes. The uncertainties are listed in Table III. The uncorrelated reactor uncertainty is $\sigma_r (0.8\%)$, $\sigma_d (0.2\%)$ is the uncorrelated detection uncertainty, and $\sigma_B$ is the background uncertainty listed in Table II. The corresponding pull parameters are ($\alpha_r, \varepsilon_d, \eta_d$). The detector- and reactor-related correlated uncertainties were not included in the analysis; the absolute normalization $\varepsilon$ was determined from the fit to the data. The best-fit value is

$$\sin^2 2\theta_{13} = 0.092 \pm 0.016\text{(stat.)} \pm 0.005\text{(syst.)},$$

with a $\chi^2$/NDF of 4.26/4 (where NDF is the number of degrees of freedom). All best estimates of pull parameters are within its 1 standard deviation based on the correspond-

ing systematic uncertainties. The no-oscillation hypothesis is excluded at 5.2 standard deviations.

The accidental backgrounds were uncorrelated while the Am-C and ($\alpha, n$) backgrounds were correlated among ADs. The fast-neutron and $^9$Li-$^8$He backgrounds were site-wide correlated. In the worst case where they were correlated in the same hall and uncorrelated among different halls, we found the best-fit value unchanged while the systematic uncertainty increased by 0.001.

Figure 4 shows the measured numbers of events in each detector, relative to those expected assuming no oscillation. The 6.0% rate deficit is obvious for EH3 in comparison with the other EHs, providing clear evidence of a nonzero $\theta_{13}$. The oscillation survival probability at the best-fit values is given by the smooth curve. The $\chi^2$ versus $\sin^2 2\theta_{13}$ is shown in the inset.

The observed $\bar{\nu}_e$ spectrum in the far hall is compared to a prediction based on the near-hall measurements in Fig. 5. The disagreement of the spectra provides further evidence of neutrino oscillation. The ratio of the spectra is consistent with the best-fit oscillation solution of $\sin^2 2\theta_{13} = 0.092$ obtained from the rate-only analysis [31].

In summary, with a 43,000 ton–GWth–day live-time exposure, 10,416 reactor antineutrinos were observed at the far hall. Comparing with the prediction based on the near-hall measurements, a deficit of 6.0% was...
found. A rate-only analysis yielded $\sin^2 2\theta_{13} = 0.092 \pm 0.016$(stat.) $\pm 0.005$(syst.). The neutrino mixing angle $\theta_{13}$ is nonzero with a significance of 5.2 standard deviations.

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*Deceased.

[29] The survival probability used in the $\chi^2$ was $P_{\text{sur}} = 1 - \sin^2 2\theta_{13} \sin^2(2\Delta m^2_{\odot}/L/E) \cos^2 \delta_{\odot} - \sin^2 2\theta_{13} \sin^2(2\Delta m^2_{\odot}/L/E) \cos^2 \delta_{\odot}$, where $\Delta m^2_{\odot}$ = 2.32 $\times 10^{-5}$ eV$^2$, $\sin^2 2\theta_{13} = 0.861 \pm 0.026$, and $\Delta m^2_{\odot} = 7.59 \pm 0.20 \times 10^{-5}$ eV$^2$. The uncertainty in $\Delta m^2_{\odot}$ has not been included in the fit. The fit $\sin^2 2\theta_{13}$ will change by +0.0007 and $-0.0004$ when $\Delta m^2_{\odot}$ changes by 1 standard deviation.
[31] Without correcting for the nonlinearity of the detector response, we have performed a preliminary shape analysis that yielded a consistent result for $\sin^2 2\theta_{13}$. 