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#### CAUSAL DISTRIBUTED ASSERT STATEMENTS

A Dissertation

Presented to

The Faculty of the Department of Computer Science

The College of William and Mary in Virginia

In Partial Fulfillment

Of the Requirements for the Degree of

**Doctor of Philosophy** 

by

Sharon J. Simmons

1**999** 

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#### ABSTRACT

Monitoring a program's execution is fundamental to the debugging, testing and maintenance phases of program development. This research addresses the issue of monitoring the execution of a distributed program. In particular, we are concerned with efficient techniques for evaluating global state predicates for distributed programs. The global state of a distributed program is not well-defined, making the monitoring task complex compared to that of a sequential programs. Processes of a distributed program execute concurrently, and the events of the program cannot be totally ordered. Each process has its own local memory, and the local memories are physically separate.

Despite the difficulties of defining a distributed computation's states. monitoring a distributed program requires reasoning about constituent processes' execution as a single collective entity. We have extrapolated the semantics of the sequential program's assert statement into the distributed context. A distributed assert statement is a global predicate that is anchored at a control point of one processes, and that is evaluated when that process executes the assert.

We have developed a runtime method for monitoring both stable and unstable properties that does not disrupt the computation of the distributed system. A distributed assert statement is evaluated with that statement's *causal global state* which incorporates the state of the system as a whole as it may have causal impact upon the assert statement. A runtime protocol has been implemented that constructs the causal global state and evaluates the assert statement. No additional synchronization or message passing is imposed on the distributed application although some message sizes are increased to propaga te state information. The causal global state is immediately available providing real-time feedback.

## CAUSAL DISTRIBUTED ASSERT STATEMENTS

## Chapter 1

## Introduction

#### 1.1 Monitoring Sequential Programs

Observing a program's execution is fundamental to the debugging, testing and maintenance phases of program development. Debugging is premised on the ability to examine the value of a variable at chosen points during the execution of a program. Testing involves detecting erroneous threads of execution and invalid variable values. Maintenance relies on the ability to follow a program's execution and detect deviations from anticipated behavior.

The ability to observe a sequential program's execution is straightforward since a single thread of execution defines a total temporal order on the program's atomic operations. The execution of each atomic operation results in a new program state, where a program state is a function from variables to values [12]. An ordered sequence of states is defined while the program is executing, and at any point of execution the state of the program is immediately available since all variable values are stored in the same local memory. Debugging, testing and maintenance examine a program's execution by comparing states with expected behavior. One common method of conveying the expected behavior of a program utilizes state predicates. A predicate used in this manner is a boolean function on a program state and is evaluated by replacing variables of the predicate with their state values [12]. Predicate evaluation is straightforward in a sequential program since a state is well-defined and immediately available.

Choosing appropriate predicates is dependent on the application and the activities monitored. Predicates can be chosen to detect program malfunction and, if skillfully designed, relay a strong clue about the location of the bug leading to the failure. Particular points of a program's execution may be crucial, and predicates should be designed for evaluation at these points. Evaluating a predicate after the execution of an identified atomic operation is consistent with Hoare-style axiomatic program verification techniques [14]. Complex verification statements such as loop invariants. upon which a proof of partial correctness is usually hinged, make obvious candidates for conversion into predicates. Debugging breakpoints and diagnostic print statements indicate positions for developing appropriate predicates. Independent of the application, predicates are a powerful monitoring tool throughout the program's life cycle.

#### **1.2 Monitoring Distributed Systems**

This research addresses the issue of monitoring the execution of a distributed program. In particular, we are concerned with efficient techniques for evaluating global state predicates for distributed programs. The global state of a distributed program is not well-defined,

making the task of monitoring complex compared to sequential programs. Processes of a distributed program execute concurrently, and the events of the program cannot be totally ordered. Each process has its own local memory, and the local memories are physically separate from one another. A process is only immediately aware of its own local state. Access to the state of a remote process requires communication and incurs a delay which is usually substantial and often unpredictable.

#### 1.2.1 System Model

A sequential program's execution and the execution of a single process of a distributed program are similar. The  $i^{th}$  atomic operation or event of a sequential program is represented by  $e_i$ , and the resulting state is represented by  $S_i$ . The execution of a sequential program is modeled as

$$\sigma = S_0 \xrightarrow{e_1} S_1 \xrightarrow{e_2} S_2 \dots$$

The notation  $S_{i-1} \xrightarrow{e_i} S_i$  denotes the execution of event  $e_i$  which causes a transition from state  $S_{i-1}$  to  $S_i$ .

A distributed system consists of a fixed number of distinct processes  $\Pi = \{P_0, \ldots, P_{N-1}\}$ . These processes share no memory and interact only via message passing. Each process consists of a totally ordered sequence of atomic events. The  $i^{th}$  event of  $P_j$  is represented by  $e_j^i$ , and the resulting local state is represented by  $S_j^i$ . The execution of  $P_j$  is modeled as

$$\sigma/j = S_j^0 \xrightarrow{\epsilon_j^1} S_j^1 \xrightarrow{\epsilon_j^2} S_j^2 \dots$$

In both a process and a sequential program, it is possible to say which event or state happened before another event or state since the events of both are totally ordered. The execution of a distributed program is viewed as a set of events  $E = E_0 \cup \cdots \cup E_{N-1}$  where  $E_i$  represents the events of  $P_i$ , and an irreflexive partial order is defined on these events [19]:

$$\rightarrow \subseteq E \times E$$
.

The  $\rightarrow$  relation is commonly referred to as happened before. For  $e, f \in E, e \rightarrow f$  if and only if e has potential causal impact upon f.

#### 1.3 The Happens Before Relation

Interprocess communication defines the happens before relationship among events on different processes. Asynchronous communication occurs when a process places a message "on the network." and continues execution. The process receiving the message blocks until it receives the message, then continues execution.

In an asynchronous communication regime.  $\rightarrow$  is the smallest relation satisfying the following three conditions: (1) if e and f are events in the same process, and e happens before f, then  $e \rightarrow f$ ; (2) if e is the sending of a message and f is the receipt of the same message, then  $e \rightarrow f$ ; and (3) if  $e \rightarrow f$  and  $f \rightarrow g$ , then  $e \rightarrow g$ .

If  $e \to f$ , we say that e causally precedes f and that f causally succeeds e. If  $e \not\to f$ and  $f \not\to e$ , then we say that e and f are causally unrelated or concurrent, denoted e || f, and neither can causally affect the other.

#### 1.3.1 Asynchronous Message Passing Library

We have developed a library of asynchronous communication functions for writing distributed programs that communicate asynchronously. Each process's program is written in the programming language C[16] with the addition of the asynchronous communication functions for message passing between processes. Appendix B covers in detail the asynchronous functions, but the two of primary interest are *async\_send* and *async\_recv*. The function async\_send has the following format:

```
async_send(i, msg, len).
```

The message pointed to by msg of length len is sent to process i. If i is -1, the message is broadcast to all the processes of the distributed program. The function async\_recv has the following format:

async\_recv(i, msg, len. waitsecs).

A message from process i is copied into the address msg. The length of the received message is *len*. If a message does not arrive within *waitsecs*, async\_recv returns with a value of -1. If i is -1, the message is accepted from any process of the distributed program. If *waitsecs* is 0, the process waits until the message is received. When presenting example programs, only the fields of i and msg for both async\_send and async\_recv will be indicated. The field *waitsecs* of async\_recv is assumed to be 0 unless otherwise indicated.

The asynchronous library routines implement reliable FIFO (First In First Out) communication by default. Unreliable or non-FIFO communication can be configured by functions

described in the appendix. The example asynchronous distributed programs that appear in this document are based on reliable and FIFO communication unless specified otherwise.

#### 1.3.2 Partial Order of Events

When a distributed program executes, a *partial order* of the program events is defined. The order is not total because some events on different processes are causally unrelated. Figure 1.1 is a distributed program of two asynchronously communicating processes. The dots denote statements that are not relevant to the communication. A time-space diagram of the program's execution is given in figure 1.2. Each vertical line corresponds to a process's execution where the direction of the line indicates time increasing, and each tick on that execution line corresponds to an event. A diagonal arrow between two processes denotes a communication. The following are some of the concurrent ( $\parallel$ ) and causal ( $\rightarrow$ ) relationships that exist between the program's events:

| Concurrent  | <u>Causal</u>  |
|---|--|
| $\begin{array}{c} e_0^3 \parallel e_1^1 \\ e_0^1 \parallel e_1^1 \\ e_0^5 \parallel e_1^6 \\ e_0^6 \parallel e_1^8 \end{array}$ | $e_0^1  ightarrow e_1^2  ightarrow e_1^2  ightarrow e_1^2  ightarrow e_1^2  ightarrow e_1^0  ightarrow e_0^1  ightarrow e_0^1  ightarrow e_1^0  ightarrow e_1^0$ |

#### **1.3.3 Multiple Partial Orders**

The communication of a distributed program is classified as defining either a *single* partial order or *multiple* partial orders. The classification is based on the control constructs and

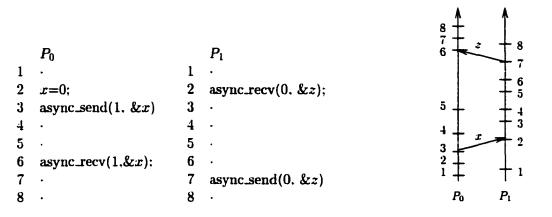


Figure 1.1: Asynchronous program

Figure 1.2: Space-time diagram

the communication functions they affect. The remaining statements of a process do not affect the partial order, and therefore are ignored.

If none of the processes have control constructs affecting the communication functions. the classification is a single partial order. If one or more of the processes have a control construct selecting among multiple communication functions, the classification is multiple partial orders. The partial order defined when the distributed program executes may differ according to which communication function is selected by the control construct.

Figure 1.3 is an example of a distributed program that is classified as defining multiple partial orders. The if/else control construct of  $P_0$  selects one of the two groups of communications functions to execute. The two possible partial orders are shown in figure 1.4. The function async\_send(1,w) is represented by *i*. function async\_send(2,w) is presented by *j*. function async\_recv(0,*y*) is represented by *k*, and function async\_recv(0,*z*) is represented by *l*.

```
P_0
                                             P_1
                                                                                             P<sub>2</sub>
:
                                                                                             :
w = i + 1
                                            \operatorname{async\_recv}(0,y);
                                                                                             \operatorname{async\_recv}(0,z)
                                                                                             :
if (w > 0)
 \operatorname{async\_send}(1, w);
 \operatorname{async\_send}(2, w);
else
  \operatorname{async\_send}(2, w);
  async_send(1, w):
:
```



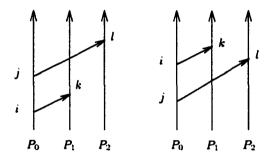


Figure 1.4: Space-time diagrams

#### 1.4 Outline of the Dissertation

Chapter two presents several distributed programs that will be used in discussing distributed monitoring methods. The programs range from a single partial order program with repeating communication patterns to a multiple partial orders program with complex communication patterns.

In chapter three we review well-known monitoring methods that appear in the literature. Problems that these monitoring methods incur are discussed. Both runtime and postmortem methods are reviewed. In chapter four our methodology for monitoring a distributed system is presented. The terminology and notation corresponding to our methodology is defined. This chapter also contains our initial algorithms.

Chapter five examines the affects of our initial algorithm to the execution of a distributed program and defines the messages that are sufficient for implementing our method of monitoring a distributed system. Chapters six and seven present algorithms for optimizing our initial results.

In chapter eight we apply our methodology for examining the execution of a distributed program to the programs of chapter two. Chapter nine concludes with possible avenues for continuing our research.

## Chapter 2

## **Distributed Programs**

Five distributed programs appear throughout this document to demonstrate and clarify concepts for monitoring distributed programs. These programs are described in detail in this chapter. The communication complexity of the programs varies greatly and is discussed with each program.

#### 2.1 Set partition

SETPART, the set partition program, by Dijkstra [7] partitions disjoint integer sets S and T. SETPART exchanges an element of S with an element of T until the elements of S are less than the elements of T. The original sizes of S and T are maintained after each exchange. SETPART consists of two distributed processes,  $P_0$  and  $P_1$ .  $P_0$  maintains S, and  $P_1$  maintains T. Processes  $P_0$  and  $P_1$  exchange an integer to determine if the sets are already partitioned correctly, then  $P_0$  initiates an integer exchange with  $P_1$  if there exists an element of S that is greater than the element previously received from  $P_1$ . For the exchange,  $P_0$  sends the maximum element of S to  $P_1$  and removes this value from its set.

 $P_1$  receives the integer from  $P_0$  and adds this integer to T, then  $P_1$  sends the minimum element of T to  $P_0$  and removes this minimum value from its set T.  $P_0$  receives the integer from  $P_1$  and adds this integer to S.  $P_0$  continues to initiate an exchange until it determines that the sets are partitioned correctly. If the last value  $P_0$  receives from  $P_1$  is greater than or equal to the maximum of S, then no element of T is less than any element of S. And  $P_0$ can conclude that partitioning is complete.

Set Partitioning's communication behavior exhibits conversational continuity [31]. which is interactive communication between processes where a continuously repeating communication pattern is formed. The number of communications between the SETPART processes is dependent on the input data, but the communication pattern is static. Figure 2.1 is the distributed SETPART program for  $P_0$  and  $P_1$ . The function **max** returns the maximum integer of the operand set, and the function **min** returns the minimum integer of the operand set.

| P <sub>0</sub> :: |                                 | P1:: |                           |
|-------------------|---------------------------------|------|---------------------------|
| 1                 | $\mathrm{mx} = \mathrm{max}(S)$ | 14   | while(true)               |
| 2                 | $async_send(1, mx)$             | 15   | $async_recv(0, y)$        |
| 3                 | $S = S - \{mx\}$                | 16   | $T = T \cup \{y\}$        |
| 4                 | $async_recv(1, x)$              | 17   | mn = min(T)               |
| 5                 | $S = S \cup \{\mathbf{x}\}$     | 18   | $async_send(0, mn)$       |
| 6                 | $\mathrm{mx} = \mathrm{max}(S)$ | 19   | $T = T - \{\mathrm{mn}\}$ |
| 7                 | while $(mx > x)$                | 20   | endwhile                  |
| 8                 | $async_send(1, mx)$             |      |                           |
| 9                 | $S = S - \{mx\}$                |      |                           |
| 10                | $async_recv(1, x)$              |      |                           |
| 11                | $S = S \cup \{\mathbf{x}\}$     |      |                           |
| 12                | $\mathrm{mx} = \mathrm{max}(S)$ |      |                           |
| 13                | endwhile                        |      |                           |

Figure 2.1: Algorithm for Set Partitioning Program

#### 2.2 Mutual Exclusion

The circulating token mutual exclusion protocol can be embedded in distributed processes' application code if global mutual exclusion control is needed. The protocol defines a logical cycle through the processes, and the communication pattern is not influenced by the distributed system's application.

```
P(i)::
  Ł
        do
  2
             \operatorname{async\_recv}((i + N - 1) \mod N, \operatorname{token}, waitsecs)
  3
             if message received
  4
                  if want_cs_i
  5
                      in_cs_i = true; critsec_i; want_cs_i = false
  5
                  endif
  7
                  \operatorname{async\_send}((i+1) \mod N. \operatorname{token})
  8
             else /* async_recv timed out */
  9
                  do_other,
  10
             endif
  11
        enddo
```

#### Figure 2.2: MUTEX

MUTEX [21]. shown in figure 2.2. is a token-based protocol for administering mutual exclusive critical section entry for a distributed system of N processes. The protocol allows only one process to enter its critical section at a time. Only one token exists in the system, and a process can neither create a token nor destroy the token. The processes are responsible for circulating the token around the system so that every process eventually receives the token. Process  $P_i$  receives the token from  $P_{((i+N-1)modN)}$  and sends the token to  $P_{((i+1)modN)}$ . A process indicates that it wants to enter its critical section by setting want\_cs to true. A process only enters its critical section when it receives the token and want\_cs is true. Immediately before the process enters its critical section, in\_cs is set to

true. Process  $P_i$  passes the token to its neighbor  $P_{(i+1) \mod N}$  either when  $P_i$  completes its critical section or when  $P_i$  does not want to enter its critical section.

#### 2.3 Bubble Sort

This distributed bubble sort algorithm is based on the odd-even transposition variation of the sequential bubble sort [43]. A total of q integers are sorted in ascending order with Nprocesses where N < q. The processes are connected in a logical ring so that  $P_i$ 's neighbors are  $P_{i-1}$  and  $P_{i+1}$ . Initially each process is assigned a list of q/N elements, and each list is sorted locally using a sequential sort.

The distributed sort consists of N phases, numbered 0 to N - 1. If the phase number is even, each even numbered process sends its sorted list to its higher numbered odd neighbor, and each odd numbered process sends its sorted list to its lower numbered even neighbor. Each process merges the received list with its own list and sorts the resulting list. Each odd numbered process retains the last q/N elements of the list as its sorted list, and each even numbered process retains the first q/N elements of the list as its sorted list.

If the phase number is odd, similar steps are followed as for an even phase number. Each odd numbered process sends its sorted list to its higher numbered even neighbor, and each even numbered process sends its sorted list to its lower numbered odd neighbor. Each process merges the received list with its own list and sorts the resulting list. Each even numbered process retains the last q/N elements of the list as its sorted list, and each odd numbered process retains the first q/N elements of the list as its sorted list. Processes 0 and N-1 do not participate in odd numbered phases.

After N phases are complete, all q numbers are sorted in ascending order where  $P_i$  has the elements  $i \times q/N$  through  $(i+1) \times q/N - 1$  of the sorted list. The bubble sort algorithm is shown in figures 2.3 and 2.4. Figure 2.5 shows the communication pattern for a bubble sort with a six process distributed system.

 $P_i$ ::

|    | integer pid. phase:                                       |  |  |
|----|---|--|--|
|    | arrays list. recv_list                                    |  |  |
| 1  | pid = process's id .                                      |  |  |
| 2  | read $q/N$ elements into list                             |  |  |
| 3  | sort list   |  |  |
| 4  | for $phase = 0$ to $N - 1$                                |  |  |
| 5  | if <i>phase</i> is even                                   |  |  |
| 6  | if <i>pid</i> is even                                     |  |  |
| 7  | $async\_send(pid + 1, list)$                              |  |  |
| 8  | $async_recv(pid + 1, recv\_list)$                         |  |  |
| 9  | <i>list</i> = merge_sort( <i>list</i> , recv_list, first) |  |  |
| 10 | else  |  |  |
| 11 | $async_send(pid - 1, list)$                               |  |  |
| 12 | $\operatorname{async\_recv}(pid - 1, recv\_list)$         |  |  |
| 13 | $list = merge\_sort(list.recv\_list. last)$               |  |  |
| 14 | endif   |  |  |
| 15 | endif   |  |  |
| 16 | if phase is odd && pid $!= 0$ && pid $!= N - 1$           |  |  |
| 17 | if <i>pid</i> is even                                     |  |  |
| 18 | $async_send(pid - 1, list)$                               |  |  |
| 19 | $async_recv(pid - 1, recv_list)$                          |  |  |
| 20 | $list = merge\_sort(list, recv\_list, last)$              |  |  |
| 21 | else  |  |  |
| 22 | async.send(pid + 1, list)                                 |  |  |
| 23 | $async_recv(pid + 1, recv_list)$                          |  |  |
| 24 | $list = merge\_sort(list, recv\_list, first)$             |  |  |
| 25 | endif   |  |  |
| 26 | endif   |  |  |
| 27 | endfor  |  |  |
|    |   |  |  |

Figure 2.3: Bubble Sort

merge\_sort(list, recv\_list, half)::

array merge\_list

- 1 merge\_list = merging of recv\_list and list
- 2 sort merge\_list
- 3 if half = first
- 4 return first half of elements in *merge\_list*
- 5 else
- 6 return last half of elements in merge\_list
- 7 endif

Figure 2.4: Local Sort

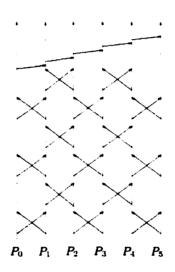


Figure 2.5: Distributed Bubble Sort

#### 2.4 Tree Sort

The N processes of the tree sort distributed program are arranged in a binary tree. The number of processes required for this sort is  $2^p - 1$ , where p > 1.  $2^{p-1}$  processes are leaf nodes. The process which is the root node of the tree initiates the sorting of q numbers, q > N. The root process splits the list in half and sends one half to each child process. If the receiving child process is not a leaf, it repeats the same steps as the root process. If the

number of elements in the list is odd, the left child receives one more element than the right child. If the receiving child process is a leaf node, it sorts the list and sends the sorted list to its parent process. Once a parent process has received both of its children's sorted lists, the parent merges the two lists into one sorted list. If the parent node is not the root node, it sends this sorted list to its parent. The sort is complete when the root node receives two sorted lists from its children, and merges the two into one sorted list of q numbers.

The tree sort algorithm is shown in figure 2.6. Figure 2.7 is the binary tree formed by 15 processes  $(p = 4) P_0 \dots P_{14}$ , and figure 2.8 shows the tree sort for the 15 processes.

| P <sub>0</sub> :: (root node) |   | Pi:: (parent node) |   |
|-------------------------------|---|--------------------|---|
|                               | integer child <sub>1</sub> .child <sub>2</sub><br>arrays list, list <sub>1</sub> ,list <sub>2</sub> |                    | integer child1.child2,parent<br>arrays list.list1,list2 |
| 1                             | read $q$ elements into <i>list</i>  | 1                  | async_recv(parent, list);                               |
| 2                             | split list into two halves: $list_1$ , $list_2$   | 2                  | split list into two halves: $list_1$ . $list_2$         |
| 3                             | $async\_send(child_1, list_1)$  | 3                  | $async\_send(child_1, list_1)$                          |
| 4                             | $\operatorname{async\_send}(child_2, list_2)$   | 4                  | $async\_send(child_2, list_2)$                          |
| 5                             | $async_recv(child_1, list_1)$   | 5                  | $async\_recv(child_1, list_1)$                          |
| 6                             | $\operatorname{async\_recv}(child_2, list_2)$   | 6                  | $async_recv(child_2, list_2)$                           |
| 7                             | merge $list_1$ and $list_2$ into $list$   | 7                  | merge $list_1$ and $list_2$ into $list$                 |
|                               |   | 8                  | async_send(parent, list)                                |
|                               |   |                    |   |

 $P_i$ :: (leaf node)

integer parent

array list

1 async\_recv(parent, list)

2 sort list

3 async\_send(parent.list)

Figure 2.6: Tree Sort

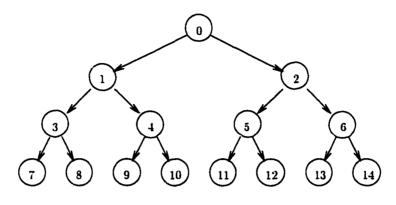
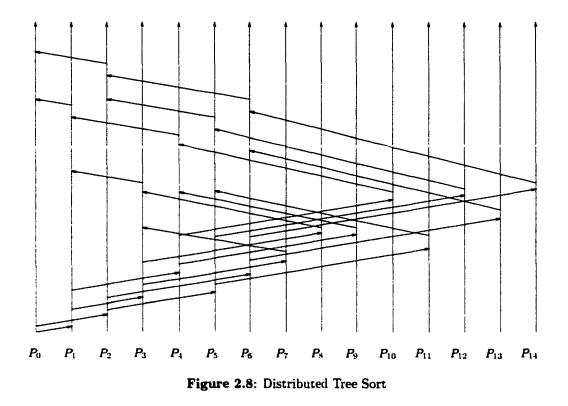


Figure 2.7: Distributed Processes

#### 2.5 Positive Ack/Retrans Protocol

The positive acknowledgement/retransmission protocol presented by Tannenbaum [41] enforces reliable communication between two communication nodes,  $CN_s$  and  $CN_r$ , on an unreliable physical transmission line. The communication node  $CN_s$  only sends data messages, and the communication node  $CN_r$  only receives data messages. Associated with  $CN_s$ is at least one host that supplies the data for the outgoing messages, and associated with  $CN_r$  is at least one host that consumes the data of the incoming messages. Once  $CN_s$  has transmitted a message, it does not send another message until the message is received by  $CN_r$  without errors. The node  $CN_r$  informs  $CN_s$  with an acknowledgement message when it has received a message without errors. If  $CN_s$  does not receive an acknowledgement within a predetermined amount of time, it retransmits the data message.

Since the communication line is unreliable, the data message and the acknowledgement message can be lost or corrupted. There exists a problem with retransmitting the data message when the acknowledgement message is lost. Suppose  $CN_r$  has received an uncor-



rupted data message and sends an acknowledgement. If the acknowledgement is lost,  $CN_s$  retransmit the same data message. The node  $CN_r$  does not realize the data message is being retransmitted and interrupts the retransmitted message as a new message.

One bit appended to the data message provides the information for the receiver to distinguish between a retransmitted message and a new message. The node  $CN_s$  maintains a bit by alternating the bit when it receives an acknowledgement and appends the current value of the bit on data messages. The node  $CN_r$  maintains a bit by alternating the bit when it receives a valid data message. The receiver only accepts a data message as a new message if the bit on the message matches its bit value. Following is the described protocol:

1**9** 

| Proc | edure CNs::                         |   |  |
|------|-------------------------------------|---|--|
|      | MsgBitSend : bit                    | /* alternating bit */                             |  |
|      | sbuffer: message                    | /* buffer for outgoing data message */            |  |
|      | event: (MsgArrival, CksumErr, Time  | Out) /* different interrupt events */             |  |
| 1    | MsgBitSend = 0                      | /* initialize alternating bit */                  |  |
| 2    | FromHost( <i>sbuffer</i> )          | /* get the data message from host */              |  |
| 3    | repeat                              |   |  |
| 4    | async_send( r, sbuffer, MsgBitSend) |   |  |
| 5    | StartTimer:                         | <pre>/* time to wait for acknowledgement */</pre> |  |
| 6    | wait(event)                         | * possibilities MsgArrival, CksumErr, TimeOut */  |  |
| 7    | if $event = MsgArrival$             |   |  |
| 8    | $async_recv(r, ack)$                | /* receive the acknowledgement */                 |  |
| 9    | FromHost(sbuffer)                   | /* an acknowledgment has arrived intact */        |  |
| 10   | inc(MsgBitSend)                     | /* increment by 1 then mod 2 */                   |  |
| 11   | endif                               | ,   |  |
| 12   | until doomsday                      |   |  |

**Procedure**  $CN_r$ :: MsgBitReceive : bit /\* alternating bit \*/ IncomingBit : bit /\* incoming message's bit \*/ rbuffer: message /\* buffer for incoming data message \*/ event: (MsgArrival, CksumErr) /\* different interrupt events \*/ 13 MsgBitReceive = 0/\* initialize alternating bit \*/ 14 repeat 15 wait(event) /\* possibilities MsgArrival, CksumErr \*/ 16 if event = MsgArrival/\* a valid message has arrived \*/ 17 async\_recv(s. rbuffer, IncomingBit) /\* accept the message \*/ 18 if IncomingBit = MsgBitReceive 19 ToHost(rbuffer) /\* pass the data to the host \*/ 20 inc(MsgBitReceive) /\* increment by 1 then mod 2 \*/ 21 endif 22 async\_send(s. acknowledgement) 23 endif 24 until doomsday

The **async\_send** command transmits a message (data message and bit) over the communication channel, and the **async\_recv** command accepts a message from the communication channel and assigns the data message to *rbuffer* and the bit to *IncomingBit*. Procedure StartTimer() starts the timer and enables the Timeout Event. Procedure Wait() waits for an event to happen, and returns the event type when one occurs. The procedure FromHost() fetches a data message from the host, and the procedure ToHost() delivers a data message to the host.

# Chapter 3

# **Monitoring Methods**

## 3.1 Global State

A partial order is defined on a distributed system's events when the system executes. The notion of a system state is complicated by the lack of a total order among events. An additional complication is the difficultly of capturing a system state since local memories are physically separate from one another. Despite the difficulties of a distributed computation's states, monitoring a distributed program requires reasoning about constituent processes' execution as a single collective entity. Previous work [28, 4, 38, 37, 29, 33] has defined a global state for unified reasoning about the distributed processes. A global state is analogous to "gluing" together local states, one from each process, such that the local states can happen at the same "time". The "gluing" produces one possible state of the system.

Global states provide a means to monitor a distributed system's execution with global predicates. A global predicate for a distributed system is comprised of relationships among variables from different processes. Once a global state is constructed, a global predicate is evaluated on this state. Constructing a global state and evaluating a predicate on that state helps in any rational scheme for debugging and monitoring the distributed program.

## **3.2 Runtime Methods**

Despite a global state's usefulness, problems exist with distributed system monitoring based on global states. A major problem is the difficulty of capturing a global state during the distributed system's execution.

Runtime methods of capturing a global state has been addressed by many researchers. Several papers that stand out in the literature are briefly described. Chandy and Lamport [4] were the first to define a global state as a global snapshot that could have occurred if all processes took a snapshot of their local states simultaneously. Their global snapshot algorithm assumes FIFO asynchronous communication, and each process has at least one incoming and outgoing unidirectional communication channel. Process  $P_i$  communicates directly with  $P_j$  if a channel exists from  $P_i$  to  $P_j$ , otherwise  $P_i$  communicates indirectly with  $P_j$  through intermediate processes and channels.

The snapshot algorithm consists of two phases. In the first phase, each process takes a snapshot of its state. In addition to the recorded local state information, the messages in-transit when the local snapshots are taken will be included in the global snapshot. The intransit messages are flushed through the channels before the local snapshots are assembled into a global snapshot. A process initiates a global snapshot by (1) saving its local state, (2) sending a snapshot token message on each of its outgoing channels, and (3) beginning the recording of messages on each incoming channel. The token informs the receiving process that a snapshot is being taken, and it flushes the messages in-transit so they are included in exactly one process's local state. When a process receives a token, it performs the same three steps as the initiating process.

A process continues to record incoming messages for a channel until the process receives a snapshot token on the channel. Once a process has received a token on each channel, the process's local state is complete for the global snapshot.

In the second phase, each process disseminates its local state information to form a global snapshot. Each process must send its state information to each of its neighbors. and when a process receives other processes' states, it must relay this information to its neighbors. This type of dissemination ensures that the process requesting the snapshot eventually receives the global state.

Every process receives the global snapshot with Chandy and Lamport's algorithm. Kearns and Spezialetti [38] improve the efficiency of the global snapshot algorithm by reducing the message-passing load for disseminating the global state. Only the process or processes that initiate the global snapshot receive it. The process(es) that initiate the snapshot by passing snapshot tokens include their process identification with the tokens. The tokens continue with their original purpose of informing other processes to record their local states. Once a process has completed recording its local state, the local state is only sent to the process that prompted this process to take a snapshot. Once a non-initiating process has sent its local state to the initiating process, it has completed the global snapshot since it no longer has the responsibility of sending neighboring processes' state information through the network.

Lai and Yang [18] extend the original global snapshot algorithm by removing the FIFO restriction. One status bit is associated with each process and is piggybacked on all messages. Each process's bit is initially 0. and a process sets the bit to 1 when it initiates a snapshot. When a process receives a 1 status bit, its status bit is set to 1, and it takes a snapshot. Since the channels are non-FIFO, messages sent before the snapshot can still be in-transit after the snapshot is taken. These message must be incorporated into the global snapshot. Each process keeps a record of all messages it has received and sent for calculating the in-transit messages.

Mattern [28] develops an algorithm similar to Lai and Yang's for non-FIFO channels. but it does not require the processes to record messages. The algorithm ensures that the result of a process initializing a global snapshot is a consistent cut. A consistent cut is a set of events that are not causally related (concurrent). and each process has exactly one event in the cut. If an event  $e_i$  happens before  $P_i$ 's cut event, and  $e_j$  happens before  $e_i$ , then  $e_j$ must happen before  $P_j$ 's cut event for the cut to be consistent. This condition disallows messages sent after the cut to be received before the cut. The only messages in-transitafter the cut are messages with a status bit of 0 being sent to processes with a status bit of 1. The global snapshot comprises the local states resulting from the cut events and the in-transit messages.

The global snapshot algorithms described share a common problem, they add causal dependencies to a distributed system's computation. To expose this problem, consider Chandy and Lamport's snapshot algorithm. The recording of  $P_i$ 's local state and propagating the

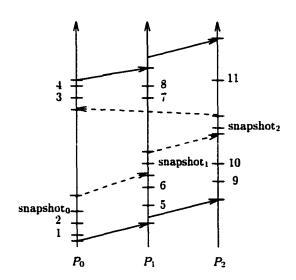


Figure 3.1: Local Snapshot phase of Global Snapshot Algorithm

snapshot token are events added to the distributed computation by the local snapshot phase of the algorithm. Figure 3.1 is a time-space diagram of a three processor system. The asynchronous messages of the computation (without the snapshot algorithm) are denoted with solid lines. The dashed lines represent snapshot token messages. The notation snapshot<sub>i</sub> indicates the local snapshot of  $P_i$ . Figure 3.1 shows both the local snapshots being taken and the propagation of the token, given that  $P_0$  initiated a global snapshot after  $e_0^2$ . Assume no messages are in transit when the local snapshots are taken and the only communication channels are  $P_0$ 's outgoing channel to  $P_1$ ,  $P_1$ 's outgoing channel to  $P_2$ , and  $P_2$ 's outgoing channel to  $P_0$ . The global state obtained by this global snapshot is denoted by global\_state, which is  $\bigcup_{i=0...2}$  snapshot<sub>i</sub>.

The token messages add causality to the computation. For the events  $e_0^1, e_0^2, e_0^3, e_0^4$  of  $P_0$ , events  $e_1^5, e_1^6, e_1^7, e_1^8$  of  $P_1$ , and events  $e_2^9, e_2^{10}, e_2^{11}$  of  $P_2$ , there exist no causal relationship between  $e_i^m$  and  $e_j^l$  for  $i \neq j$ , according to the distributed computation. For example,  $e_0^2$  and

 $e_1^8$  are concurrent in the underlying computation. The token messages add (false) causality to these events as defined by the happens before relationship. Event  $e_0^2$  happens before  $e_1^8$ according to the causal relationship added by the token transmission from  $P_0$  to  $P_1$ . The concurrent execution of  $e_0^2$  and  $e_1^8$  is inconsistent with the causal order defined by the token messages. Events  $e_0^1$  and  $e_0^2$  are causally related to  $e_1^7$ ,  $e_1^8$  and  $e_2^{11}$ ,  $e_1^5$  and  $e_1^6$  are causally related to  $e_0^3$ ,  $e_0^4$  and  $e_2^{11}$ , and  $e_2^9$  and  $e_2^{10}$  are causally related to  $e_0^3$  and  $e_0^4$  due to the three token messages. For example,  $e_0^2 \to e_1^7$  and  $e_0^2 \to e_2^{11}$ .

Adding causality to concurrent events invalidates legitimate global states of the underlying computation. For example, the cut consisting of events  $e_0^1, e_1^7$  and  $e_2^{11}$  is consistent in the underlying computation, but is an inconsistent cut due to the causality added by the token messages. Since the cut of  $e_0^1, e_1^7$  and  $e_2^{11}$  is not consistent, the global state consisting of the local states after the execution of  $e_0^1, e_1^7$  and  $e_2^{11}$  is not a valid global state. The global state defined by  $e_0^1, e_1^7$  and  $e_2^{11}$  is valid in the underlying computation.

Global snapshot algorithms require that obtaining a global state should not disrupt the computation of the distributed system, but these algorithms do interfere by imposing order on concurrent events. Distributed system monitors should be based on the uncorrupt computation of the system. and should not allow a method that invalidates legitimate global states.

An additional problem with global snapshots is their usefulness. Global snapshots are only adequate for detecting *stable* properties. Once a stable property occurs, it persists until the system is terminated. Examples include deadlock and termination. Predicates

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periodically, a stable property can be detected by a predicate evaluated on the sequence of snapshots.

Distributed monitoring and debugging properties are, in general, not stable. Predicates for detecting unstable properties are called unstable predicates. Repeated snapshots are inadequate for evaluating an unstable predicate, as the property expressed by the predicate may have occurred between snapshots, and gone undetected.

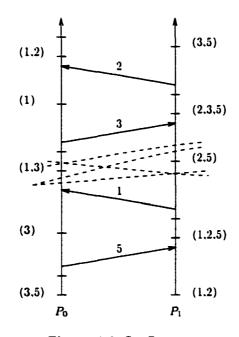


Figure 3.2: Set Partition

Consider the distributed program SETPART. A reasonable and informative global predicate to evaluate after each exchange of maximum and minimum datum values is  $S \cap T = \emptyset$ . If this predicate evaluate to true, SETPART is correctly updating the sets after an exchange. But many global states are possible after an exchange. A simple execution of SETPART is shown in figure 3.2. Each dashed line represents a possible global state after the first exchange. Figure 3.2 represents a valid execution of SETPART, but the evaluation of the global predicate may be either true or false. The predicate's evaluation does not provide insight into the correctness of the execution. If the global states are restricted by  $P_0$  initiating the global snapshot after if receives x and adds x to S. two global states are possible:  $S = \{1.3\}, T = \{1.2,5\}$  and  $S = \{1.3\}, T = \{2.5\}$ . One resulting in a false evaluation of the predicate, and the other resulting in a true evaluation. Although SETPART's communication has a simple repeating pattern, it exemplifies the deficiencies of monitoring unstable properties with existing runtime methods.

Cooper and Marzullo [5] propose an algorithm, *Currently*, for evaluating an unstable predicate while the system is executing. A process sends a monitor process,  $P_{mon}$ , its local state if the local state might affect the outcome of a known global predicate  $\Phi$ .  $P_{mon}$ maintains the last received state of each process, and evaluates  $\Phi$  each time it receives a process's state. If  $\Phi$  evaluates to true,  $P_{mon}$  has detected an undesirable global state.

When a process enters a state that might falsify the evaluation of  $\Phi$ . it freezes and sends a block message to  $P_{mon}$  before informing  $P_{mon}$  of its new state. The process remains blocked until  $P_{mon}$  has received all in-transit messages from the other processes. This flushing of messages allows  $P_{mon}$  to obtain in-transit states that might detect the predicate. Once the messages have been flushed, the blocked process sends  $P_{mon}$  its state and continues execution.

Although *Currently*'s objective is detecting unstable predicates, it is equivalent to taking snapshots periodically, and it can miss a state on which  $\Phi$  evaluates to true. *Currently* incurs the same problem as the previously described algorithms, legitimate global states are invalidated by imposing causal relationships on concurrent events. When processes send state information to  $P_{mon}$  and receive acknowledgements from  $P_{mon}$ , order is imposed on concurrent events.

#### **3.3 Postmortem Methods**

Instead of capturing a global state while the system is executing, the postmortem algorithms *Definitely* and *Possibly* by Cooper and Marzullo [5] construct a lattice of all consistent global states based on trace data gathered during execution. *Possibly*  $\Phi$  evaluates to true if there exists a global state which causes  $\Phi$  to be true. *Definitely*  $\Phi$  evaluates to true if for all total orders there exists at least one global state in each total order which causes  $\Phi$  to be true. *Possibly* and *Definitely* provide a meaningful evaluation of unstable predicates since all global states are considered.

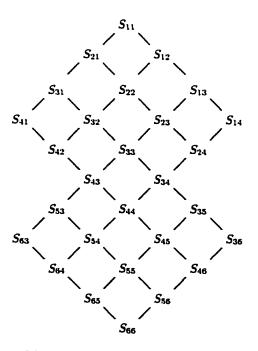


Figure 3.3: Two asynchronously communicating processes

2

 $P_2$ 

6

5 4

3

2

1

 $P_1$ 

Figure 3.4: Lattice of global states

While the distributed system is running, each process informs  $P_{mon}$  of each local state it enters.  $P_{mon}$  maintains a FIFO list of these states for each process. Once the execution has completed,  $P_{mon}$  assembles the local states to construct a lattice of all consistent global states. Figure 3.4 shows the lattice constructed for the 2 processor distributed execution of figure 3.3. Point  $S_{i,j}$  of the lattice is the global state where *i* events have occurred on  $P_1$ , and *j* events have occurred on  $P_2$ . The level of  $S_{i,j}$  is i+j. A possible total ordering of states is a path starting at the level 1 global state, and each subsequent global state has a level increase of one. *Possibly* is true if at least one point in the lattice satisfies  $\Phi$ . *Definitely* is true at least one point in every total ordering satisfies  $\Phi$ .

Definitely and Possibly provide a meaningful predicate evaluation methodology by considering all global states. The outcome of evaluating  $\Phi$  provides unambiguous information about the system's behavior. Although they provide meaningful results, the inability to monitor the system at runtime is a significant weakness of both algorithms. By waiting for the system to complete execution, on-line corrective actions such as recovery or abortion can not be made for invalid execution behavior. Real-time feedback is crucial for life- or mission- critical control applications.

We have developed a runtime method for monitoring a distributed system that is meaningful for both stable and unstable properties. Predicates are evaluated with all the processes' state information that may affect the evaluation. Any invalid system state, indicated by evaluation of the predicate, is detected. Evaluation is only with system states that can occur in the distributed computation, and legitimate global states are not invalidated. The following chapter describes our methodology, both in terms of design and implementation.

# Chapter 4

# Causal Distributed Assert Statement

Some sequential programming languages [39, 40] facilitate predicate evaluation with assert statements. An assert statement [30] (or library function, depending on it's implementation) generally has the form

#### assert(P)

where P is a predicate defined on the state of the program. The semantics of this assert statement are that P is evaluated, without side-effects, on the program state at the point at which the **assert** () is executed. If P is true then the program continues its execution. If P is false, however, the program is aborted, and a diagnostic message is produced.

We have extrapolated the semantics of the assert statement for sequential programs into the distributed context. A distributed assert statement is a global predicate that is anchored at a control point of one process, and that is evaluated when the process executes the assert. A distributed assert statement monitors a distributed system's execution, but only a subset of the system states of the execution are relevant for evaluating the assert. Two possibilities exist for which portion of the execution the distributed assert monitors. One possibility is the distributed assert statement monitors the global states that are defined by consistent cuts including the assert statement. This interpretation is in accord with the global predicate evaluation methods described in chapter 3. If the distributed assert monitors concurrent execution, then any consistent cut of the system that includes the assert event defines a valid global state for predicate evaluation. A simplistic three processor system is shown in figure 4.1. The broken lines represent all possible consistent cuts, and the  $\times$  represents an assert statement.

The only previous work that resembles this interpretation of the distributed assert statement is Cooper and Marzullo's *Currently*[5]. *Currently* evaluates the global predicate  $\Phi$ while the system is executing and is claimed to be appropriate for unstable predicates. But *Currently* is incomplete: global states can be missed that cause a true evaluation of  $\Phi$  [33]. *Currently* is also intrusive of the system's execution since it introduces extra synchronization into the monitored computation, and it can cause a significant degradation in system performance. Every modification of a variable in  $\Phi$  can be considered a possible invalidation of  $\Phi$ , causing the network to be congested with block and acknowledgment messages and causing the process about to execute the modification to freeze until all in-transit messages to  $P_{mon}$  are received.

Another interpretation of the distributed assert statement is that it monitors the execution that has the most recent causal impact on the assert statement. We have developed

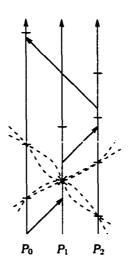


Figure 4.1: Consistent Cuts of the Assert Statement

a methodology for evaluating a distributed assert statement in accordance with this interpretation. Our methodology does not have the problems associated with global state reasoning. The state of the system necessary for evaluating the predicate is well-defined, and the evaluation result relays unambiguous information about the state of the system. Our distributed assert statement is characterized by two properties:

- A1 The asserted predicate is evaluated during execution of the program. We do not generate and analyze traces *post mortem*.
- A2 No additional synchronization or message passing is added to the original distributed application in support of the distributed assert statement. We do increase the size of some application messages.

#### 4.1 Model and Notation

Recall that a distributed program consists of a fixed number of processes  $\Pi = \{P_0, \ldots, P_{N-1}\}$ , and the happened before relationship,  $\rightarrow$ , is a partial order on the program's events. For event e in  $P_i$ , LCP(e, j) where  $j \neq i$ , denotes event e's latest causally preceding event in  $P_j$ . We define LCP(e, j) = f if and only if f is an event in  $P_j$ , such that f happens before e. and there does not exist event f' in  $P_j$  such that f happens before f' and f' happens before e.

**Definition 4.1** For some event  $e \in P_i$ , the latest causally preceding event in  $P_j$  where  $j \neq i$ , denoted LCP(e, j), is event f if and only if

- 1.  $f \in P_j$
- 2.  $f \rightarrow e$
- 3.  $\not Af' \in P_j : f \to f' \to e$

One of possibly many partial orders is defined when a distributed system executes. This is due to branches in control of execution and to the fact that communication delays and process speeds are unpredictable. Hence sends and receives will "match up" unpredictably in general. Consider the source code of a three process distributed system shown in figure 4.2. One of possibly two partial orders is defined when this program executes. The two possible partial orders,  $PO_1$  and  $PO_2$ , are shown in figure 4.3. Set  $\mathcal{P}$  is the set of possible partial orders of a distributed system's execution. For the distributed system shown in

```
P_1::
P_0::
                                                        P_2::
begin
                          begin
                                                        begin
                                                            y = 3
   x = 1
                             if
   async_send(1,x)
                                 async_recv(0, x)
                                                            async_send(1, y)
   x = 2
                                 async_recv(2,y)
                                                        end
   async_send(1, x)
                             else
end
                                 async_recv(2,y)
                                 async_recv(0, x)
                             endif
                             async_recv(0, x)
                             assert(x = y)
                          end
```

Figure 4.2: 3 process distributed system

figure 4.2.  $\mathcal{P} = \{PO_0, PO_1\}$ . For a given execution of the distributed system, one partial order.  $\alpha \in \mathcal{P}$ , is produced.

For a partial order,  $\alpha \in \mathcal{P}$ , at most one *LCP* event exists in each process for any event e. Each partial order may identify a different LCP(e, j). The maximum unique *LCP* events of  $P_j$  for event e is bounded by the number of partial orders, i.e., the size of set  $\mathcal{P}$ .

**Lemma 4.1** For a partial order  $\alpha \in \mathcal{P}$  of a distributed system and an event e of  $P_i$ , at most one LCP(e, j) exists for  $j \neq i$ .

**Proof by contradiction.** Assume two LCP(e, j) events, e' and e'', exist for the one partial order  $\alpha$ . According to the definition of LCP events (definition 4.1),

1.  $e' \to e$ , and there does not exist another event f such that  $e' \to f \to e$ 

2.  $e'' \rightarrow e$ , and there does not exist another event f such that  $e'' \rightarrow f \rightarrow e$ 

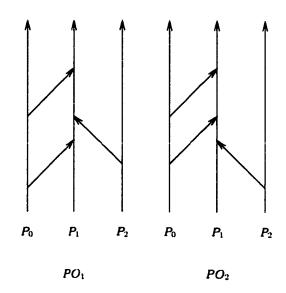


Figure 4.3: Partial orders

From 1. and 2..  $e' \neq e''$  and  $e'' \neq e'$ . therefore e' ||e''. The concurrency of e' and e'' is a contradiction since both are events of  $P_j$  and the events of one process are totally ordered.

Consider event e in process  $P_i$ . A causal cut through e is the set of events consisting of e and the LCP event of e of each process for a partial order  $\alpha$ .

**Definition 4.2** A causal cut through event e. denoted CC(e), is defined as

$$CC(e) = \{e\} \cup \left(\bigcup_{\substack{0 \leq j < N \ j \neq i}} \{LCP(e, j)\}\right).$$

Intuitively, CC(e) is the "latest" set of events of  $\Pi$  which can have a causal impact upon e. In figure 4.4, the causal cut through  $P_0$ ,  $P_1$ , and  $P_2$  for event e is shown as a dashed line. An event f is said to be *before* causal cut CC(e) if there exists event  $g \in CC(e)$  such that

 $f \to g$ ; f is after CC(e) if there exists event  $g \in CC(e)$  such that  $g \to f$ . Accordingly, we use CC to define a notion of global state to be used in the evaluation of a distributed assert statement.

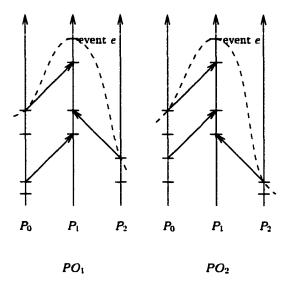


Figure 4.4: Causal cuts for event e

A causal cut does not necessarily include an LCP event from each process since each process may not have an event that occurs before an event e. For each  $\alpha \in \mathcal{P}$ , there is one causal cut for a given event. Also, the LCP events that comprise the causal cut for an event and one partial order may differ from the LCP events that comprise the causal cut for the same event and a different partial order.

**Theorem 4.1** For a partial order  $\alpha \in \mathcal{P}$  of a distributed system and an event e of  $P_i$ , at most one CC(e) exists.

**Proof.** This follows directly from Lemma 4.1 and Definition 4.2. Since each process has at most one LCP(e, j) for each  $\alpha \in \mathcal{P}$  (lemma 4.1) and CC(e) is comprised of the LCP(e, j)

from each process (definition 4.2), at most one CC(e) can exist.

For event e in process  $P_i$ , let pre(e) denote the local state of  $P_i$  in which the execution of e is begun. Execution of e effectively terminates state pre(e). If e is the execution of a causal distributed assert statement in  $P_i$ , then the causal global state, anchored on e, is simply

$$CGState(e) = \{ pre(f) : f \in CC(e) \}.$$

CGState is the set of process states which immediately precede the causal cut through e. the execution of the assert statement. CGState thus incorporates the state of the system as a whole as it may have causal impact upon  $P_i$  at the point the assert statement is executed. Events which are after the causal cut through e cannot affect the execution of e. All events which happen before the causal cut will have their effect on e through transitivity.

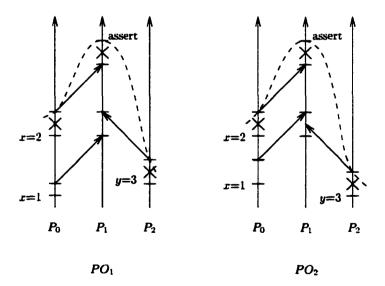


Figure 4.5: Causal Global State for an Assert

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Figure 4.5 shows a causal distributed assert statement being evaluated in process  $P_1$ . The horizontal lines across the process time lines represents events, and the dashed line represents CC(assert(P)). The individual process states compromising the causal global state anchored on the assert is denoted by ×'s on the process time lines. Partial orders  $PO_0$  and  $PO_1$  each have a corresponding causal cut and causal global state. Although in this example the causal cut and causal global state are identical, in other distributed systems they can be different. The causal global state is  $P_0.x = 2$  and  $P_2.y = 3$  for both partial orders.

## 4.2 Implementation

Our implementation of the causal distributed assert statement ensures that when an assert is executed, the relevant components of the causal global state are immediately available at the process executing the assert (Property A1). To that end, process  $P_i$  maintains its current view of the *CGState* in the causal global state buffer. *CGSBuffer<sub>i</sub>*. Processes maintain their causal global state buffers independently. Buffer maintenance requires no message-passing or synchronization beyond that required by the underlying application (Property A2). Each causal state buffer consists of tuples of the following form

(process id, variable name, variable value, vector timestamp)

The meaning and use of vector timestamp is discussed below. A process maintains its causal state buffer to contain only the *latest* (causally speaking) state information for each process.

When an assert statement is executed in  $P_i$ , say at event e,  $CGSBuffer_i$  will contain all components of CGState(e).

A process receives state information from each process in the system by having the processes *piggyback* state information on application messages. When a process sends an application message, it piggybacks its *CGSBuffer* on the message. Process  $P_j$  acquires state information from  $P_i$  when  $P_i$  directly communicates with  $P_j$  or when  $P_i$  indirectly communicates with  $P_j$ . Process  $P_i$  directly communicates with  $P_j$  by sending a message to  $P_j$ . Process  $P_i$  indirectly communicates with  $P_j$  by sending a message to another process  $P_k$  and  $P_k$  either directly or indirectly communicates with  $P_j$ . If  $P_i$  does not directly or indirectly communicate with  $P_j$ , then  $P_i$  does not contribute to  $P_j$ 's causal global state. In this case, LCP(e, i) does not exist.

Consider the communication pattern shown in figure 4.6.  $P_2$  receives state information for  $P_0$  from two different sources: the message  $P_0$  sends to  $P_2$ , and the message  $P_1$  sends to  $P_2$ . When  $P_1$  and  $P_2$  communicate.  $P_2$  requires a mechanism for determining the causally latest value of x.  $P_2$  has one value of x in  $CGSBuffer_2$  from its direct communication with  $P_0$ , and a new arriving value of x is piggybacked on  $P_1$ 's message to  $P_2$ . In fact, the newly arriving value of x is stale and should not overwrite the tuple for x in  $CGSBuffer_2$ . Vector time [29] is the mechanism we adopt for determining the latest causal values associated with variables.

Timestamping a set of events with vector time has been shown to be isomorphic to the causal partial order on those events [33]. Each  $P_i$  maintains a vector  $V_i$  of N integers,  $(V_i[0], \ldots V_i[N-1])$ , where  $V_i[i]$  is the counter of the number of events which have occurred on  $P_i$ .  $V_i[i]$  is incremented before each event in  $P_i$ .  $V_i(e)$  is the vector time of event e of process  $P_i$ . The vector time associated with event e is also associated with the state resulting from e. The rules for maintaining asynchronous vector time are:

- 1. Initially, for each  $P_i$ ,  $V_i[j] = 0$  for  $0 \le j < N$
- 2.  $V_i[i] = V_i[i] + 1$  when an event occurs on  $P_i$ .
- 3. Suppose P<sub>i</sub> sends a message to P<sub>j</sub>, and e<sub>i</sub> and e<sub>j</sub> are the corresponding send and receive events. respectively. If V<sub>i</sub> = (V<sub>i</sub>[0],...,V<sub>i</sub>[N-1]) corresponds to e<sub>i</sub> and V<sub>j</sub> = (V<sub>j</sub>[0],...,V<sub>j</sub>[N-1]) corresponds to e<sub>j</sub>, then as a result of P<sub>i</sub> and P<sub>j</sub> communicating, P<sub>j</sub> updates its vector clock to

$$V_j(e_j) = MAX((V_i[0], \dots, V_i[i] + 1, \dots, V_i[N-1]), (V_j[0], \dots, V_j[j] + 1, \dots, V_j[N-1])),$$

where MAX designates component-by-component maximum.

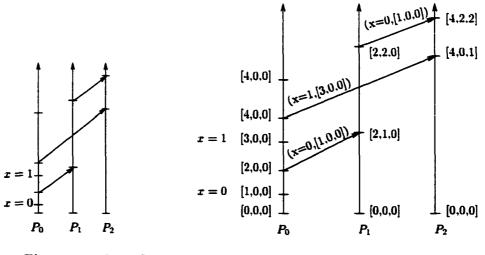


Figure 4.6: Latest State

Figure 4.7: Vector Time

Vector time can be used to indicate the relative "causal timeliness" of state information. Suppose  $P_j$  propagates a state datum stamped with a vector time to  $P_k$ . If the datum is a variable of  $P_j$ , it will be timestamped with the vector time of  $P_j$  just before the communication with  $P_k$ . If, however, the datum is not local to  $P_j$  or  $P_k$ , then it must reside in  $CGSBuffer_j$  (it is being propagated in order to handle the indirect communication), and the vector time of the component's tuple in  $CGSBuffer_j$  will be used. Upon receipt of the vector timestamped datum (assume the datum resides at  $P_i$ ), the *i*th component of its timestamp is compared with the *i*th component of the vector timestamp of the tuple in  $CGSBuffer_k$  associated with the appropriate variable of  $P_i$ . If the *i*th vector component of the tuple in  $CGSBuffer_k$  is greater than or equal to the *i*th component of the timestamp on the incoming datum, then the copy in  $CGSBuffer_k$  is the valid latest causal value of the variable. and the tuple is not updated. Otherwise, the incoming datum is causally later than the value of the variable stored in  $CGSBuffer_k$ , and the tuple must be overwritten with the incoming datum.

Figure 4.7 is derived from figure 4.6 by adding vector time. Note that  $P_2$  receives two copies of the datum for  $P_0$ 's variable x. It receives x with value 1 and vector timestamp [3,0,0] when  $P_0$  sends a message to  $P_2$ . The tuple  $(P_0, x, 1, [3,0,0])$  is inserted into  $CGSBuffer_2$ . When  $P_0$  sent a message to  $P_1$ , the tuple  $(P_0, x, 0, [1,0,0])$  was inserted into  $CGSBuffer_1$ . When  $P_1$  sends a message to  $P_2$ ,  $P_1$  forwards a datum for x with value 0 and vector timestamp [1,0,0] to  $P_2$  to account for the indirect communication between  $P_0$  and  $P_2$ . However, when  $P_2$  receives the second datum for x, the first component of the datum's timestamp, 1, is compared to the first component of the vector timestamp for  $P_0$ 's x in  $CGSBuffer_2$ . 3. Process  $P_2$  then knows to discard the second datum.

The causal state propagation is implemented by the protocol shown in figure 4.8 on each communication. This protocol is not intended as a final implementation but as a foundation for a more efficient result.

#### **Protocol: Causal State Propagation**

| $P_i$ sends to $P_j$ :                  | $P_j$ receives from $P_i$ :                                     |
|---|---|
| $V_i[i] = V_i[i] + 1$                   | $V_j[j] = V_j[j] + 1$   |
| send (msg. $V_i.CGSBuffer_i$ ) to $P_j$ | receive (msg <sub>buffer</sub> , $V_i$ , Tmp_Buffer) from $P_i$ |
|   | Update(CGSBuffer, Tmp_Buffer)                                   |
|   | $V_j = MAX(V_i, V_j)$   |
|   | consume(msg <sub>buffer</sub> )                                 |

Figure 4.8: Propagation Protocol

To simplify the presentation. the above pseudo-code assumes that each process keeps its local state in its causal state buffer along with remote state components it has acquired via message passing. The Update procedure in figure 4.9 is invoked to alter the local causal state buffer based on this communication.

#### **Procedure Update(B1,B2)**

Updates local state buffer B1 based on contents of remote buffer B2. Recall that buffer tuples contain fields (Pid, var, value, V)

for all tuples T in B2 do
 if (T.Pid,T.var.\*,\*) not in B1
 insert T in B1
 else /\* Let T' be the tuple in B1 matching T. \*/
 if T'.V[T'.Pid] < T.V[T.Pid]
 replace T' with T</pre>

endfor

Figure 4.9: Update Causal State Buffer

The asynchronous communicants piggyback state information on all messages to track the causal global state. Although this does guarantee that the causal global state is immediately available for the process evaluating the assert. we piggyback all state information on all messages. Optimizations of this naive approach are addressed in chapters 5, 6 and

7.

## Chapter 5

# Optimization

## 5.1 Timing Results

Our evaluation of an assert statement alters the distributed system by piggybacking data on existing messages, resulting in increased message sizes. Intuitively, one way message transmission time is linear in size of the message. To verify linear transmission time increases, we have conducted an experiment with datagram communication on real systems.

Two processes,  $P_{sender}$  and  $P_{receiver}$ , communicate with each other through UDP/IP datagrams.  $P_{sender}$ 's and  $P_{receiver}$ 's only function is communicating with each other. This provides an adequate environment to measure the full impact of increased message length on execution time.  $P_{sender}$  sends to  $P_{receiver}$  1,000 datagrams, and for each datagram sent,  $P_{sender}$  waits for an acknowledgment from  $P_{receiver}$  before sending the next datagram. One thousand samples of  $P_{sender}$ 's execution time are gathered to obtain a sufficient number of samples to determined  $P_{sender}$ 's average execution time with 95% confidence. For the first 1,000 samples, the datagram size is 50 bytes. The datagram size is incremented by 50 bytes, and samples are gathered for each datagram size. This experiment is completed after the samples are gathered for a 3500 byte datagram. The experiment is conducted between two Sun workstations running SOLARIS 1.1. The average execution times and associated 95% confidence intervals are plotted in figure 5.1. The same experiment is conducted on two additional machine platforms and similar results are obtained. For one platform, the sender is an IBM RS6000 workstation running AIX 3.23, and the receiver is a Sun workstation. For the other platform, the sender is a DECstation 5000 workstation running Ultrix 4.2A, and the receiver is a Sun workstation.

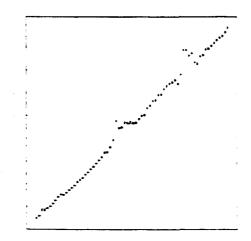


Figure 5.1: Datagram experiment

In all three datagram experiments, the execution times are roughly linear as message size increases. Common to all three experiments is a fluctuation in execution time when the message size is approximately 1500 and 3000. The significance of these numbers lies in the maximum transmission unit (MTU) for the Sun which is 1500 bytes, and datagram fragmentation into packets occurs for every MTU. The Internet protocol (IP) layer, or network

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layer, is responsible for fragmentation into packets and reconstruction of the datagram. The overhead of fragmentation occurs when the message size reaches an MTU multiple. The important conclusion gained from the datagram experiment for assert statement evaluation is that increasing the message size does increase the execution time of a distributed system. but the increase is linear in the size of the piggybacked data.

## 5.2 Piggybacking messages

The naive implementation described for a causal distributed assert statement constructs a causal state buffer consisting of each process's causally latest state information. Each process piggybacks its entire causal state buffer on the application messages. This does ensure that all data is available for assert statement evaluation, but one expects that a majority of the data is not necessary for the evaluation. The amount of state information gathered in the causal state buffers and piggybacked onto messages can be reduced by preprocessing with regard to the assert statement.

If the messages that are not necessary for delivering the *CGState* can be identified, the number of messages marked for piggybacking can be reduced. The *LCP events* are the means by which we reduce the number of messages piggybacking state information. The first step in achieving our reduction is showing that *LCP* events are communication events.

**Lemma 5.1** For event e of  $P_i$ , each  $LCP(e, j), j \neq i$ , is a communication event.

**Proof.** According to the happens before relation and the definition of LCP events (definition 4.1), if there exists an LCP(e, j), then there must exist a communication event f in

 $P_j$  such that  $f \to e$ , and there does not exist another communication event f' in  $P_j$  such that  $f \to f' \to e$ . Events in  $P_j$  either occur before or after f. Consider an event  $g \neq f$  in  $P_j$ . There are two cases:

- 1. Assume  $g \to f$ . Since  $g \to f \to e$  and an event that occurs before f is not LCP(e, j), it follows that g is not LCP(e, j).
- 2. Assume  $f \to g$ . Since there does not exist a communication event after f that happens before e, we know  $g \not\to e$ . Therefore g is not the LCP(e, j).

We can conclude from 1. and 2. that LCP(e, j) is the communication event f.

For asynchronous message passing, each LCP event is a send. We will be concentrating on results for asynchronous message passing, but our results can easily be extended to (the less practically significant) synchronous message passing.

**Lemma 5.2** For event e of  $P_i$ , each LCP(e, j),  $j \neq i$ , is a send event.

**Proof.** We know from lemma 5.1 that each LCP event is either a send or receive event. Assume that the event  $e_{j\neq i} = LCP(e, j)$  is a receive event. For  $e_j$  to be the LCP(e, j),  $e_j \rightarrow e$  and there does not exist another event  $e'_j$  such that  $e_j \rightarrow e'_j \rightarrow e$  (definition 4.1).

For an event of  $P_j$  to happen before an event of  $P_i$  process, there must exist a causal chain of communication events from  $P_j$  to  $P_i$  where the causal chain begins with  $P_j$  sending a message and ends with  $P_i$  receiving a message (definition of  $\rightarrow$ ). For  $e_j$  to happen before e there must exist a send event  $e''_j$  in  $P_j$  that happens after  $e_j$  and that happens before the

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event e. Since  $e_j \to e''_j \to e$  and  $e''_j$  is a send event, the receive event  $e_j$  can not be an *LCP* event.

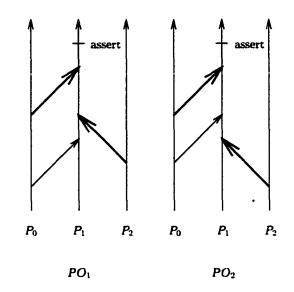


Figure 5.2: LCP and LCP' events of the Assert Event

Corresponding to each LCP send event is a receive event, denoted LCP'. A causal cut for event *e* consists of LCP send events. The LCP and LCP' events of the distributed program shown in figure 4.2 are shown in figure 5.2. The wider communication line indicates the message of the LCP and LCP' events. The LCP and LCP' events of a partial order comprise the communication events that are sufficient for delivering the CGState data to the process evaluating the assert. Before proving this property, the following definitions are necessary:

**Definition 5.1** A communication path of length t + 1 from  $e_j^0$  to  $e_i^t$ , where t is odd and  $j \neq i$ , is a series of communication events  $e_j^0, \ldots, e_i^t$  such that

1.  $e_j^0$  is the only communication event of  $P_j$  in the path,

- 2.  $e_i^t$  is the only communication event of  $P_i$  in the path.
- 3.  $e_k^r \to e_l^{r+1}$ , where  $k \neq l$  or k = l, and there does not exist an event e' that is an event of the path such that  $e_k^r \to e' \to e_l^{r+1}$ .
- 4. for  $e_k^r$  and  $e_l^{r+1}$ , where  $k \neq l$  and r is even,  $e_k^r$  and  $e_l^{r+1}$  are a send/receive pair ( $e_k^r$  being the send and  $e_l^{r+1}$  being the receive), and
- 5. for  $e_k^r$ ,  $e_l^{r+1}$ , where  $k \neq l$ , the next event of the path (if it exists) must occur on  $P_l$ , denoted  $e_l^{r+2}$ , and the the event following  $e_l^{r+2}$  is not an event of  $P_l$ .

If  $e_j^0$ ,  $e_k^1$ ,  $e_k^2$ ,  $e_l^3$ ,  $e_l^4$ ,  $e_i^5$  is a valid communication path of length 6,  $e_j^0$  is a send to  $P_k$ ,  $e_k^1$  is the receive corresponding to  $e_j^0$ ,  $e_k^2$  is a send to  $P_l$ ,  $e_l^3$  the receive corresponding to  $e_k^2$ , and  $e_l^4$  is a send to  $P_i$ , and  $e_i^5$  is the receive corresponding to  $e_l^4$ .

**Definition 5.2** A non-repetitive communication path is a communication path such that when two communication events of  $P_k$  occur in the path  $\ldots, e_k^r, e_k^{r+1}, \ldots$ , no other events of  $P_k$  can occur in the path.

A non-repetitive communication path differs from a communication path in that

- if  $P_k$  has events in the path,  $k \neq j$ , and  $k \neq i$ , then exactly one send and one receive of  $P_k$  occurs in the path.
- $P_j$  has exactly one event in path, the send event  $e_j^0$ , and
- $P_i$  has exactly one event in the path, the receive event  $e_i^t$ .

A non-repetitive communication path is a special case of a communication path.

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**Lemma 5.3** If a communication path exists from  $e_j^0$  to  $e_i^t$ , then at least one non-repetitive communication path exists from  $P_j$  to  $P_i$  consisting of a subset of the events of the communication path.

**Proof by contradiction.** Assume a communication path exists from  $e_j^0$  to  $e_i^t$  but a non-repetitive communication path does not exist from  $P_j$  to  $P_i$  consisting of a subset of the events of the communication path.

Consider the communication path from  $e_j^0$  to  $e_i^t$ ,

Case 1.

The communication path from  $e_j^0$  to  $e_i^t$  is not a non-repetitive communication path due to there existing at least two send commands and two receive commands of the same process.  $P_k$ .  $k \neq j$ ,  $k \neq i$ , in the path. Let  $p = e_j^0, \ldots, e_k^{r-1}, e_k^r, \ldots, e_k^{r+l}, e_k^{r+l+1}, \ldots, e_i^t$ represent such a path where  $P_k$  is the only process that has multiple send and receives in the communication path. The events  $e_k^{r-1}$  and  $e_k^{r+l}$  are receive events of  $P_k$ , and the events  $e_k^{r+l}$  and  $e_k^{r+l+1}$  are the send events of  $P_k$ . We know from the definition of a communication path that  $e_k^{r-1} \rightarrow e_k^r \rightarrow e_k^{r+l} \rightarrow e_k^{r+l+1}$ . We also know that  $e_j^0, \ldots, e_k^{r-1}$  is a non-repetitive communication path and that  $e_k^{r+l+1}, \ldots, e_i^t$  is a nonrepetitive communication path, therefore  $e_j^0 \ldots e_k^{r-1} \cdot e_k^{r+l+1}, \ldots, e_i^t$  is a non-repetitive communication path.

Case 2.

The communication path from  $e_j^0$  to  $e_i^t$  is not a non-repetitive communication path due to there existing in addition to the send command  $e_j^0$  at least one send and receive of  $P_j$  in the path. Let  $p = e_j^0, \ldots, e_j^{r-1}, e_j^r, \ldots, e_i^t$  represent such path. The event  $e_j^{r-1}$ is a receive event of  $P_j$  and  $e_j^r$  is a send event of  $P_j$ . We know from the definition of a communication path that  $e_j^0 \to e_j^{r-1} \to e_j^r$ . We can conclude that  $e_j^r \ldots e_i^t$  is a non-repetitive communication path.

Case 3.

The communication path from  $e_j^0$  to  $e_i^t$  is not a non-repetitive communication path due to there existing in addition to the receive command  $e_i^t$  at least one send and receive of  $P_i$  in the path. Let  $p = e_j^0, \ldots, e_i^{r-1}, e_i^r, \ldots, e_i^t$  represent such path. The event  $e_i^{r-1}$ is a receive event of  $P_i$  and  $e_i^r$  is a send event of  $P_i$ . We know from the definition of a communication path that  $e_i^{r-1} \to e_i^r \to e_i^t$ . We can conclude that  $e_j^0 \ldots e_i^{r-1}$  is a non-repetitive communication path.

If a non-repetitive communication path exists from event  $e_i$  to event  $e_j$ , then event  $e_i$  happens before  $e_j$ . Also, if event  $e_i$  happens before event  $e_j$ , then there exists a non-repetitive communication path from  $P_i$  to  $P_j$  where the first event of the path happens after  $e_i$  and the last event of the path happens before  $e_j$ .

**Lemma 5.4** Event  $e_j$  happens before  $e_i$  if and only if there exists a non-repetitive communication path from a send of  $P_j$  that happens after  $e_j$  and a receive of  $P_i$  that happens before  $c_i$ .

#### Proof

If  $e_j \rightarrow e_i$ , then there exist a non-repetitive communication path from a send of  $P_j$  that happens after  $e_j$  and a receive of  $P_i$  that happens before  $e_i$ .

Assume  $e_j \rightarrow e_i$  but there does not exist a non-repetitive communication path that starts with a send event of  $P_j$  that happens after  $e_j$  and ends with a receive event of  $P_i$  that happens before  $e_i$ .

For  $e_j \to e_i$ , there must be communication path,  $e_j^0 \dots e_i^t$ , such that  $e_j \to e_j^0$  and  $e_i^t \to e_i^t$  ( $e_j$  can be  $e_j^0$  and  $e_i^t$  can be  $e_i^t$ ). From lemma 5.3 we know that there must also exist at least one non-repetitive communication path from  $P_j$  to  $P_i$  that consist of a subset of the communication path  $e_j^0 \dots e_i^t$ .

If there exists a non-repetitive communication path from a send of  $P_j$  that happens after  $e_j$  and a receive of  $P_i$  that happens before  $e_i$  then  $e_j \rightarrow e_i$ .

Proof. Let  $e'_j$  be the send event that happens after  $e_j$  and  $e'_i$  be the receive event that happens before  $e_i$ . From definition 5.2, we know that  $e'_j \rightarrow e'_i$  and therefore  $e_j \rightarrow e_i$ .

**Theorem 5.1** For each  $LCP(e_i, j)$  event of  $CC(e_i)$ , there exists a non-repetitive communication path from  $LCP(e_i, j)$  to an LCP' of  $P_i$  such that each event of the path is either an LCP event or an LCP' event.

#### **Proof.**

CASE 1 For each  $LCP(e_i, j)$  event of  $CC(e_i)$ , there exists a non-repetitive communication path from  $LCP(e_i, j)$  to a receive event  $e'_i$  such that  $e'_i \to e_i$ 

Let  $e_j = LCP(e_i, j)$ . From lemma 5.2, we know  $e_j$  is a send event. From definition 4.1 we know  $e_j \rightarrow e_i$ . From lemma 5.4, we know there exists a non-repetitive communication path from  $e_j$  to some receive  $e'_i$  such that  $e'_i \rightarrow e_i$ .

CASE 2 The non-repetitive communication path that exists from  $LCP(e_i, j)$  to receive event  $e'_i$  consists of LCP and LCP' events.

CASE 2.A The send events of the path are LCP events.

In order for every non-repetitive communication path that exists from  $LCP(e_i, j)$ to event  $e'_i$  not to consist of LCP send events, in each path there must exist at least one send event in  $P_k$ ,  $e_k$ , that is not an LCP event.

Since  $e_k$  is a send event of a non-repetitive communication path from  $e_j$  to  $e'_i$ , we know from definition 5.2 that  $e_k \rightarrow e_i$ . For  $e_k$  to not be an *LCP* event, there must exist another event,  $e'_k$ , of  $P_k$  such that  $e_k \rightarrow e'_k \rightarrow e_i$ ; i.e.,  $e'_k$  is *LCP*( $e_i, k$ ). From this follows a contradiction. If  $e'_k$  exists then there does exist a nonrepetitive communication that includes  $LCP(e_i, k) = e'_k$  according to 5.4. If  $e'_k$ does not exist, then  $e_k$  is the LCP(e, k).

CASE 2.B The receive events of the path are LCP' events.

We know from case 2.A that the sends of a non-repetitive communication path

from  $e_j$  to  $e'_i$  are *LCP* events. And from definition 5.2, the receives of the path correspond to the sends, therefore the receives are *LCP'* events.

The following theorem is the basis for reducing the number of messages on which state information is piggybacked.

**Theorem 5.2** If the state data of the processes are piggybacked only on the messages of the LCP's and LCP's of the CC(e) of the current execution, the process executing the assert statement is delivered exactly the CGState prior to the assert statement's execution.

**Proof.** This follows directly from theorem 5.1. From theorem 5.1 we know there exists a non-repetitive communication path from each LCP event to an LCP' of  $P_i$  that consists of LCP and LCP' events. If a process only piggybacks its local state information, and the state information it has received from other processes. on the message corresponding to its LCP event, the data will be received by  $P_i$ 's LCP' event(s).

Our first objective in reducing the amount of piggybacked data is to analyze the source code of the distributed processes to determine all possible partial orders and the LCP and LCP' events of each partial order. Chapters 6 and 7 explain our static analysis methods for achieving this objective.

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## Chapter 6

## **Static Analysis**

### 6.1 Goals of Static Analysis

The causal state propagation protocol presented in chapter 4 satisfies the two properties of the distributed assert:

- A1 The asserted predicate is evaluated during execution of the program. We do not generate and analyze traces *post mortem*.
- A2 No additional synchronization or message passing is added to the original distributed application in support of the distributed assert statement. We do increase the size of some application messages.

This protocol can be improved by reducing the amount of data piggybacked. We know from the timing experiments in chapter 5 that these reductions will result in less interference with message transmission time. Hence, the "natural" time in the program can be preserved. The objective of static analysis is to determine which send and receive events are the *LCP*  and LCP' events of the assert. By piggybacking data only on these messages, the assert statement is evaluated with the CGState and the amount of data piggybacked is reduced.

The first step in our static analysis is to examine the source code of each process and generate a flow graph. From the flow graphs, communication analysis matches send and receive events to generate a tree called a partial order graph (POG). We prove that the POG represents all partial orders of the distributed system (property 6.12) and that each path of the POG from root to a leaf node represents a unique partial order (property 6.13). After analyzing the source code and generating the POG, our technique detects the LCP and LCP' events for an assert statement. Properties 6.14 and 6.15 are our concluding properties of our analysis, and these properties establish that our technique for identifying LCP and LCP' events is valid.

By performing this analysis before execution, a reduction in the amount of piggybacked data is achieved by tagging the LCP and LCP' events as piggybacking events, and properties A1 and A2 are upheld. Before presenting algorithms for identifying the LCP and LCP' events. Taylor's static analysis technique is discussed.

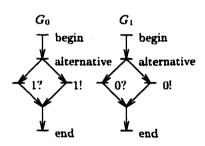
### 6.2 Static Analysis in the Distributed Domain

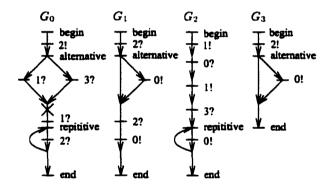
Taylor [42] has developed an algorithm for statically analyzing the synchronous communication of a distributed program. Synchronous communication occurs when the sending process blocks until the message is received by the destination process. Effectively, the rendezvous of the send and receive appears as a distributed assignment, var = expr, that takes place in the context of both processes. The sender evaluates *expr*, and the receiver stores the value into *var*.

The transformation of the  $\rightarrow$  relation into the synchronous communication regime only affects condition (2) of the three conditions stated in chapter one for asynchronous communication. All the conditions are repeated for completeness: (1) if e and f are events in the same process, and e happens before f, then  $e \rightarrow f$ ; (2) if e and f are a send and receive pair which rendezvous, consider e/f as a single event (the rendezvous which effects the distributed assignment) on both the sending and receiving processes: and (3) if  $e \rightarrow f$ and  $f \rightarrow g$ , then  $e \rightarrow g$ .

Taylor's algorithm matches all possible synchronous communications for the programming language Ada [44]. The following is a discussion of Taylor's technique as modified (by us) to deal with communicating sequential processes (CSP)[15]. CSP is a well-defined language which supports strictly synchronous communication. The semantics of CSP constructs have been formalized, and sound and relatively complete verification methodologies for CSP are well-established [20, 21, 3]. Two message transmission operations are available in CSP. Process  $P_i$  sends a message,  $msg\_out$ , to process  $P_j$  by a matching send/receive pair.  $P_i$  executes the send operation  $j!msg\_out$ , and  $P_j$  executes the receive operation  $i?msg\_in$ .

As part of the static analysis, each process is represented by an annotated flow graph  $G_i$ , which is a modification of a sequential program's flow graph derived from flow analysis [13]. A distributed program is represented by  $\{G_0, G_1, \ldots, G_{N-1}\}$  such that  $G_i = \{V_i, A_i, r_i\}$ where  $V_i$  is the set of nodes,  $A_i$  is the set of arcs, and  $r_i \in V_i$  is the root node of  $G_i$ . In contrast to a flow analysis flow graph that usually represents all statements, nodes of  $G_i$  represent only the statements necessary for communication analysis. In particular, the following commands are represented by nodes: send and receive communication commands, guards comprised of communication commands, and repetitive and selective constructs comprised of communication commands. In addition, the root node of  $G_i$  represents the beginning of  $P_i$ 's execution (begin node), and the node whose out-degree is zero represents the completion of  $P_i$ 's execution (end node). Arcs show the possible paths of execution between the nodes, and all paths of  $G_i$  are assumed to be executable. Figures 6.1 and 6.2 demonstrate two distributed programs' flow graphs. The horizontal lines of the flow graph represent the nodes.





**Figure 6.1**: Flow graphs of a 2 process system

Figure 6.2: Flow graphs of a 4 process system

For any node  $v_i$  of  $G_i$ , the set of immediate successor nodes is the set of all nodes  $v'_i$ . for which there exists a path p from  $v_i$  to  $v'_i$  in  $G_i$  such that there is no node  $v''_i$  ( $v''_i \neq v_i$ ;  $v''_i \neq v'_i$ ) on the path from  $v_i$  to  $v'_i$ . Succ $(v_i)$  denotes the set of immediate successors of  $v_i$ . Figure 6.3 list some of the successor sets for figures 6.1 and 6.2.

Taylor defines a concurrency state C as an ordered N-tuple  $(v_0, v_1, \ldots, v_{N-1})$  where each  $v_i$  is a node of  $G_i$  or is an inactive marker. Each  $v_i$  denotes the next node to be executed in  $P_i$  or indicates process inactivity. A concurrency state C has successor concurrency states

| Successor sets of figure 6.1 |  | Successor sets of figure 6.2 |                  |
|------------------------------|--|------------------------------|------------------|
| <i>G</i> <sub>0</sub> :      | <i>G</i> <sub>1</sub> :  | <i>G</i> <sub>0</sub> :      | G <sub>1</sub> : |
|                              | e succ(begin)=alternative<br>succ(alternative)=0?,0!<br>succ(0?)=end<br>succ(0!)=end |                              | •                |

| Figure | <b>6.3</b> : | Successor | sets |
|--------|--------------|-----------|------|
|--------|--------------|-----------|------|

based on the successor sets of the nodes of C. A concurrency state  $C' = (v'_0, v'_1, \dots, v'_{N-1})$ is a successor of C, SUCC(C), if and only if

- 1. For all  $i, 0 \leq i \leq N 1$ , either
  - (a)  $v'_i \in \operatorname{succ}(v_i)$ ,
  - (b)  $v'_{i} = v_{i}$ , or
  - (c)  $v_i = \text{end and } v'_i = \text{inactive}$
- 2. There exists at least one  $v'_i$  which represents application of case a or c.
- 3. Adherence to the communications semantics of CSP is reflected in the application of the three cases a-c. If  $v_i$  is a send or receive command,  $v_i$  can not be replaced by an element of  $succ(v_i)$  until the command's matching communication command occurs in the concurrency state. When a matching send/receive occur in the concurrency state, either both or neither are replaced by their respective successor nodes for the successor concurrency state.

A matching send  $(v_i)$  and receive  $(v_j)$  in a concurrency state indicates the CSP communication between  $P_i$  and  $P_j$  can occur. The communication between  $P_i$  and  $P_j$  is an i/orendezvous between  $P_i$  and  $P_j$ . A nonterminal concurrency state has at least one successor state, and a terminal concurrency state has no successor states. Taylor's *concurrency history* is a sequence of concurrency states  $C_0, C_1, \ldots, C_m$  such that

- 1.  $C_0 = (\text{begin}_0, \text{ begin}_1, \dots, \text{ begin}_{N-1}), C_0$  represents the initial state of the distributed computation.
- 2. For  $i, 0 \leq i \leq m 1$ .  $C_{i+1} \in \text{SUCC}(C_i)$

A proper concurrency history is a finite concurrency history such that  $C_m$  has no successors; i.e.,  $C_m$  is a terminal state. A complete concurrency history of a distributed system is the collection of all possible proper concurrency histories. A directed graph provides a visual representation of a complete concurrency history, where each node of the graph represents a concurrency state. For the distributed program in figure 6.1, the complete concurrency history is shown in figure 6.4.

Relating Taylor's algorithm to previously defined distributed system terminology, we see that each proper concurrency history corresponds to a possible total order of the synchronous communications. A proper concurrency history where  $C_m$  does not contain all inactive markers represents an execution that does not allow all the processes to complete their execution. For example, if process  $P_i$  executes the receive j?, but  $P_j$  does not send a message to  $P_i$ , then  $P_i$  hangs on the receive and can not complete execution. The complete concurrency history corresponds to all possible communication patterns since all execution paths are considered possible.

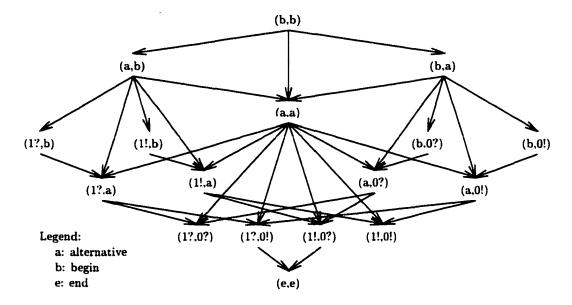


Figure 6.4: Complete Concurrency History of figure 6.1

Taylor's algorithm has been modified and expanded for various distributed system's applications [27, 45, 22, 8, 26]. We have developed algorithms, motivated by Taylor's work, designed to identify the LCP and LCP, messages in each process for an assert statement.

# 6.3 Communication Analysis for Asynchronous Message Passing

In this work, the processes of a distributed program are written in the programming language C. The language has been augmented with three commands: async\_send, async\_recv, and assert. The statements async\_send and async\_recv are for asynchronous communication between processes and are described in detail in chapter 1. The assert command has the format assert(P) where P is a predicate. The predicate P is a boolean expression over the variables of the distributed program. Currently, the placement of async\_send, async\_recv and assert statements is restricted to the main function of the program. In this chapter, the language does allow nested if and if/else constructs, but it does not allow loops. This is done for ease of presentation. Loops are added to the language and handled by our analysis in chapter 7.

Each process  $P_i$  is represented by a control flow graph  $(FG_i)$ . A distributed program is represented by  $\{FG_0, FG_1, \ldots, FG_{N-1}\}$  such that  $FG_i = \{V_i, A_i, r_i\}$  where  $V_i$  is the set of nodes.  $A_i$  is the set of arcs, and  $r_i \in V_i$ . The root node  $\dot{r}_i$  represents the start of  $P_i$ 's execution. The nodes of  $FG_i$  represent either computation statements or control constructs of the source code. Assignment. async\_send, async\_recv. and assert statements are classified as computation statements. The if and else constructs and begin and end delimiters are classified as control constructs. An end node represents the completion of  $P_i$ 's execution. The arcs represent  $P_i$ 's flow of execution. If an arc exists from node n to node n', n' can be executed following the execution of n. Although multiple branches may exist in the flow of execution, all flow of execution will terminate into a single end node.

Consecutive assignment statements that occur between control constructs and other types of computation statements are grouped into one node labeled ASSIGN. The commands **async\_send**, **async\_recv**, and **assert** are represented by SEND. RECEIVE, AS-SERT nodes, respectively. The control constructs **if** and **else** are represented by nodes labeled IF and ELSE, respectively. The end of the **if** side of an **if/else** is represented by a END\_IFSIDE node. The end of an **if** statement is represented by an END\_IF node, and the end of the **else** side of an **it if/else** is represented by a END\_ELSE node.

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Each  $FG_i$  is generated by parsing the source code of  $P_i$ . First a lexical analyzer reads in the source code, and scans this code to recognize tokens. The software tool Lex has been used to produce the lexical analyzer.

The lexical analyzer passes the token to a parser. The tokens are parsed according to the ANSI C grammar that appears in Appendix A. This grammar is LR(1). The software tool Yacc helped produce the parser. The productions of the grammar that are relevant for describing the algorithm for generating the  $FG_i$ s are postfix\_expression, unary\_expression, assignment\_expression, and selection\_statement.

Actions are embedded in these productions to call functions that collectively generate the control flow graphs. The algorithm,  $Create_FG_i()$ , implemented by these function calls, is described. For grouping consecutive assignment statements into one node, each assignment statement of the node is an entry in a linked list, and the assignment node references this linked list. A stack is employed to match the begin and end of control constructs. An entry in the stack is a pointer to a node of  $FG_i$ . The variable *TopStack* is a pointer to the node referenced by the top entry of the stack. The variable *CrtNode* is a pointer to the current node of  $FG_i$ . Associated with each node of  $FG_i$  are two fields that are for constructing the flow graph. The fields are *HoldPtr* and *AddEdgeFlag*. *HoldPtr* is a pointer to a node of  $FG_i$  and *AddEdgeFlag* is a boolean flag. The input for Create\_FG\_i() is the source code of  $P_i$ , and the output of Create\_FG\_i() is the flow graph  $FG_i$ .

Create\_FG\_i()/\* Input:  $P_i$ ; Output:  $FG_i$ Create the ROOT node of  $FG_i$ CrtNode = ROOT nodeif an assignment statement is recognizedAdd assignment statement to the tail of the linked list

if an async\_send is recognized if the linked list is not empty AddNode(CrtNode, ASSIGN) /\* for the assignment statements \*/ linked list is set to empty AddNode (CrtNode, SEND) if an async\_recv is recognized if the linked list is not empty AddNode(CrtNode, ASSIGN) /\* for the assignment statements \*/ linked list is set to empty AddNode (CrtNode, RECEIVE) if an assert is recognized if the linked list is not empty AddNode(CrtNode, ASSIGN) /\* for the assignment statements \*/ linked list is set to empty AddNode (CrtNode, ASSERT) if an if statement is recognized if the linked list is not empty AddNode(CrtNode, ASSIGN) /\* for the assignment statements \*/ linked list is set to empty AddNode(CrtNode, IF) /\* for the if statement \*/ Push CrtNode onto the stack TopStack = CrtNodeif an else is recognized AddNode (CrtNode, END\_IFSIDE) if the linked list is not empty Set field in *CrtNode* to point to linked list linked list is set to empty TopStack.HoldPtr = CrtNode/\* Set HoldPtr of the IF node to the \*/ /\* address of the END\_IFSIDE \*/ CrtNode = top entry of the stackCrtNode.AddEdgeFlag = true/\* Flag an edge needed from END\_IFSIDE node \*/ /\* to the first node following END\_ELSE node \*/ if the end of the else side of an if/else is recognized AddNode (CrtNode, END\_ELSE) /\* for the ending of the else side \*/ if the linked list is not empty Set field in CrtNode to point to linked list linked list is set to empty CrtNode.HoldPtr = TopStack.HoldPtr /\* Move the address of the END\_IFSIDE \*/ /\* node to the END\_ELSE node \*/ CrtNode.AddEdgeFlag = true /\* Flag an edge will be needed from END\_IFSIDE \*/ /\* node to the first node following END\_ELSE node \*/ Pop the stack if the end of an if statement is recognized AddNode(CrtNode, END\_IF) /\* for the ending of the if statement \*/ if the linked list is not empty

| Set field in <i>CrtNode</i> to point to  | linked list                                       |
|--|---|
| linked list is set to empty              |   |
| CrtNode.HoldPtr = TopStack               | <pre>/* Set the HoldPtr of END_IF node */</pre>   |
|  | /* to the address of the IF node */               |
| CrtNode.AddEdgeFlag = true               | /* Flag an edge will be need from the IF node */  |
|  | /* to the first node following the END_IF node */ |
| Pop the stack                            |   |
| if the current control construct or stat | tement is not recognized                          |
| Generate an error and halt               |   |
| if the end of the source code is recogn  | ized  |
| AddNode(CrtNode, END)                    |   |
| If the linked list is not empty          |   |
| Set field in CrtNode to point to         | o linked list                                     |
| linked list is set to empty              |   |
| al almantahan                            |   |

#### end algorithm

The algorithm  $Create_FG_i()$  calls the algorithm AddNode().

```
AddNode(CrtNode, type)

NewNode = Allocate a node

Create a directed edge from CrtNode to NewNode

<u>if</u> CrtNode.AddEdgeFlag

Create a directed edge from the node CrtNode.HoldPtr to NewNode

/* An edge is added either from END_IFSIDE or IF node to NewNode */

<u>if</u> type = ASSIGN

Set field in NewNode to point to assignment linked list

CrtNode = NewNode

end algorithm
```

When a node is added to  $FG_i$ , if the previously added node is the end of the else side of an if/else, the END\_IFSIDE and END\_ELSE nodes must both have an edge to this newly added node. Figure 6.5 shows the adding of *NewNode*. The dashed lines indicate the edges AddNode() creates to *NewNode*. The END\_ELSE is *CrtNode* so the edge from END\_ELSE to *NewNode* is added by the second line of AddNode(). But creating the edge from END\_IFSIDE to *NewNode* is more complicated. When END\_IFSIDE is added to  $FG_i$ , the address of this node is stored in the IF node. This is accomplished with the following line from  $Create_FG_i()$ :

TopStack.HoldPtr = CrtNode

When the END\_ELSE node is added, the address of the END\_IFSIDE node is moved from the IF node to the END\_ELSE node. This is accomplished with the following line from  $Create_FG_i()$ :

#### CrtNode.HoldPtr = TopStack.HoldPtr

By moving the address of the END\_IFSIDE. when a new node is added and *CrtNode* is equal to END\_ELSE. the address of the END\_IFSIDE node is available in *CrtNode* to add the edge from END\_IFSIDE to *NewNode*. The flag *AddEdgeFlag* of the END\_ELSE node is set to true to indicate that function **AddNode()** should add an edge from the END\_IFSIDE node to *NewNode*.

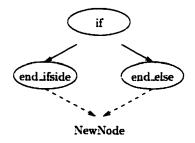


Figure 6.5: if/else portion of control flow graph

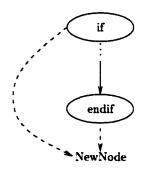


Figure 6.6: if portion of control flow graph

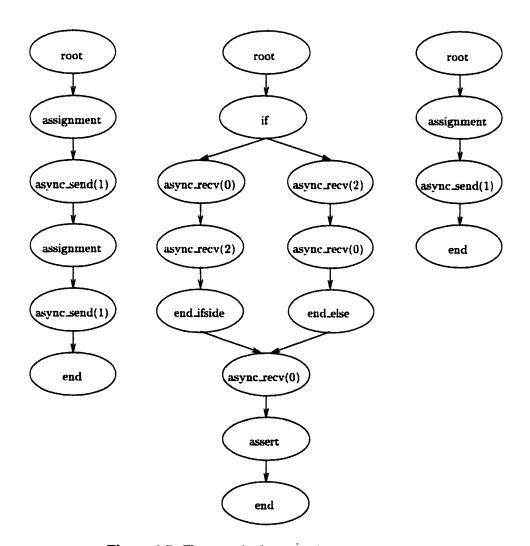


Figure 6.7: Flow graphs for a simple 3 process system

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Figure 6.6 shows the adding of a new node when CrtNode is a END\_IF node. When the END\_IF node is created, the address of the IF node, which is available on top of the stack. is stored in the END\_IF node. This is accomplished with the following line from  $Create_FG_i()$ :

CrtNode.HoldPtr = TopStack

When NewNode is added to  $FG_i$ , the address of the IF node is available in CrtNode so that an edge from the IF node to NewNode can be created by AddNode(). The flag AddEdgeFlag of the END\_IF node is set to true to indicate that function AddNode() should add an edge from the IF node to NewNode. Figure 6.7 is the resulting control flow graphs for the source code of figure 4.2. Another example of a flow graph is figure 6.9 which is the result of one process's source code with nested if constructs shown in figure 6.8.

```
P_i::
{
      a = random number
      b = a - l
      if (a > 1) {
            if (b > 1) {
                  async_send(0, a)
                  b = b * 2
            }
            else {
                  async.recv(0, b)
                  a = b * 2
            }
      }
      \mathbf{a} = \mathbf{b}
}
```

**Figure 6.8**:  $P_i$ 's source code

70

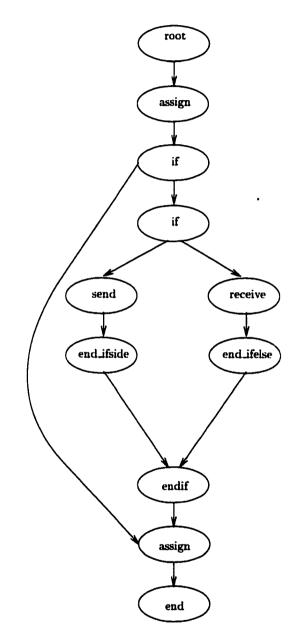


Figure 6.9:  $FG_i$ 

As we know from the definition of  $FG_i$ , the nodes of  $FG_i$  represent syntactic constructs in the source code of  $P_i$ . The execution of  $P_i$  may be viewed as a traversal of  $FG_i$ , starting at the root node and ending at the end node. An event in the execution of  $P_i$  corresponds to the locus of control passing through a node of  $FG_i$ . In the remaining discussion of the flow graphs, the symbol representing a node of  $FG_i$  is also used to represent the event corresponding to the execution of the source associated with that node. The context of the use of the symbol determines whether it is representing a node of  $FG_i$  or an event. For example, if the context is  $a \to b$ , the symbols a and b represent events.

We make use of the following properties of a  $FG_i$ .

**Property 6.1** A path exists from node a to node b in  $FG_i$  if and only if  $a \rightarrow b$  when both a and b are executed.

Proof.

- PART 1. If a path exists from node a to node b, then  $a \rightarrow b$  when both a and b are executed.
  - CASE 1. First consider a process's source code in which no if or if/else statements exist. The resulting control flow graph contains only nodes of type ROOT. ASSIGN, SEND. RECEIVE. ASSERT and END, and one path exists from the ROOT node to the END node. Since execution must follow the edges  $inFG_i$ , a path from a to b implies  $a \rightarrow b$ .
  - CASE 2. Now consider the case in which if and if/else constructs exist. According to the construction algorithm, flow graphs of the form shown in figure 6.10 are generated for an if control construct and an if/else control construct.

For the if control construct, the branch of control resulting from the falsifying of the if statement is the edge from the IF node to S2. When the condition of the if statement evaluates to false, the statements represented by S2 are executed next, and therefore IF  $\rightarrow$  S2. Let node *a* occur before the IF node in  $FG_i$ , and let node *b* occur after S2 as are shown in figure 6.10. Two paths exist from node *a* to node *b*. Independent of which path is followed in an execution  $P_i$ ,  $a \rightarrow b$ .

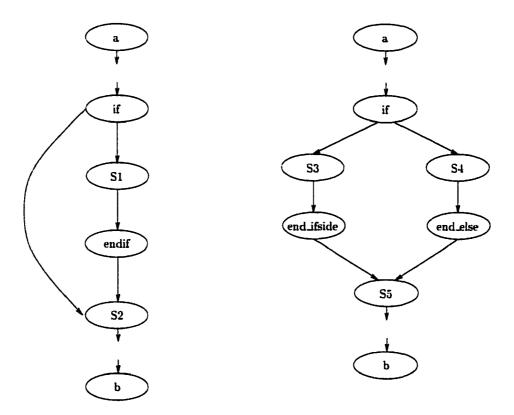


Figure 6.10: if and if/else flow graphs

Next consider the if/else control construct. For the branch resulting from a true evaluation of the condition of the if/else, a path is created by  $Create\_FG_i()$  from the IF node to the END\_IFSIDE and from the END\_IFSIDE to S5. If the condition evaluates to true, the statements represented by S3 are executed

then the statements represented by S5 are executed. Therefore, IF  $\rightarrow$  S3  $\rightarrow$ END\_IFSIDE  $\rightarrow$  S5. For the branch resulting from a false evaluation of the if statement, a path exists from the IF node to the END\_ELSE and from the END\_ELSE to S5. If the condition evaluates to false, IF  $\rightarrow$  S4  $\rightarrow$  END\_ELSE  $\rightarrow$  S5. Let node *a* occur before the IF node in *FG*<sub>i</sub>, and let node *b* occur after S5 in *FG*<sub>i</sub> as are shown in figure 6.10. Two paths exist from node *a* to node *b*. Independent of which path is followed in an execution *P*<sub>i</sub>,  $a \rightarrow b$ .

PART 2. If  $a \to b$  when both a and b are executed, then a path exists from node a to node b in  $FG_i$ .

Assume  $a \to b$  but that a path does not exist from node a to node b in  $FG_i$ . Two cases can exist in  $FG_i$  such that a path does not exist from node a to node b.

- 1. there exists a path from node b to node a, or
- node a occurs in one branch of a if/else and node b occurs in the other branch of the if/else.

If a path exists from node b to node a, we know from part 1 of this proof that  $b \to a$ when both b and a are executed. This contradiction stands in to our assumption that  $a \to b$ , therefore a path cannot exist from b to a. Now consider case 2. Only one branch of the **if/else** will be executed for any execution of  $P_i$ . Therefore,  $a \neq b$ . So we can conclude that if  $a \to b$ , a path exists from node a to node b. **Property 6.2** Each path of  $FG_i$  from ROOT node to the END node represents an execution of  $P_i$ .

Proof. Assume there exists a path from the root node to the end node that does not represent an execution of  $P_i$ . For such a path to exist, there must exist at least two nodes v and v' where v is a parent of v', and it is not possible that  $v \to v'$  for any execution of  $P_i$ . This is a contradiction of property 6.1.

**Property 6.3** For each path, the occurrence of the nodes in the path represents the total order of events if this path is executed.

Proof: For each statement and control construct of the source code, a node is generated in  $FG_i$  (algorithm Create\_ $FG_i$ ()). From this observation of Create\_ $FG_i$ () and properties 6.1 and 6.2, it follow that this property is true.

**Property 6.4**  $FG_i$  represents all execution paths of  $P_i$ .

Proof. This property may be falsified under two conditions:

- CONDITION 1. Flow graph  $FG_i$  only represents a subset of execution paths of  $P_i$ . We know from Create\_ $FG_i$ () that every statement and control construct is represent in  $FG_i$ . For a path not to be represented in  $FG_i$ , one or more directed edges between nodes are omitted. Three cases exist when an edge can be omitted:
  - 1. an edge from current node to new node is not added,

- 2. an edge from END\_IFSIDE node to first node following the END\_ELSE node is not added, or
- 3. an edge from IF node to first node following the END\_IF node is not added.

For any of these cases to occur. the AddNode() algorithm is contradicted.

CONDITION 2.  $FG_i$  represents an invalid execution of  $P_i$ . For this to be true, at least one path from the ROOT node to the END node represents an invalid execution of  $P_i$ . This contradicts property 6.2.

For each communication node, v, of  $FG_i$ , an immediate successor set S(v) is determined from  $FG_i$ . Node v' is an immediate successor of node v if

- 1. there exists a path from v to v',
- 2. v' is a communication node or END node, and
- 3. there does not exist a communication node v'' on the path from v to v' such that  $v'' \neq v'$ .

Concurrency communication states (CCSs) are generated from the flow graphs

 $\{FG_0, FG_1, \ldots, FG_{N-1}\}$  of the constituent processes of the distributed system. Each *CCS* is an ordered *N*-tuple  $(v_0, v_1, \ldots, v_{N-1})$  where  $v_i$  is the root node of  $FG_i$ , a communication node of  $FG_i$ , or the END node of  $FG_i$ . In the examples, an underscore denotes the END node. If  $v_i$  is a communication node,  $v_i$  denotes the next communication command to be executed in  $P_i$ . The communication commands of a *CCS* represent the events that may

occur concurrently. Not all communication commands are ready to be executed: i.e., a receive is not ready if its corresponding send has not been executed. All the communication commands of a CCS that are ready to execute are concurrent. A series of CCSs are generated, as described shortly, to mimic the execution of the distributed system represented by  $\{FG_0, FG_1, \ldots, FG_{N-1}\}$ . Collectively, a tree, H, of CCSs is generated that represents all the possible partial orders  $\mathcal{P}$  of the distributed system. Figure 6.11 is an example of an H tree where each node of the tree represents a CCS. The concurrency among the communication events is preserved in H by not imposing a total order on the concurrent events.

Associated with each send command in a CCS is a counter. If  $v_i$  is a send to  $P_j$ , the counter associated with  $v_i$  is how many messages have been sent to  $P_j$  including this send. Assume we have a four process system, and  $v_1 \in CCS$  is equal to 5:async\_send(0). This five means four messages have been sent collectively to  $P_0$  from  $P_1, P_2$  and  $P_3$  prior to this message. Associated with each receive command whose matching send command has already been executed is also a counter. If  $v_j$  is a receive command and has an associated counter, the counter is how many messages have been received by  $P_j$  including the message received with  $v_j$ .

The initial concurrency communication state,  $CCS_0$ , contains the root node of each flow graph  $\{FG_0, FG_1, \ldots, FG_{N-1}\}, CCS_0 = (r_0, \ldots, r_{N-1})$ . Successor  $CCS_0$  of  $CCS_0$  are determined from  $S(r_i), 0 \le i < N$ . The successors of  $CCS_0$  are a set of concurrency communication states denoted by  $SUCC(CCS_0)$ . The following steps determine  $SUCC(CCS_0)$ :

1. Generate a successor of  $CCS_0$  by replacing each  $r_i$  with an element of  $S(r_i)$ ; i.e.,

 $CCS = (v_0, \ldots, v_{N-1})$  is an element of SUCC( $CCS_0$ ) if each  $v_i$  is an element of  $S(r_i)$ .

2. Generate  $SUCC(CCS_0)$  by repeating step 1 until all unique CCSs are generated from the root nodes' immediate successor sets. The number of successor CCSs of  $CCS_0$  is

 $|\mathbf{S}(r_0)| * \cdots * |\mathbf{S}(r_{N-1})| = |\mathbf{SUCC}(CCS_0)|$ 

A CCS. where each  $v_i$  is a communication node or an inactive marker, has at least one successor,  $CCS' = (v'_0, v'_1, \ldots, v'_{N-1})$ , if CCS has at least a send command or a ready receive command. If node *n* of *H* represents the concurrency communication state CCS, the successors of CCS are represented in *H* as the children nodes of *n*. The predecessor of CCS is represented in *H* as the parent (immediate ancestor) of *n*. A ready receive means that the necessary send command for this receive command occurred in the predecessor of the CCS or in a ancestor of CCS. A message queue.  $Msg_Q_i$ , is maintained for each process. If  $v_j \in CCS$  is a send command to  $P_i$ , the entry *j* is added to the queue  $Msg_Q_i$ following the generation of SUCC(CCS). If  $v_i$  is a receive from  $P_j$  and  $Msg_Q_i$  contains a *j*, the receive is ready and the first *j* in  $Msg_Q_i$  is removed.

Associated with each  $Msg_Q_i$  is a counter that is incremented each time an entry is placed in the queue. The current value of the counter is appended to an entry when it is added to  $Msg_Q_i$ . An entry in  $Msg_Q_i$  has the format <counter, process id>. The value of counter is also appended to the send entry of the CCS node of H that generated the entry in  $Msg_Q_i$ . Send commands that are syntactically identical in a process's source code are distinguished in the CCS nodes of H by their associated counter. When a receive  $v_i$  from  $P_j$  is ready, the counter associated with the first j entry in the queue  $Msg_Q_i$  is appended to the receive entry in the CCS node of H. Not only are syntactically identical receives distinguishable, the counter provides a method to match sends with corresponding receives. The use of this counter for matching sends and receives will be seen in a later algorithm.

A CCS may contain multiple sends and ready receive commands. For example,

 $CCS = (async\_send(1), async\_send(0), async\_recv(3),-)$  has the two sends, and a possible ready receive. If  $Msg\_Q_2$  has the entry <*counter*, 3> to indicate that  $P_3$  has sent a message to  $P_2$  but the message has not been received by  $P_2$ ,  $v_2$  ( $v_2 = async\_recv(3)$ ) is a ready receive. If  $v_2$  is a ready receive, the value of *counter* is appended to  $async\_recv(3)$  in the H node. If CCS has no sends and no ready receives. CCS has no successor states. The successor concurrency communication states of CCS. SUCC(CCS), are determined from the immediate successor sets of CCS's send and ready receive commands. The following steps determine SUCC(CCS):

- 1. In CCS, find the send and ready receive commands.
- 2. Generate a successor of CCS. CCS'. by replacing each  $v_i$  of CCS that is either a send or ready receive command with an element of  $S(v_i)$ . If the element of  $S(v_i)$  chosen is the end node, replace  $v_i$  with the inactive marker.
- 3. Generate SUCC(CCS) by repeating step 2 until all unique CCS's are generated from the send and ready receive immediate successor sets. For example, if CCS has two sends,  $v_0$  and  $v_1$ , and one ready receive,  $v_3$ , then the number of successor states of CCS is  $|S(v_0)| * |S(v_1)| * |S(v_3)| = |SUCC(CCS)|$

A CCS containing more than one send and/or ready receive commands signifies these commands happen concurrently. If a CCS consists of no send commands and one or more

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receive commands, where the receive commands are not ready, the CCS has no successors and is an *invalid terminal state* of the distributed system. A CCS comprised of all inactive markers is a *valid terminal state*.

A proper CCS history is a sequence of concurrency states  $CCS_0, CCS_1, \ldots, CCS_m$  such that

- 1.  $CCS_0 = (r_0, r_1, \ldots, r_{N-1}),$
- 2. For all  $i, 0 \leq i \leq m 1$ ,  $CCS_{i+1} \in SUCC(CCS_i)$ , and

3.  $CCS_m$  has no successors ( $CCS_m$  is a valid or invalid terminal state).

A complete CCS history of a distributed system is a collection of all possible proper CCS histories. The complete CCS history is represented by a directed graph H = (N, A, r)where N is the set of nodes, A is the set of arcs, and  $r \in N$  is the root node of the graph. The nodes represent the CCSs, r represents CCS<sub>0</sub>, and an arc exists from the node that represents CCS to the node that represents CCS' if CCS'  $\in$  SUCC(CCS). A path from the root node to a node of the graph that has no successors (out-degree is 0) is a proper CCS history. Figure 6.11 is a complete CCS history for the distributed system shown in figure 6.7. The underlined communication events are the sends and ready receive events. The number preceding the communication event is the counter associated with the event.

The following algorithm, Crt\_H(), generates the graph H to represent the complete concurrency history. The graph H is built breath first, that is, one level of the tree is created before the next level is begun. A node of H consists of two entries, CCS and FGnode[0...N-1]. The entry CCS is the CCS this node represents. The array entry

.

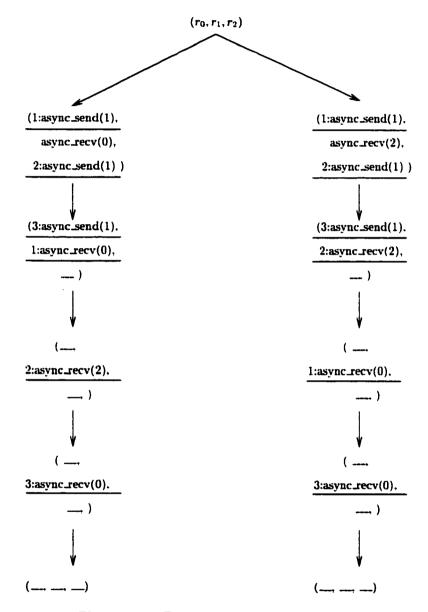


Figure 6.11: Tree H for simple 3 process system

FGnode[i] is the node of  $FG_i$  that  $v_i$  of CCS represents. The array FGnode is set to the appropriate values by algorithm  $Crt_H()$  and is used later by algorithm  $Crt_POG()$ .

An array of size N of integers is maintained,  $counter[0], \ldots, counter[N-1]$ , by algorithm  $Crt_H()$  for counting the number of messages that have been sent to each process. The value of counter[i] is the number of messages that have been sent to  $P_i$  and the number of entries that have been placed in  $Msg_Q_i$ . In addition to the  $Msg_Q_i$  queues, another queue  $CCS_Q$  is maintained for recording the CCSs that are to be added next to H. An entry in  $CCS_Q$  consists of four parts, a CCS, a linked list representing the set SUCC(CCS), the values of the queues  $Msg_Q_0, \ldots, Msg_Q_{N-1}$  that correspond to CCS after SUCC(CCS) has been determined, and the value of array counter that corresponds to CCS after SUCC(CCS) has been determined. The format of an object in the queue is <node. list. $Msg_Q_0, \ldots, Msg_Q_{N-1}$ , counter>. An entry in the linked list list consist of two two values, CCS and the variable FGnode corresponding to this CCS. The input to  $Crt_H()$  is  $\{FG_0, FG_1, \ldots, FG_{N-1}\}$ , and the output is the tree H.

Algorithm Crt\_H() calls function Determine\_SUCC() to determine the successors of a CCS and to place the appropriate entries in the  $Msg_Q$  queues and  $CCS_Q$  queue. Function Determine\_SUCC() calls function Generate\_SUCC() to generate all the successors of a CCS. The variables employed by function Generate\_SUCC() to generate the successors are  $S_{\cdot}v_i$  and *index*. Corresponding to each send and receive node of  $FG_i$  is an array  $S_{\cdot}v_i$  that contains the successors of node  $v_i$ ,  $S(v_i)$ , in  $FG_i$ . If  $v_i$  is an entry in a CCS, array  $S_{\cdot}v_i$  is the successor nodes of  $v_i$ . The maximum number of successors of a node is MAXKIDS, and the dimension of each  $S_{\cdot}v_i$  is MAXKIDS+1. Each  $S_{\cdot}v_i$  array is filled with -1 for

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unused entries. Variable *index* is an array of N integers. Function Permute() determines a successor of CCS by selecting an index into each  $S_v_i$  array for each  $v_i \in CCS$  that is a send or ready receive. The array *index* contains indexes into each  $S_v_i$ . If  $v_i \in CCS$  is a send or ready receive. *index[i]* is an index into the array  $S_v_i$ . If  $v_i \in CCS$  is neither send nor ready receive. *index[i]* is a -1 meaning this  $v_i$  should not be changed in the successors of CCS. Function Generate\_SUCC() calls function Permute() to obtain the indexes for a successor of a CCS and continues to call function Permute() until all successors of a CCS are generated.

Crt\_H() Initialize queues  $Msg_Q_0, \ldots, Msg_Q_{N-1}, CCS_Q$  to empty Initialize array counter[0] ... counter[N - 1] to 0 Create root node r $r.CCS = CCS_0$ Determine\_SUCC( $r. CCS_0, Msg_Q_0, \dots, Msg_Q_{N-1}, CCS_Q$ ) while CCS\_Q is not empty  $item = behead(CCS_Q)$ /\* format of item is < node, list.  $Q_0, \ldots, Q_{N-1}$ . counter> \*/ Parent = item.nodeLL = item.list $Msg_Q_0,\ldots,Msg_Q_{N-1} = item.Q_0,\ldots,item.Q_{N-1}$ counter = item.counter for each < CCS.FGnode > entry in LL Create a node n in Hn.CCS = CCSn.FGnode = FGnodeCreate edge from Parent to n**Determine\_SUCC**(n, CCS,  $Msg_Q_0$ ,...,  $Msg_Q_{N-1}$ , counter,  $CCS_Q$ ) end for end while end algorithm

Determine\_SUCC( $n, CCS, Msg_Q_0, \dots, Msg_Q_{N-1}, counter, CCS_Q$ )  $Msg_Q'_0, \dots, Msg_Q'_{N-1} = Msg_Q_0, \dots, Msg_Q_{N-1}$  counter' = counter<u>if</u> (n = root node)

```
SUCC(CCS) = Generate_SUCC(n) /* < CSS.FGnode> is entry in SUCC(CCS) */
       \mathbf{if} (SUCC(CCS) \neq NULL)
           Add \langle n.SUCC(CCS), Msg_Q'_0, \dots, Msg_Q'_{N-1}, counter' \rangle to the tail of CCS_Q
       end if
   <u>else</u>
       for i = 0 to N - 1
           \underline{if}(v_i \text{ of } CCS = async_recv(j))
              if (Msg_Q'_i \text{ has entry } < counter. j >)
                   /* v_i is a ready receive */
                  item = behead first < counter, j > entry in Msg_Q'_i
                  append item.counter to v_i in CCS
                                                                /* item.counter:async_recv(j) */
              end if
           end if
       end for
       for i = 0 to N - 1
           if(v_i \text{ of } CCS = async_send(j))
               counter[j]'++
               Add \langle counter/j \rangle'. i > to Msg_Q'_i
               Append counter/j]' to v_i in CCS
           end if
       end for
       SUCC(CCS) = Generate_SUCC(n)
       \underline{if} (SUCC(CCS) \neq NULL)
           Add \langle n, SUCC(CCS), Msg_Q'_0, \dots, Msg_Q'_{N-1}, counter' \rangle to the tail of CCS_Q
       end if
   end if
end function
```

```
\begin{aligned} \textbf{Generate_SUCC}(n) \\ & \textbf{SUCC}(CCS) = \textbf{NULL} \\ & index[0] \dots index[N-1] = -1 \\ & \underline{\textbf{for}} \ i = 0 \ \text{to} \ N-1 \\ & \underline{\textbf{if}} \ (v_i \in CCS = \text{send OR } v_i \in CCS = \text{ready receive OR } v_i \in CCS = r_i) \\ & index[i] = 0 \\ & \underline{\textbf{end if}} \\ & \underline{\textbf{end for}} \\ & \underline{\textbf{do}} \\ & CCS' = n.CCS \\ & FGnode' = n.FGnode \\ & \underline{\textbf{for}} \ i = 0 \ \text{to} \ N-1 \\ & \underline{\textbf{if}} \ (index[i] \neq -1) \\ & v_i \in CCS' = \text{commo command or inactive marker for node } S_{-v_i}[index[i]] \\ & FGnode[i] = S_{-v_i}[index[i]] \end{aligned}
```

```
endif
endfor
Add < CCS',FGnode> to the tail of linked list SUCC(CCS)
while (Permute(index) = true)
return(SUCC(CCS))
end function
```

```
Permute (index)
   current = N - 1
   <u>while</u> (index/current/ == -1) AND (current \geq -1)
       current = current - -
   endwhile
   if (current \geq 0)
       index/current/++
   else
      return(false)
                                                                            /* index is all -1's */
   endif
   while (current \geq 0) AND (S<sub>vcurrent</sub>/index/current/] = -1)
       index(current) = 0
       current --
       while (current \geq 0) AND (index/current/ = -1)
          current --
      end while
       <u>if</u> (current \geq 0)
          index/current/++
      endif
   end while
   \underline{if}(current < 0)
       return(false)
                                                         /* have been through all permutations */
   else
       return(true)
   endif
end function
```

The following are useful properties of H. In proving these properties, the function  $\rho$  maps an event e to the process of the distributed system in which the event occurs.

 $\rho(e) = i \in \Pi$  if  $e \in P_i$ 

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#### Property 6.5 If

•  $v_i$  and  $v_j$  are events in the execution of a distributed system,

•  $v_i \rightarrow v_j$ ,

- $v_i \in CCS$  and  $v_i$  is a send or ready receive, and
- $v_j \in CCS'$  and  $v_j$  is a send or ready receive.

then CSS is an ancestor of CCS'.

CASE 1 For  $\rho(v_j) = \rho(v_i)$ .

Proof by induction.

BASIS. If

- $v_i \in CCS$ .
- $v_i$  is a send or ready receive.
- CCS occurs on level l of H,
- $v_j \in \mathcal{S}(v_i)$ , and
- $v_j \in CCS'$

then CCS' occurs on level l + 1.

Proof. We know that the SUCC(CCS) are children of CCS in H. According to the construction of H, SUCC(CCS) is determined with the  $S(v_i)$  for each  $v_i$ that is send or ready receive. Node  $v_j$  is represented in at least one CCS'  $\in$ SUCC(CCS) which occurs on the next level, l + 1, of the tree H. INDUCTIVE HYPOTHESIS. If

- $v_i \in CCS$ ,
- $v_i$  is a send or ready receive.
- CCS occurs on level l of H.
- $v_i \rightarrow v_k$ .
- $\rho(v_i) = \rho(v_k)$ , and
- $v_k \in CCS''$ .

then CCS'' occurs on level l + n for n > 2.

INDUCTIVE STEP. If

- $v_k$  is a send or ready receive.
- $v_j \in \mathcal{S}(v_k)$ , and
- $v_j \in CCS'$

then CCS' occurs on level l + n + 1.

Proof. We know from the inductive hypothesis that CCS'' occurs on level l + nand that CCS'' is an ancestor of CCS. Since  $v_j \in S(v_k)$ , we know from the basis that CCS' occurs on level l + n + 1. We can conclude that CCS' is an ancestor of CCS.

CASE 2. For  $\rho(v_j) \neq \rho(v_i)$ .

Proof. Since  $v_i \rightarrow v_j$ , we know from lemma 5.4 there exists a non-repetitive communication path from  $P_i$  to  $P_j$  from a send of  $P_i$  that happens after  $v_i$  (or  $v_i$  is this send) and a receive of  $P_j$  that happens before  $v_j$  (or  $v_j$  is this receive). Let  $NCP = e_i^0, \ldots, e_j^t$  be this non-repetitive communication path. Two possibilities exist for  $v_i$ : either  $v_i$ and  $e_i^0$  are the same event, or  $v_i$  occurs before  $e_i^0$ . Two possibilities exist for  $v_j$ , either  $v_j$  and  $e_j^t$  are the same event or  $v_j$  occurs after  $e_j^t$ . In the remaining proof we assume without loss of generality that  $v_i$  and  $e_i^0$  are the same event, and  $v_j$  and  $e_j^t$  are the same event.

The events of the path *NCP* correspond to one or more messages. Consider the following 2 cases:

CASE 2.A. NCP corresponds to one message.

Event  $v_i$  is the sending of a message to  $P_j$ , and  $v_j$  is the corresponding receive of the message from  $P_i$ . Let the following be true for the nodes CCS and CCS'of H:  $v_i \in CCS$  and  $v_j \in CCS'$ . According to the construction of H, when  $v_j$ is ready, the *i* entry in  $Msg_Q_j$  corresponds to  $v_i$ . For the *i* that corresponds to  $v_i$  to be in  $Msg_Q_j$ . CCS must be an ancestor of CCS'.

CASE 2.B. NCP defines two or more messages.

Let  $NCP = e_i^0 \dots e_k^m, e_k^{m+1}, e_l^{m+2} \dots e_j^t$ , where m+2 < t, and  $e_i^0 \in CCS$  and is a send,  $e_k^m \in CCS''$  and is a receive,  $e_k^{m+1} \in CSS'''$  and is a send,  $e_l^{m+2} \in CCS''''$ and is a receive, and  $e_j^t \in CCS'$  and is a receive. We know from case 1 that for events  $e_k^m, e_k^{m+1}$  of NCP, where  $e_k^m \in CCS''$  and  $e_k^{m+1} \in CCS'''$ , that CCS'''is an ancestor of CCS''' We know from case 2.a that for events  $e_k^{m+1}, e_l^{m+2}$  of NCP, where  $e_k^{m+1} \in CCS'''$  and  $e_l^{m+2} \in CCS''''$ , that CCS''' is an ancestor of CCS''''. Therefore, CCS''' is an ancestor of CCS''''. If  $e_k^m$  is the receive event immediately following  $e_i^0$  in NCP, then from case 2.a we know that CCS is an ancestor of CCS''. Therefore, CCS is an ancestor of CCS''''. If  $e_l^{m+2}$  is the send immediately preceding  $e_j^t$  in NCP, then from case 2.a we know CCS'''' is an ancestor of CCS'. We conclude that CCS is an ancestor of CCS'.

Property 6.6 The sends and ready receives of a CCS are concurrent.

Proof. Assume for  $v_i, v_j \in CCS$  that  $v_i \to v_j$ . This contradicts property 6.5.

**Property 6.7** If CCS is an ancestor of CCS'.  $v_i \in CCS$  and  $v_j \in CCS'$ , and  $v_i$  and  $v_j$  are either sends or ready receives, then  $v_i \rightarrow v_j$  if one of the following is true:

CASE 1.  $\rho(v_i) = \rho(v_j)$ 

- CASE 2.  $v_i$  is send to  $P_j$ ,  $v_j$  is a ready receive from  $P_i$ . and the next i entry in  $Msg_Q_j$ corresponds to  $v_i$ .
- CASE 3.  $v_i \rightarrow v_k$  and  $v_k \rightarrow v_j$  where  $v_k \in CCS''$  such that  $v_k$  is either a send of ready receive. CCS is an ancestor of CSS''. and CCS'' is an ancestor of CCS'.

#### Proof.

CASE 1.

For  $v_j$  to occur in CCS' that is a descendant of CCS,  $v_j \in S(v_i)$  or  $v_j \in S(S(\ldots S(v_i) \ldots))$  where the nesting of immediate successor sets is two or greater. Therefore  $v_i \rightarrow v_j$ . CASE 2.

According to the algorithm for constructing H, for  $v_j$  to be a ready receive and the next *i* entry in  $Msg_Q_j$  to correspond to  $v_i$ ,  $v_i$  must happen before  $v_j$ .

CASE 3.

This follows directly from the transitive property of the happens before relationship.

We know from property 6.6 that the sends and ready receives of a CCS are concurrent. We can deduce concurrent sends and ready receives that occur in different CCSs. Entries  $v_i$ and  $v_j$  are concurrent if  $v_i \in CCS$ ,  $v_j \in CCS'$ ,  $v_i$  and  $v_j$  are either sends or ready receives, CCS is an ancestor of CCS', and  $v_i \neq v_j$ .

Before stating and proving the next property, lemma 6.1 is established. The execution of a communication event in  $P_i$  represented by node n in  $FG_i$  is possible if there exists at least one path from the root node to n such that the communication events occurring in the path prior to n are either sends or ready receives in H. In other words, the communication event of node n has a possibility of being executed if the communication events that occur prior to it are executed. If a receive is possible, its execution is then dependent on a message being sent, and the receive is labeled as ready when the necessary message is sent. If the necessary message is not sent, the receive does not become ready and does not execute. If a send is possible, it executes since a send's execution is not dependent on the occurrence of a communication event in another process.

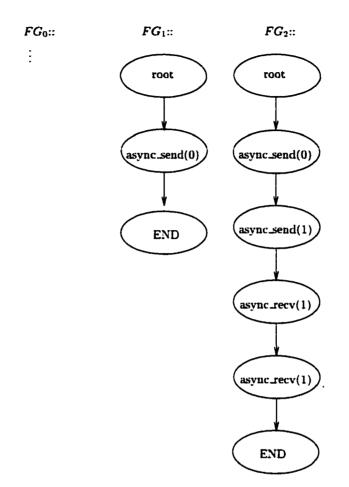


Figure 6.12: Possible and impossible receives

An example of a possible receive event and an impossible receive event is shown in figure 6.12. In  $FG_2$  there exists a path from the root node to the first  $async\_recv(1)$ . We know from the construction of H that  $async\_send(0)$  will be an element of a node of H. and  $async\_send(1)$  will be an element of a node of H. The first  $async\_recv(1)$  of  $FG_2$  will occur in a node of H as a receive, but this receive will not be ready since the sending of a message from  $P_1$  to  $P_2$  does not exist. This receive occurs as an entry in an H node to represent the receive waiting to execute. The communication commands of  $P_2$  prior to the first  $async\_recv(1)$  are executed, and  $async\_recv(1)$  is possible although it will not execute. Since the first  $async_recv(1)$  of  $P_2$  can not execute, the second  $async_recv(1)$  of  $P_2$  will not occur in a node of H and is therefore impossible.

**Lemma 6.1** If node n of  $FG_i$  is a communication node and the execution of n is possible, then n is a send or receive in at least one node of H.

Proof.

BASIS.

If node n is a successor of the root node of  $FG_i$ ,  $n \in S(r_i)$ , then  $v_i = n$  for at least one  $CSS \in SUCC(CCS_0)$ .  $CCS_0$  occurs on level 0 of H. therefore each  $CCS \in$  $SUCC(CCS_0)$  occurs on level 1 of H.

Proof. According to the construction of H, the SUCC( $CCS_0$ ) is determined by  $S(r_i)$  for all i. Node n of  $FG_i$  is represented in at least one  $CCS \in SUCC(CCS_0)$ .

#### INDUCTIVE HYPOTHESIS.

If node n' is a communication node of  $FG_i$ , n' is an immediate predecessor of node n in  $FG_i$ , and the execution of n' is possible, then node n' is represented in CCS' on level i of H.

INDUCTIVE STEP.

If node  $n \in S(n')$  and the execution of node n is possible, then node n is represented in at least one  $CCS \in SUCC(CCS')$  on level i + 1 of H.

Proof. From the inductive hypothesis, we know n' is represented in node CCS' on level *i* of *H*. For the execution of node *n* to be possible, node n' is either a send or ready receive element of CCS' In the construction algorithm, SUCC(CCS') is determined by  $S(v_i)$  for all i of CCS'that are sends or ready receives. Let  $v'_i = n'$  in node CCS'. Since  $v'_i$  is a send or a ready receive of CCS' and  $n \in S(v'_i)$ , we can conclude that node n is represented in at least one  $CCS \in SUCC(CCS')$  on level i + 1 of H.

**Property 6.8** The tree H derived from  $\{FG_0, \ldots, FG_{N-1}\}$  represents all partial orders of the distributed system represented by  $\{FG_0, \ldots, FG_{N-1}\}$ .

Proof.

- 1. From properties 6.1. 6.3. and 6.4. we know each  $FG_i$  represents all execution paths of  $P_i$ , and the occurrence of the nodes of a path of  $FG_i$  represents the total order of events of  $P_i$ .
- 2. From properties 6.5 and 6.7, we know all the happens before relationship among local and non-local events of the distributed system are correctly represented in H.
- 3. From lemma 6.1. we know that if the execution of a communication node of  $FG_i$  is possible, then the communication event is represented in H.

From (1), (2) and (3), we can conclude all possible executable events of each process are represented in H, and all happens before relationships among these events are correctly represented in H. Therefore all partial orders of the distributed system are represented in H.

In some cases, two or more branches of H represent the same partial order. Consider the portion of tree H for a four processor system in figure 6.13. In this example, the receives of the CCSs are not ready. The sends of each CCS are replaced in the child CCSs with an inactive marker. Both leaf node branches indicate that  $P_0$  does not complete execution. The two branches shown represent the same partial order. From the tree H, a partial order graph, POG, is constructed that combines branches that represent the same partial order are represented in the POG. In other words, the sends and ready receives are presented in the POG.

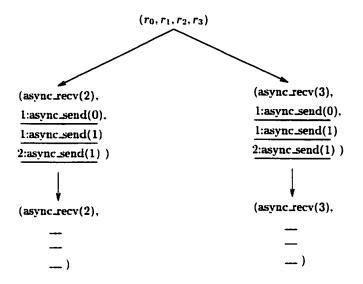


Figure 6.13: Same partial orders

A POG is a directed graph (N, A, s) where N is the set of nodes. A is the set of arcs. and  $s \in N$  is the root node of POG. The nodes of the POG are generated from H's nodes such that the POG nodes represent the sends and ready receives command of the H nodes. In the remaining discussion of POG nodes, the following format of an entry is a POG node is adapted for conciseness. A send entry has the format c: iSj where c is the counter, i is the process executing the send and j is the destination process. A ready receive entry has the format c: iRj where c is the counter, i is the process executing the receive and j is the sender. The POG is constructed by traversing H breath first, starting at the the root node of H, and generating the nodes of the POG in breath first order. The algorithm for constructing the POG determines whether CCSs have equivalent send and ready receive communication entries.  $CCS_1, \ldots, CCS_t$  have equivalent communications if the following conditions are true:

- 1. If at least one  $CCS_{q:1 \le q \le t}$  contains one or more send and/or ready receive commands.
- 2. If  $v_i$  is a send command of  $CCS_{q:1 \le q \le t}$ , then each  $v_i$  in all  $CCS_{r:1 \le r \le t}$  is the same<sup>1</sup> send command.
- 3. If  $v_i$  is a ready receive command of  $CCS_{q:1 \le q \le t}$ , then each  $v_i$  in all  $CCS_{r:1 \le r \le t}$  is the same receive command and is a ready a receive.

If  $CCS_i$  and  $CCS_j$  have equivalent communication commands, the equivalent communication commands of  $CCS_i$  and  $CCS_j$  are all the send and ready receive commands that occur in  $CCS_i$  and  $CCS_j$ .

The algorithm for constructing the POG relies on the function EQUIV(). The input to EQUIV() is a set of H nodes, *node\_set*, and the return value is a subset of *node\_set*. If *node\_set* contains two or more nodes that have equivalent communication commands, EQUIV() re-

<sup>&</sup>lt;sup>1</sup> Same meaning each  $v_i$  represents the same node of  $FG_i$  and the counters are equal.

turns these nodes, else EQUIV() returns  $\emptyset$ . Nodes of H that have equivalent communication commands are called equivalent nodes. If EQUIV() finds a subset of *node\_set* that have equivalent communication commands, EQUIV() removes these nodes from *node\_set*.

If node\_set contains two or more equivalent node subsets. EQUIV() nondeterministicly returns only one of these subsets. For example, let the CCSs of node\_set equal {(2:0S1, 3:1R2, 2R0, 3R0), (2:0S1, 3:1R2, 2R1, 3R1), (1:0R1, 1R3, 2:2S0, 3R0), (1:0R1, 1R0, 2:2S0, 3R0)}. The first and second entries in node\_set are equivalent and the third and forth entries in node\_set are equivalent. EQUIV() will return either the nodes corresponding to {(2:0S1, 3:1R2, 2R0, 3R0), (2:0S1, 3:1R2, 2R1, 3R1)} or {(1:0R1, 1R3, 2:2S0, 3R0), (1:0R1, 1R0, 2:2S0, 3R0)}. To select a node from a set of H nodes for testing if a subset of the nodes are equivalent, function EQUIV() calls function Select(). Function Select() randomly picks a node element from a set of nodes, removes the element from the set, and then returns this element.

If the return value of EQUIV() is not NULL, the returned nodes are represented with one node in the *POG*. This *POG* node is labeled with the sends and ready receives of the returned nodes.

The POG construction algorithm, Crt\_POG(), places information about the newly added nodes of the POG in the queue data structure VisitNodes. An entry in the VisitNodes queue has the format <node\_ptr, node\_set>. The entry node\_ptr points to a node of the POG, and node\_set is a set of one or more H nodes. The set node\_SuccSet is a set of H nodes that is built from the successors of equivalent nodes. The string Commos is set to the sends and ready receives of an H node and is for labeling the nodes of the POG. For example if the constructs the POG from H:

#### Crt\_POG()

```
Initialize queue VisitNodes to empty
   Create root node S (labeled root)
   Add \langle S.SUCC (root node of H) > as the first entry in the queue VisitNodes
   while (VisitNodes not empty)
       item = behead(VisitNodes)
                                                /* format of item is < node_ptr, state_set> */
       POG_ptr = item.node_ptr
                                                 /* state_set= {CCS_1, \ldots, CCS_m}, m \ge 1 */
       node\_set = item.node\_set
      while ((EQUIV_set = EQUIV(node_set) \neq \emptyset))
          Commos = the sends and ready receives of the CCSs of EQUIV_{set}
          Create POG node N and label with Commos
          Create an arc from node of POG_ptr to N
          node_SuccSet = \emptyset
          for each node of EQUIV_set
             node_SuccSet = node_SuccSet \cup SUCC(node)
          end for
          Add the entry \langle N. node_SuccSet \rangle to the tail of VisitNodes
          node_set = node_set - EQUIV_set
       end while
       for each node \in node_set
          if ((Commos = sends and ready receives of the CCS of node) \neq NULL)
             Create POG node N and label with Commos
             Create an arc from node of POG_ptr to N
             Add the entry \langle N.SUCC(node) \rangle to the tail of VisitNodes
          else
             Create POG node N and label as END node
             Create an arc from node of POG_ptr to N
          endif
      endfor
   end while
end algorithm
```

```
EQUIV (node_set)

node_set' = node_set

EQUIV_found = false

<u>while</u> (node_set' \neq \emptyset) AND (EQUIV_found = false)

Node_1 = Select(node_set')
```

```
EQUIV_set = \{Node_1\}
      Commos = the sends and ready receives of Node_1.CCS
      FGnode = Node_1.FGnode
      local_set = node_set'
      while (local_set \neq \emptyset)
          Node_2 = Select(local_set)
          Commos_2 = the sends and ready receives of Node_2.CCS
          FGnode2 = Node_2.FGnode
          if (Commos = Commos_2) AND (FGnode = FGnode2)
             EQUIV_{found} = true
             Add Node_2 to EQUIV_set
          end if
      end while
   end while
   if (EQUIV_found=true)
      return(EQUIV_set)
   else
      return(\emptyset)
end function
```

The POG represents the causal and concurrent relationship among the communication events. The first four properties of the POG are derived directly from the properties of H.

**Property 6.9** If  $e_i \rightarrow e_j$ , where  $e_i$  and  $e_j$  are communication events, and  $e_i$  is an entry in node N of the POG and  $e_j$  is an entry in node N' of the POG, then N is an ancestor of N'.

**Property 6.10** The communication events represented in a node of the POG are concurrent.

**Property 6.11** If POG node N is an ancestor of POG node N' and  $e_i \in N$  and  $e_j \in N'$ , then  $e_i \rightarrow e_j$  if one of the following is true:

1.  $\rho(i) = \rho(j)$ 

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- 2.  $e_i$  is a send to  $P_j$ ,  $e_j$  is a receive from  $P_i$ , and  $e_j$  is the corresponding receive for this send.
- 3.  $e_i \rightarrow e_k$  and  $e_k \rightarrow e_j$  where  $e_k \in N''$  such that N is an ancestor of N'' and N'' is an ancestor of N'.

**Property 6.12** The POG represents all partial orders.

The construction of the POG prunes the tree H with the EQUIV() function so that one branch of the POG from root to leaf node represents an unique partial order  $\alpha \in \mathcal{P}$ . The nodes of the POG are minimized from the nodes of H to represent only the communication commands that occur in an execution of the distributed system. The properties of H remain true in the POG since the construction does not eliminate or create new information about the occurrence of the communication events.

**Lemma 6.2** The construction of the POG from H preserves the causal and concurrent relationships represented in H.

#### **Proof.**

CASE 1. Nodes of H with equivalent communication commands do not exist.

Function EQUIV() always returns  $\emptyset$  for nodes of tree H; i.e., there exists no nodes of H that have equivalent communication commands.

Algorithm Crt\_POG() traverses H in a breath-first order with the use of queue Visit-Nodes. The next entry in VisitNodes represents the next group of nodes in H to be represented in the POG. Consider creating the nodes and edges of the POG.

#### NODES.

If a node of H, h, has at least one send or ready receive, the node is represented in the *POG* by creating a *POG* node and labeling it with the corresponding sends and ready receives of h.CCS.

If a node of H does not have at least one send or ready receive, a node is not created in the *POG* to represent this node. A node of H, h, that does not have at least one send or ready receive means no communication commands are executed after the sends and ready receives of h's parent, and therefore node hdoes represent any causal or concurrent relationships among events.

EDGES.

If a node of H, h, is represented in the POG by node n and if a child of h is represented in the POG with node n', then an edge is created from node n to node n' of the POG. Therefore, causal and concurrent relationships among nodes of H are preserved in the POG. Since all nodes of H that have at least one send or ready to receive are represented in the POG, all causal and concurrent relationships are preserved.

CASE 2. Nodes of H with equivalent communication commands do exist.

Function EQUIV() finds nodes of H that have equivalent communication commands. The nodes that are input to EQUIV() are nodes that occur in the same level of H. If the nodes of H, {  $h_1 \dots h_t$  }, are equivalent (the CCSs have equivalent communication commands) one node n is created in the POG to represent these t nodes and is labeled with the equivalent communication commands. Then set *node\_SuccSet* is built so that  $node\_SuccSet = SUCC(h_1) \cup \cdots \cup SUCC(h_t)$ . Set  $node\_SuccSet$  is placed in the queue *VisitNodes* for generating the children of node n. Therefore nodes of H that represent the same causal and concurrent relationships are represented as one node in the *POG*. and all causal and concurrent relationships that are represented by the successor nodes of  $\{h_1 \dots h_t\}$  will be represented in the *POG* as children of n.

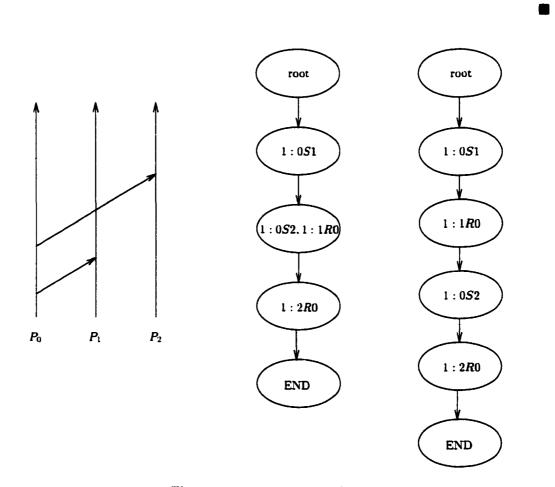


Figure 6.14: 2 possible POGs

A partial order  $\alpha \in \mathcal{P}$  is represented in the *POG* by a path beginning at the root node and ending at a leaf node of the tree. The process of generating the *POG* guarantees that there exists only one possible representation of a partial order in the *POG*. Figure 6.14 is the time-space diagram of a distributed system's execution and the two possible unique path representations of the partial order defined by the system's execution. From property 6.11 we can determine from either of the two paths the following relationships:  $1:0S1 \rightarrow 1:0S2, 1:0S1 \rightarrow 1:1R0, 1:0S2 \rightarrow 1:2R0$ , and 1:0S1 and 1:0S2 are concurrent. Of the two paths shown in figure 6.14, only the path to the left is generated by the  $Crt_POG()$  algorithm. Since the *POG* is derived from *H*, algorithm  $Crt_H()$  dictates the path that will occur in the *POG* for a partial order. The *H* generated by algorithm  $Crt_H()$  is shown in figure 6.15 for the execution shown in figure 6.14. The left path in 6.14 is generated from this *H*.

**Lemma 6.3** For partial order  $\alpha \in \mathcal{P}$ , there exists one possible representation of  $\alpha$  in the POG.

#### Proof.

A partial order is represented in the POG by a path beginning at the root node and ending at a leaf node of the tree.

Assume there exist two different representations of  $\alpha$  in the *POG*, thus there must exist two differing paths from the root node to a leaf node that correspond to  $\alpha$ . For this to occur, *H* must have at least one path from the root to a leaf node that corresponds to each path of  $\alpha$  in the *POG* (according to algorithm Crt\_POG() and lemma 6.2). Let *p* be one such path of *H*, and let *p'* be the other path of *H*. The nodes of paths *p* and *p'* must differ in the order that the sends and ready receives occur in the path to generate two different

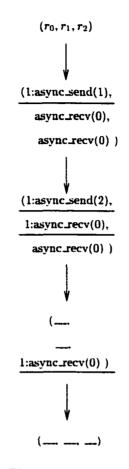


Figure 6.15: H tree

representations of  $\alpha$  in the *POG* (according to algorithm Crt\_POG() and function EQUIV()). For p and p' to differ in this manner, there must exist a node n of H that is common to both paths that has at least two children that mark the differing of paths p and p'. Let c be a child of n that corresponds to path p and let c' be a child of n that corresponds to path p'. For nodes c and c' to correspond to different paths in the *POG*, nodes c and c' must consist of different send and ready receives (according to algorithm Crt\_POG() and function EQUIV()).

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For node *n* to have children, node *n* must have at least one send or ready receive. Let  $v_i \in n$ where  $v_i$  is a send, iSj. The children of *n*, SUCC(*n*), are determined by the successors of iSj. S(iSj). For SUCC(n) = {c, c'}, S(iSj) must have two entries. For S(iSj) to have two entries, there must exist two branches in  $FG_i$  from the node of  $FG_i$  that corresponds to iSjsuch that each branch includes a successor of iSj. In  $FG_i$ , a branch indicates a different total order of events of  $P_i$ . Therefore c and c' of H mark the beginning of two different partial orders. and the *POG* paths that are derived from p and p' represent two different partial orders. A contradiction to our assumption has been reached.

Let  $v_i \in n$  where  $v_i$  is a ready receive. iRj. Since SUCC $(n) = \{c, c'\}$  occurs under the same conditions as when  $v_i = iSj$ , the same contradiction is reached for  $v_i = iRj$ .

**Property 6.13** Each path of the POG from root node to leaf node represents a unique partial order

#### Proof.

Assume two paths of the POG represent the same partial order. Two cases are possible for this to occur.

CASE 1. The two paths are identical.

For this to occur, there must exist a node of the POG that has two children that are identical. This contradicts function EQUIV().

CASE 2 . The two paths differ but represent the same partial order. This contradicts lemma 6.3.

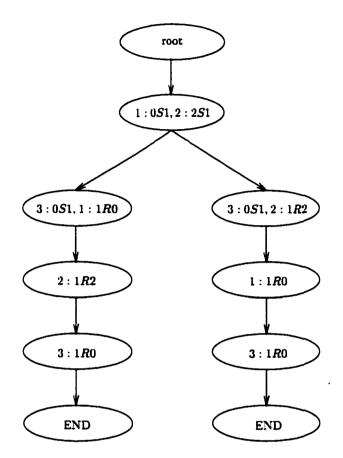


Figure 6.16: POG derived from H of figure 6.11

Figure 6.16 is the POG of the distributed program in figure 4.2. and this POG is generated from H shown in figure 6.11. Notice that the two partial orders of figure 4.3 are each represented as a path from root to a leaf node in the POG. In particular, the left path of the POG represents  $PO_1$ , and the right path of the POG represents  $PO_2$ .

## 6.4 LCP and LCP' Events

For an event  $e_i$ , each process's *LCP* and *LCP'* events can be determined from the *POG*. From theorem 4.1 and lemma 5.1, we know that for a partial order  $\alpha$  and event  $e_i$ , at most one  $CC(e_i)$  exists and this  $CC(e_i)$  consists of LCP events which are communication events. The causal global state for event  $e_i$  is identified by  $CC(e_i)$ . From theorem 5.2. we know that by piggybacking state data on the LCP and LCP' events. the  $CGState(e_i)$  is available in  $P_i$  for event  $e_i$ .

Before determining the LCP and LCP' events of the assert statement  $e_i$ , the last LCP'receive event that occurs in  $P_i$  must be identified for each execution path of  $P_i$  that includes  $e_i$ . "Last" means the receive event corresponding to the last of the latest causal messages that will piggyback state information to  $P_i$  for evaluating the assert statement. Since the assert statement and all possible executions of  $P_i$  are represented in  $FG_i$ , the last LCP'event(s) of  $P_i$  is(are) identified from  $FG_i$ .

The algorithm Bound\_Assert() determines the last LCP' event(s) of an event. Referring to figure 6.7. note that an async\_recv(0) of  $P_1$  has two parents. Since a node of  $FG_i$  can have more than one parent. the parents of each node are maintained as a linked list of node pointers. The variable *current\_list* is set to this linked list. The variable *NextBranch* is a stack. and an entry in the stack is a linked list of  $FG_i$  node pointers. The variable *Local\_LCPs* is a linked list of  $FG_i$  node pointers, and at the completion of the algorithm the entries in this linked list are the last LCP' receive events of an event in  $P_i$ .

The input to Bound\_Assert() is  $FG_i$  and  $assert_node$ . The variable  $assert_node$  is a pointer to the assert node in  $FG_i$ . Algorithm Bound\_Assert() begins the search for the last LCP' events of  $assert_node$  with the first parent node in  $assert_node$ 's  $current_list$ . The search continues by traveling up the tree until a receive event is found or the root node is reached. Each possible path from  $assert_node$  to the root node of  $FG_i$  is searched for a

receive event. In the case that multiple paths exist from the *assert\_node* to the root node, a different receive event may be found on each path. If a receive event is found on the path, this receive event is a last LCP' event and is placed in the linked list *Local\_LCPs*, and the search is stopped on this path. The output of the algorithm is *Local\_LCPs*.

Bound\_Assert()

```
current_list = the parent nodes of assert_node
   NextBranch = NULL
   Local_LCPs = NULL
   crnt_node = first entry in current_list
   Remove crnt_node from current_list
   receive_found = false
   do
      while (receive_found=false) AND (crnt_node \neq root node of FG_i)
          if (current\_list \neq NULL)
             Push current_list on the stack NextBranch
          endif
          if crnt_node = receive
             Add crnt_node to Local_LCPS
             receive_found = true
          else
             current_list = parent nodes of crnt_node
             crnt_node = first entry in current_list
             Remove crnt_node from current_list
          endif
      endwhile
      <u>if</u> (NextBranch \neq NULL)
          receive_found = false
          current_list = Pop(NextBranch)
          crnt_node = first entry in current_list
          Remove crnt_node from current_list
      endif
   while (NextBranch \neq NULL)
end algorithm
```

From Bound\_Assert() we have identified the last LCP' events in  $FG_i$ . The next step is to identify these same events in the POG. Each entry in Local\_LCPs is represented in

/\* input:  $FG_i$  and assert\_node \*/

the POG at least once if the execution of the receive is possible. To access the POG node that corresponds to an entry in Local\_LCPs, it is necessary to know which send and receive commands of the control flow graphs each POG node represents. When creating a POG node, a linked list of pointers is built that identifies the send and/or receive nodes of the control flow graph that the POG node represents. Also, each send or receive node of  $FG_i$ has a linked list of pointers to the POG nodes that represent this communication event. For each entry in Local\_LCPs, which is actually a pointer to the appropriate receive node in  $FG_i$ , the POG node(s) that represent the receive can be accessed.

If an entry in Local\_LCPs is represented by a POG node, then this receive is a LCP' event of assert\_node in  $P_i$ . If an entry in Local\_LCPs is not represented by a POG node, then this receive can not be executed and therefore is not an LCP' event.

Continuing with the distributed program shown in figure 4.2. we find the last LCP' events of  $P_1$  from figure 6.7 using algorithm Bound\_Assert(). Process  $P_1$  has only one such message. async\_recv(0). This is the async\_recv(0) that immediately precedes the assert statement in  $FG_1$ . Two nodes of the POG represent this communication command, one for partial order  $PO_1$  and the other for partial order  $PO_2$ . These two POG nodes are shown in figure 6.17 with double circles.

From theorem 5.2 we know for assert event  $e_i$  there exist a non-repetitive communication path from each *LCP* event to an *LCP'* event of  $P_i$  that consists of *LCP* and *LCP'* events. The algorithm Find\_LCPs() accesses the *POG* to find these *LCP'* and *LCP* events for the assert event  $e_i$ . For each partial order branch of the *POG* corresponding to an entry in *Local\_LCPs*, the algorithm traverses the branch in an upward direction beginning with

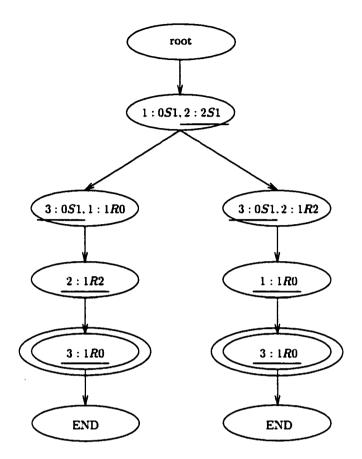


Figure 6.17: LCP and LCP' events

the receive event of *Local\_LCPs* up to possibly the root node to find these non-repetitive communication paths. Since the branch is traversed upward, the receives (LCP's) of the messages are encountered before the matching sends (LCPs).

When a receive event, c:jRk, is encountered in a POG node, it is a candidate LCP' event if:

1. a non-repetitive communication path has been found from  $P_j$  to  $P_i$  that occurs after c:jRk and a non-repetitive communication path from  $P_k$  to  $P_i$  has not been found, or

2. the receive event is an event of  $P_i$  and a non-repetitive communication path from  $P_k$  to  $P_i$  has not been found.

The reason for *candidate* is the receive event c:jRk is not an LCP' event of  $P_j$  if another non-repetitive communication path from  $P_k$  to  $P_i$  is found before<sup>2</sup> the matching send of c:jRk is encountered in the POG.

When a send event, c:jSk, is encountered in the POG, it is an LCP event if:

- 1. the matching receive. c:kRj, has been encountered, and
- 2. receive event, c:kRj, is a candidate LCP' event.

Six data structures are employed by algorithm Find LCPs () to find the LCP and LCP'events when traveling up a branch of the POG. Three of the six data structures are sets of process numbers. These sets are *FoundProcs*, *Sends*, and *Rec\_wo\_Sends*. The set *FoundProcs* contains the entry j if the piggybacking message for  $P_j$ , consisting of the send event of  $P_j$  and the matching receive event, has been determined from the POG. Set *Sends* contains the entry j if the send event for piggybacking data from  $P_j$  has been found. Set *Rec\_wo\_Sends* contains the entry j if the receive end of a piggybacking message has been found for  $P_j$  but the matching send has not. The other three data structures are queues: *RwoSQ*, *SendQ* and *RecvQ*. The queue *RwoSQ* contains entries for receive commands whose matching send command has not been found in the *POG*. An entry in *RwoSQ* has the format  $\langle c, i, j, POGnode \rangle$  where c is the counter, i is process number of the receiver,

<sup>&</sup>lt;sup>2</sup>Before in this context meaning the path happens after the matching send since the POG is traversed upward

*j* is the process number of the sender, and *POGnode* is a pointer to the *POG* node that contains the receive. The queue *SendQ* contains an entry for each *LCP* send event. and an entry has the format  $\langle c, j. POGnode \rangle$  where *c* is the counter. *j* is the process number of the sender and *POGnode* is a pointer to the *POG* node containing the send event. The queue *RecvQ* contains an entry for each *LCP'* receive event, and an entry has the format  $\langle c, j,$ *POGnode* where *c* is the counter. *j* is the process number of the receiver and *POGnode* is a pointer to the *POG* node containing the receive event.

Find\_LCPs()

/\* Input: Local\_LCPs Output: SendQ, RecvQ \*/

for each entry in Local\_LCPs where the event format is  $c:iR_j$ for each POG node that contains c:iRjPOGnode = POG node that contains c:  $iR_j$  $FoundProcs = Sends = \emptyset$  $Rec\_wo\_Sends = \{i\}$ RwoSQ = NULLInsert  $\langle c, i, j, POGnode \rangle$  in RwoSQPOGnode = ParentOf(POGnode)while (POG node  $\neq$  root node) AND (FoundProcs  $\neq$  ({ 0, ..., N-1 } - i)) for each receive. c:jRk. in POGnode if  $(j \in Sends)$  OR (j = i) AND  $(k \notin FoundProcs)$ AND (*Rec\_wo\_Sends* does not have entry jRk) Insert  $\langle c, j, k. POGnode \rangle$  in RwoSQ $Rec_wo_Sends = Rec_wo_Sends + j$ endif endfor for each send, c:jSk, in POGnode if  $(k \in \text{Rec.wo.Sends}) \text{AND}((\text{Recv_POGnode} = \text{SearchQ}(c, k, j)) \neq \text{NULL})$ **if** (*RwoSQ* does not have an entry with k as the receiver)  $Rec_wo_Sends = Rec_wo_Sends - k$ endif Sends = Sends + iFoundProcs = FoundProcs + jInsert  $\langle c, j, POGnode \rangle$  in SendQ Insert  $\langle c, k, Recv\_POGnode \rangle$  in RecvQendif endfor

### POGnode = ParentOf(POGnode) <u>endwhile</u> <u>endfor</u> <u>endfor</u> end algorithm

The if statements of the algorithm are complex and require explanation. When a receive event c:jRk occurs in a POG node, the following check is made:

if  $((j \in \text{Sends}) \text{ or } (j = i))$  and  $(k \notin \text{FoundProcs})$ and  $(Rec_wo_Sends \text{ does not have entry } jRk)$ 

The value j being in the set Send indicates a non-repetitive communication path has been found from  $P_j$  to  $P_i$  that occurs after this receive. Any data received by  $P_j$  from receive event c:jRk can then be piggybacked on the messages of the path to  $P_i$ . If j = i, then the receive is a local event of the process evaluating the assert. The data piggybacked on the message of this receive event will be available to the assert statement without having to piggyback the data on additional messages. The value k being in FoundProcs indicates the LCP and LCP' events for piggybacking the state information of  $P_k$  have been found, and the message associated with this receive is not needed for piggybacking data from  $P_k$ to  $P_i$ . If the if statement evaluates to true, the receive event is a candidate LCP' event.

Assume  $P_j$  has two or more jRk receive events, and one jRk is already inserted in RwoSQ. If the other jRk receive events are encountered by the algorithm, they should not be considered as LCP' events since there execution occurs before the jRk that is represented in RwoSQ. The last condition of the if statement prevents these events from being considered.

When a send event c:jSk occurs in a POG node, the following check is made first:

if 
$$(k \in Rec_wo_Sends)$$
 and  $((Recv_POGnode = SearchQ(c, k, j)) \neq NULL)$ 

The value k being in the Rec\_wo\_Sends set indicates  $P_k$  has a receive event that is a candidate LCP' event and the matching send event has not be found. For this send to be the matching send event, the receive for  $P_k$  must be expecting a message from  $P_j$ . The function SearchQ() searches the queue RwoSQ for the occurrence of the entry  $\langle c. k. j. POGnode \rangle$ . If found, the entry is deleted from RwoSQ and POGnode is returned. If not found, NULL is returned. The if statement evaluating to true indicates this send, c:jSk, is an LCP event and the matching receive pointed to by Recv\_POGnode is an LCP' event. The nested if statement checks whether k should be removed from Rec\_wo\_Sends.

#### if (RwoSQ does not have an entry with k as the receiver)

If. after SearchQ() removes the entry corresponding to c:jSk. RwoSQ has an entry where  $P_k$  is the receiver of a message, then there is a possibility that  $P_k$  has additional LCP' events. The value k should remain in  $Rec\_wo\_Sends$  to indicate that receives of  $P_k$  are candidate LCP' messages. If RwoSQ does not have an entry where  $P_k$  is the receiver of a message, then the value k is removed from  $Rec\_wo\_Sends$ .

Since we have identified the last LCP' events of the distributed program shown in figure 4.2, we next identify the LCP and LCP' events. For each partial order, the LCP and LCP' events are determined with algorithm Find\_LCPs(). The steps taken by Find\_LCPs() to find the LCP and LCP' events of partial order  $PO_1$  are given. For each iteration of

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the algorithm's loop, the variables values are shown. The values of the variables before executing the loop are:

Rec\_wo\_Sends = 
$$\{1\}$$
  
FoundProcs =  $\emptyset$   
Sends =  $\emptyset$   
 $i = 1$   
RwoSQ = (<3,1,0,3:1R0>)  
SendQ = NULL  
RecvQ = NULL  
POGnode = 2:1R2

For the first iteration of the loop, the if statement  $((j \in Sends) \text{ OR } (j = i))$  AND  $(k \notin \text{FoundProcs})$  AND  $(Rec\_wo\_Sends$  does not have entry jRk) evaluate to true for event 2:1R2. The values of the variables after this iteration are:

$$Rec\_wo\_Sends = \{1\}$$

$$FoundProcs = \emptyset$$

$$Sends = \emptyset$$

$$i = 1$$

$$RwoSQ = (<3.1,0.3:1R0 >, <2.1.2.2:1R2 >)$$

$$SendQ = NULL$$

$$RecvQ = NULL$$

$$POGnode = 3:0S1,1:1R0$$

For the second iteration of the loop, the if statement ( $k \in \text{Rec.wo}$ .Sends AND (*Recv\_POG-node* = SearchQ(c, k, j))  $\neq$  NULL) evaluates to true for event 3:0S1. The values of the variables after this iteration are:

 $Rec.wo\_Sends = \{1\}$   $FoundProcs = \{0\}$   $Sends = \{0\}$  i = 1 RwoSQ = (<2,1,2,2:1R2>) SendQ = (<3,0.3:0S1>) RecvQ = (<3,1.3:1R0>)POGnode = 1:0S1, 2:2S1

For the third iteration of the loop, the if statement ( $k \in \text{Rec\_wo\_Sends AND}$  (*Recv\_POG-node* = SearchQ(c, k, j))  $\neq$  NULL) evaluates to true for event 2:2S1. The values of the variables after this this iteration are:

$$Rec\_wo\_Sends = \emptyset$$
  
 $FoundProcs = \{0.2\}$   
 $Sends = \{0.2\}$   
 $i = 1$   
 $RwoSQ = NULL$   
 $SendQ = (<3.0.3:0S1>. <2.2.2:2S1>)$   
 $RecvQ = (<3.1.3:1R0>. <2.2.2:1R2>)$   
 $POGnode = root$ 

The condition of the while loop evaluates to false, and the LCP and LCP' events for  $PO_1$  are identified in SendQ and RecvQ. The LCP events are 3:0S1 and 2:2S1, and the LCP' events are 3:1R0 and 2:1R2. For  $PO_2$ , algorithm Find\_LCPs() identifies the LCP events 3:0S1 and 2:2S1, and the LCP' events 3:1R0 and 2:1R2. These events are underlined in figure 6.17. In this particular example, the LCP and LCP' events are the same for both partial orders, but this is not always the case. Notice that the send and receive of the first

message from  $P_0$  to  $P_1$  are not identified as LCP and LCP' events. This message need not be used for piggybacking data.

The properties resulting from this algorithm are:

- 1. Event  $e_j$  is an *LCP* event if and only if event  $e_j$  is an entry in *SendQ*.
- 2. Event  $e_j$  is an LCP' event if and only if event  $e_j$  is an entry in RecvQ.

These two properties establish that our technique for identifying LCP and LCP' events is valid. Two lemmas are prerequisites for proving these properties.

**Lemma 6.4** If Find\_LCPs() adds send event  $e_k$  to SendQ,  $e_k$  is an event of a non-repetitive communication path, and  $e_k$  is an LCP event.

#### Proof.

Event  $e_i$  is the assert event of  $P_i$ .

#### BASIS.

If  $e_k = c:kSi$ ,  $k \in Rec\_wo\_Sends$  and RwoSQ has the entry  $\langle c.i, k. POG\_node \rangle$ , then c:kSi is an event of the non-repetitive communication path c:kSi, c:iRk and  $e_k$  is an LCP event.

Proof: By definition 5.2, c:kSi, c:iRk is a a non-repetitive communication path. The send event c:kSi is the *LCP* event of  $P_k$  if  $c:kSi \rightarrow c:iRk$  and there does not exist another send event  $e'_k$  such that  $c:kSi \rightarrow e'_k \rightarrow c:iRk \rightarrow e_i$ . Since c:kSi is the corresponding send to c:iRk (*RwoSQ* has the entry  $\langle c, i, k, POGnode \rangle$ ) then  $c:kSi \rightarrow c:iRk \rightarrow e_i$ , and since  $k \in Recv.wo.Send$ ,  $e'_k$  does not exist. INDUCTIVE HYPOTHESIS.

The events  $jRk, jSl, lRj, \dots mSi, iRm$  form a non-repetitive communication path of length n, and  $iRm \rightarrow e_i$ .

INDUCTIVE STEP.

If  $e_k = c:kSj$ , then

- the send event c:kSj is added to the non-repetitive communication path jRk,
   jSl. lRj. ....mSi.iRm to form the non-repetitive communication path kSj,
   jRk. jSl. lRj. .... mSi.iRm of length n + 1, and
- 2. the send event c:kSj is an LCP event.

Proof:

The event c:kSj is the corresponding send of c:jRk, and the relationship  $c:kSj \rightarrow c:jRk$  is true Therefore.  $kSj, jRk, jSl, lRj, \ldots, mSi, iRm$  is a non-repetitive communication path (definition 5.2) of length n + 1. Event c:kSj is added to SendQ by algorithm Find\_LCPs() when it is found to be part of the non-repetitive communication path.

We know  $c:kSj \rightarrow e_i$  since c:kSj is an event of  $kSj, jRk, jSl, lRj, \ldots, mSi, iRm$  and  $iRm \rightarrow e_i$ . From the basis and  $c:kSj \rightarrow e_i$ , we can conclude that c:kSj is an *LCP* event.

**Lemma 6.5** If Find\_LCPs() adds receive event jRk to RecvQ, jRk is an event of a nonrepetitive communication path and jRK is an LCP' event.

#### Proof.

For event jRk to be added to RecvQ, k must first be an entry in  $Rec\_wo\_Sends$  and RwoSQ contains the entry for c:jRk. For these to exist, we know from algorithm Find\_LCPs()

- $j \in Sends$  or j = i, and
- $k \notin FoundProcs$

Consider the two possibilities:

1.  $j \in Sends$  and  $k \notin FoundProcs$ .

From lemma 6.4. if  $j \in Sends$ , a non-repetitive communication path exists from a *LCP* send of  $P_j$ , *jSl*. to a *LCP'* event of  $P_i$ , *iRm*: *jSl*,...,*iRm*. And for  $k \notin$ *FoundProcs*, the *LCP* and *LCP'* of  $P_k$  have not been found in the *POG*. We can also conclude that  $jRk \rightarrow jSl$ . For *jRk* to be added to *RecvQ*, the send *kSj* must have been found in an ancestor node of the of *jRk* (from algorithm Find\_LCPs()). Therefore,  $kSj \rightarrow jRk$ . From this we can conclude the send event corresponding to *jRk*. *kSj*. is found and is an *LCP* event (Lemma 6.4). *jRk* is an *LCP'* event, and *jRk* is an event of the non-repetitive communication path kSj, *jRk*, *jSl*....*iRm*.

2. j = i and  $k \notin FoundProcs$ . Event jRk is a receive event of the process evaluating the assert, and the *LCP* event of  $P_k$  has not been found. Then for jRk to be added to *RecvQ*, the send kSj has been found in the *POG*, is the *LCP* event of  $P_k$  and forms the non-repetitive communication path kSj, jRk (lemma 6.4). Since jRk is the corresponding receive of kSj, jRk is an *LCP*' event. **Property 6.14** Event  $e_j$  is an LCP event if and only if event  $e_j$  is an entry in SendQ.

#### Proof.

PART 1. If  $e_i$  is an *LCP* event, then  $e_i$  is in *SendQ*.

Proof by contradiction.

Assume  $e_j = jSk$  is an *LCP* event but is not in *SendQ*. Since jSk is an *LCP* event, there exists a non-repetitive communication path  $jSk, kRj, kSl, lRk, \ldots, mSi, iRm$ that consists of *LCP* and *LCP'* event where  $jSk \rightarrow kRj \rightarrow kSl \rightarrow lRk \rightarrow \cdots \rightarrow$  $mSi \rightarrow iRm$  (theorem 5.1 and definition 5.2). For jSk to not be in *SendQ*, kRj is not in *RwoSQ* and k is not in *Rec\_wo\_Sends*. For this to occur either

- 1.  $j \in FoundProcs$  or
- 2.  $k \notin Sends$ .
- 1. For j to be in FoundProcs. another  $e'_j$  exists where  $e'_j$  is in SendQ and  $e'_j$  is an LCP event of  $P_j$ . But since  $P_j$  can have only one LCP event (lemma 4.1) a contradiction has been reached.
- 2. For  $k \notin Sends$ , kSl, the *LCP* event of  $P_k$ , is not in *SendQ*. The same reasoning holds as to why each *LCP* event of the non-repetitive communication path jSk, kRj, kSl, lRk,...,mSi, iRm is not in *SendQ* except for mSi. For mSi to not be an *LCP* event, iRm is not recognized as an *LCP'* event. For iRm to not a *LCP'* event, m must be in *FoundProcs*. For m to be *FoundProcs*, a send event  $e_m$  and a receive event  $e'_i$  exist where  $mSi \rightarrow iRm \rightarrow e_m \rightarrow e'_i$ . Thus  $e_m$  is the

LCP event of  $P_m$  (definition 4.1). A contradiction has been reached since mSi is the LCP event of  $P_m$ .

PART 2. If  $e_j$  is in SendQ, then  $e_j$  is an LCP event.

Proof. This follows directly from lemma 6.4.

**Property 6.15** Event  $e_j$  is an LCP' event if and only if event  $e_j$  is an entry in RecvQ.

#### Proof.

PART 1. If  $e_j$  is an LCP' event, then  $e_j$  is in RecvQ.

Proof.

If  $e_j = jRk$  is a receive LCP' event, then jRk is part of a non-repetitive communication path to an LCP' event of  $P_i$  that consists of LCP and LCP' events, jSk, kRj, kSl, lRk,  $\dots mSi$ , iRm (theorem 5.1). We know the LCP sends are entries in SendQ (property 6.14). If the sends are entries in SendQ, then the corresponding receives are also entries in RecvQ according to algorithm Find\_LCPs().

PART 2. If  $e_j$  is in RecvQ, then  $e_j$  is an LCP' event.

Proof. This follows directly from lemma 6.5.

## 6.5 POG and Taylor's Complete Concurrency History

Taylor's work motivated our static analysis to generate the *POG* for representing the possible executions of a distributed system, but our static analysis algorithms have been developed independent of Taylor's work. The only portion of our static analysis that is a derivation of Taylor's static analysis is representing each process with a flow graph and the successor relationship between nodes of the graph.

A path of the POG has a different meaning from a path in Taylor's complete concurrency history. A path of Taylor's history represents a possible total ordering of i/o rendezvous and does not represent the concurrent execution of i/o rendezvous. Each path of the *POG* represents a partial order of the distributed system, and a path does represent the concurrency of the communication commands. One or more of Taylor's paths can correspond to one path of the POG since one or more total orders can correspond to the same partial order.

## 6.6 Static Analysis in the Parallel Domain

Work in the parallel domain that is most closely related to ours is the automated parallelization of sequential code. Parallelizing compilers collect data flow information for a source program and use this information to detect potential parallelism, determine an appropriate grain size, and then transform the program into a functionally equivalent parallel program that can exploit the underlying architecture. These compilers also aim at automating the selection of data distributions and reducing nonlocal data accesses in distributed memory systems.

The majority of the data flow analysis performed by these compilers is dependence analysis. Two computations that have a dependence relationship means that constraints on their execution order are present. By identifying these constraints with dependence analysis, it can be determined whether transformations of the source code will alter the semantics of the computation.

Two types of dependencies that can be identified with data flow analysis are data and control. Consider two statements, a and b, of a sequential program. Statement b is control dependent on statement a, if a determines whether b executes. Statements a and b have a data dependence if they cannot be executed simultaneously because of conflicting uses of the same variable.

Dependence analysis performed at the procedure and function level is useful for identifying coarse grain parallel transformations [35, 17, 24, 23, 36]. Dependence analysis performed at the loop level is useful for identifying fine grain parallelism [6, 10, 11, 9, 25, 36]. Languages, such as Fortran D [34], provide commands the programmer uses to annotate the sequential program with data decompositions. The compiler then performs dependence analysis to determine the computation decomposition [2]. Other languages [32, 2] exist in which the compiler determines both data and computation decompositions with the aid of dependence analysis.

The objective of the compiler is to produce parallel code in which the execution is maximally parallel and nonlocal data accesses are minimized. Dependency analysis provides information for achieving this objective. Initially our static analysis appeared similar to the static analysis performed by parallelizing compilers. By comparing the two more closely, the similarities are only superficial. A parallelizing compiler generates control flow graphs of the sequential program and performs sequential data flow analysis. The compiler uses these results to create a functionally equivalent parallel program and decompose the sequential program's data. As part of this process, the necessary communication commands are also created. Our work generates control flow graphs for the source code of the distributed processes to analyze the communication. The source code is already comprised of communication commands. We do not perform dependence analysis and we do not add communication to the distributed system.

In the next chapter, the analysis of distributed programs with the addition of loops is described. The distributed programs in chapter 2 are analyzed in chapter 8, and the LCP and LCP' events determined. These programs further demonstrate the benefits of identifying LCP and LCP' events for reducing the number of messages that piggyback data.

## Chapter 7

# Loops

Chapter 6 presented algorithms for creating the  $FG_i$ , H and POG graphs. Algorithms where also presented for determining the LCP and LCP' events of an assert statement from the POG. These algorithms did not support loops in the source code of the distributed processes. In this chapter we make the additions to the algorithms to allow loops, and the algorithms are modified so all properties and lemmas of chapter 6 are preserved. By concluding with the preservation of properties 6.14 and 6.15, we demonstrate that our technique remains valid for identifying LCP and LCP' events.

## 7.1 Control Flow Graphs

Three loops constructs can occur in the source code of a process: do - while. while, and for. Each loop has one unique entry point and one unique exit point. Nesting of loops are allowed, but each loop has its own entry and exit point. Neither goto nor break statements are allowed in the source code since either can create additional entry or exit points for loops. Algorithm Create\_FG<sub>i</sub>() requires additions for representing loops in  $FG_i$ . Each loop in a process's source code is represented as a cycle in the process's corresponding flow graph. The cycle is accomplished with a *back edge* from the exit point of the loop to the entry point of the loop. The concept of a *dominating* node is necessary to define a back edge. A node *a* of flow graph  $FG_i$  *dominates* node *b* of  $FG_i$  if every path from the root node of  $FG_i$  to node *b* passes though *a*. If (*a*. *b*) is an edge, then *a* is the initial node and *b* is the terminal node. An edge is a back edge if its terminal node dominates its initial node. An edge of a flow graph that is not a back edge is referred to as either a forward edge or an edge.

The control flow graph for a process.  $FG_i$ , requires additional node types for representing loops. The entry point of a loop is represented with a head node, and the exit point of a loops is represented with a tail node. The head and tail of a while loop are nodes labeled WHILE and END\_WHILE, respectively. The head and tail of a do - while loop are nodes labeled DO and END\_DO. respectively. The head and tail of a for loop are nodes labeled FOR and END\_FOR, respectively. The nodes that occur between the head and tail nodes make up the body of the loop.

The while and for loop are similar in that the loop condition is evaluated at the head of the loop. The loop body is executed zero or more times. This type of loop is referred to as a *precondition* loop. The loop condition of the **do** loop is evaluated at the tail of the loop so the loop body is executed one time before testing the condition. This type of loop is referred to as a *postcondition* loop.

Algorithms Create\_FG<sub>i</sub>() and AddNode() are repeated from chapter 6 with the additions required for the loop constructs. Figure 7.1 shows the three loop constructs represented

by a portion of a control flow graph. The dashed edges between nodes indicate the edges added by algorithm AddNode() when *NewNode* is added to the flow graph. A back edge is added by Create\_FG<sub>i</sub>() for any one of the loop constructs from the tail of the loop (e.g., END\_WHILE node) to the head of the loop (e.g., WHILE node). The back edge creates a cycle in the graph.

Three additional stacks and three additional variables are required to handle loops in algorithm  $Create_FG_i()$ . The stacks are *WhileStack*. *DoStack* and *ForStack*. The three pointer variables are *TopDoStack*, *TopWhileStack*, and *TopForStack*. Each pointer references the top entry of its respective stack. The stacks are initially empty, and the pointers are initially NULL. The stacks are used to match the begin and end of the loop constructs.

| $Create_{FG_i}()$                                      | /* Input: P <sub>i</sub> ; Output: FG <sub>i</sub> */ |
|--|---|
| Create the ROOT node of $FG_i$                         |   |
| CrtNode = ROOT node                                    |   |
| if an assignment statement is recognized               |   |
| Add assignment statement to the tail of t              | he linked list  |
| if an async_send is recognized                         |   |
| if the linked list is not empty                        |   |
| AddNode (CrtNode, ASSIGN)                              | /* for the assignment statements */                   |
| linked list is set to empty                            |   |
| AddNode(CrtNode. SEND)                                 |   |
| if an async_recv is recognized                         |   |
| if the linked list is not empty                        |   |
| AddNode(CrtNode, ASSIGN)                               | /* for the assignment statements */                   |
| linked list is set to empty                            |   |
| AddNode(CrtNode, RECEIVE)                              |   |
| if an assert is recognized                             |   |
| if the linked list is not empty                        |   |
| AddNode(CrtNode, ASSIGN)                               | /* for the assignment statements */                   |
| linked list is set to empty                            |   |
| AddNode(CrtNode, ASSERT)                               |   |
| $\mathbf{if}$ an $\mathbf{if}$ statement is recognized |   |
| if the linked list is not empty                        |   |
|  |   |

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| AddNode(CrtNode, ASSIGN)<br>linked list is set to empty | /* for the assignment statements $*/$   |
|---|---|
| AddNode(CrtNode, IF)                                    | /* for the if statement */  |
| Push CrtNode onto the stack                             | , <b>j</b> , <b>j</b> , ,   |
| TopStack = CrtNode                                      |   |
| if an else is recognized                                |   |
| AddNode(CrtNode, END_IFSIDE                             | )   |
| if the linked list is not empty                         |   |
| Set field in <i>CrtNode</i> to point                    | to linked list  |
| linked list is set to empty                             |   |
| TopStack.HoldPtr = CrtNode                              | /* Set HoldPtr of the IF node to the */   |
| ·   | /* address of the END_IFSIDE */   |
| CrtNode = top entry of the stack                        |   |
| CrtNode.AddEdgeFlag = true                              | /* Flag an edge needed from END_IFSIDE node  */ /* to the first node following END_ELSE node */ |
| if the end of the else side of an if/els                | · · ·   |
| AddNode(CrtNode, END_ELSE)                              | /* for the ending of the else side */   |
| if the linked list is not empty                         |   |
| Set field in <i>CrtNode</i> to point                    | to linked list  |
| linked list is set to empty                             |   |
| CrtNode.HoldPtr = TopStack.Ho                           | ldPtr /* Move the address of the END_IFSIDE */  |
|   | <pre>/* node to the END_ELSE node */</pre>  |
| CrtNode.AddEdgeFlag = true                              | /* Flag an edge will be needed from END_IFSIDE */   |
|   | /* node to the first node following END_ELSE node */  |
| Pop the stack   |   |
| $\underline{if}$ the end of an if statement is recog    | mized   |
| AddNode(CrtNode. END_IF)                                | <pre>/* for the ending of the if statement */</pre>   |
| if the linked list is not empty                         |   |
| Set field in <i>CrtNode</i> to point                    | to linked list  |
| linked list is set to empty                             |   |
| CrtNode.HoldPtr = TopStack                              | <pre>/* Set the HoldPtr of END_IF node */</pre>   |
|   | <pre>/* to the address of the IF node */</pre>  |
| CrtNode.AddEdgeFlag = true                              | /* Flag an edge will be need from the IF node $*/$  |
|   | /* to the first node following the END_IF node */   |
| Pop the stack   |   |
| if a while statement is recognized                      |   |
| if the linked list is not empty                         |   |
| AddNode(CrtNode, ASSIGN)                                | /* for the assignment statements */   |
| linked list is set to empty                             |   |
| AddNode(CrtNode, WHILE)                                 | /* for the if statement */  |
| Push CrtNode onto WhileStack                            |   |
| Top WhileStack = CrtNode                                |   |
| $\underline{\mathbf{if}}$ a for statement is recognized |   |
| if the linked list is not empty                         |   |
| AddNode (CrtNode, ASSIGN)                               | /* for the assignment statements */   |

| linked list is set to empty                    |   |
|--|---|
| AddNode(CrtNode, FOR)                          | /* for the if statement */                    |
| Push CrtNode onto ForStack                     |   |
| TopForStack = CrtNode                          |   |
| if a do statement is recognized                |   |
| if the linked list is not empty                |   |
| AddNode (CrtNode, ASSIGN)                      | /* for the assignment statements */           |
| linked list is set to empty                    | , , , ,                                       |
| AddNode(CrtNode, DO)                           | /* for the if statement */                    |
| Push CrtNode onto DoStack                      |   |
| TopDoStack = CrtNode                           |   |
| if the end of a while loop is recognized       |   |
| AddNode (CrtNode, END_WHILE)                   | /* for the end of the while loop $*/$         |
| if the linked list is not empty                |   |
| Set field in <i>CrtNode</i> to point to linked | list  |
| linked list is set to empty                    |   |
| • •  | hileStack /* create cycle in the graph */     |
| •  | /* Set the HoldPtr of END_WHILE node */       |
|  | /* to the address of the WHILE node */        |
| CrtNode.AddEdgeFlag = true /* Indica           | ate an edge will be needed from the WHILE */  |
|  | first node following the END_WHILE node */    |
| Pop WhileStack                                 | ,,  |
| if the end of a for loop is recognized         |   |
| AddNode (CrtNode, END_FOR)                     | /* for the end of the for loop $*/$           |
| if the linked list is not empty                | , jet ale cha oj ale jet teop ,               |
| Set field in <i>CrtNode</i> to point to linked | list  |
| linked list is set to empty                    |   |
| Add back pointer from CrtNode to TopFa         | orStack /* create cycle in the graph */       |
| CrtNode.HoldPtr = TopForStack                  | /* Set the HoldPtr of END_FOR node */         |
|  | /* to the address of the FOR node */          |
| CrtNode.AddEdgeFlag = true /*                  | Indicate an edge will be need from the FOR */ |
| •••  | the first node following the END_FOR node */  |
| Pop ForStack                                   | , , , , , , , , , , , , , , , , , , ,         |
| if the end of a do loop is recognized          |   |
| AddNode (CrtNode, END_DO)                      | /* for the end of the do loop $*/$            |
| if the linked list is not empty                |   |
| Set field in <i>CrtNode</i> to point to linked | list  |
| linked list is set to empty                    |   |
|  | /* create cycle in the graph for loop */      |
| Add back pointer from CrtNode to node          |   |
| Pop DoStack                                    |   |
| if the current control construct or statement  | is not recognized                             |
| Generate an error and halt                     |   |
| if the end of the source code is recognized    |   |
| AddNode(CrtNode, END)                          |   |
|  |   |

If the linked list is not empty Set field in *CrtNode* to point to linked list linked list is set to empty

### end algorithm

The only valid exit point of a postcondition loop is from the tail of the loop. Algorithm AddNode() creates an edge from the END\_DO node to the first node added to the graph after the END\_DO node (*NewNode*). The only valid exit point of a precondition loop is from the head of the loop. Algorithm AddNode() creates an edge from the WHILE node and the FOR node to the first node that occurs after the loop's end node.

```
AddNode(CrtNode, type)
NewNode = Allocate a node
if CrtNode ≠ END_WHILE, END_FOR
Create a directed edge from CrtNode to NewNode
if CrtNode.AddEdgeFlag
Create a directed edge from the node CrtNode.HoldPtr to NewNode
if type = ASSIGN
Set field in NewNode to point to assignment linked list
CrtNode = NewNode
end algorithm
```

Algorithm AddNode() does not require additional code or modification to create the edge from the exit point of a do-while loop. Additional code is required for the exit point of the while and for loops. To create an edge from a WHILE or FOR node to *NewNode*, the same steps are taken when an edge is added from an IF node to the END\_IF node. The description of this process is presented in terms of the while loop, but is generalized to any precondition loop. When the END\_WHILE node is added, the address of the WHILE node, available on top of *WhileStack*, is stored in the END\_WHILE node. This is accomplished with the following line from Create\_FG<sub>i</sub>():

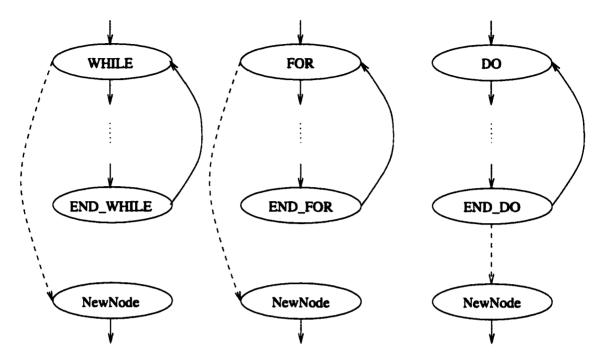


Figure 7.1: Control flow graph of the loop constructs

### CrtNode.HoldPtr = TopWhileStack

When NewNode is added to  $FG_i$ . the address of the WHILE node is available in CrtNode so that AddNode() can create an edge from the WHILE node to NewNode. The flag AddEdgeFlag of the END\_WHILE node is set to true to indicate that function AddNode() should add an edge from the WHILE node to NewNode.

Properties 6.1 through 6.4 correspond to the control flow graphs. Properties 6.2 and 6.4 are not affected by loops, but property 6.1 requires some modification when loops occur in the source code.

First we will consider precondition loops. Consider the while loop shown in figure 7.2. If the loop is executed zero times, the happens before relationship among the nodes is: WHILE  $\rightarrow$  S2

If the loop is executed one time, the happens before relationships among the nodes are:

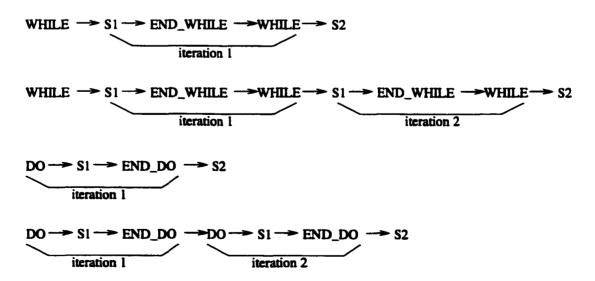
WHILE  $\rightarrow$  S1  $\rightarrow$  END\_WHILE  $\rightarrow$  WHILE  $\rightarrow$  S2

A new iteration of the loop is begun when the first node of the loop body is executed. In this example, node S1 is the first node of the loop body. The last node of an iteration is the WHILE node. If i iterations of a precondition loop occur, the WHILE node is executed i+1times, and the back edge is followed i times. Consider the case when the loop is executed two times. The happens before relationships are:

WHILE  $\rightarrow$  S1  $\rightarrow$  END\_WHILE  $\rightarrow$  WHILE  $\rightarrow$  S1  $\rightarrow$  END\_WHILE  $\rightarrow$  WHILE  $\rightarrow$  S2

The following summarizes the happens before relationships and the beginning and ending of loop iterations for the while loop.





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The happens before relationship and the beginning and ending of loop iterations are also shown for do-while loops, which will be discussed next.

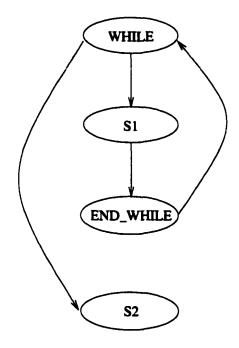


Figure 7.2: Control flow graph with a while loop

According to property 6.1. if a path exists from node a to node b. then  $a \rightarrow b$  when both are executed. By examining the happens before relationship between the S1 node and the END\_WHILE node, we see that property 6.1 requires updating. A path exists from node END\_WHILE to node S1 in figure 7.2. but it is not the case that END\_WHILE  $\rightarrow$  S1 when one iteration of the loop occurs. Consider two iterations of the loop. The END\_WHILE of the first iteration does not happen before the S1 of the first iteration, but the END\_WHILE of the first iteration does happen before the S1 of the second iteration. In general, END\_WHILE  $\rightarrow$  S1 if

1. the loop is executed 2 or more times

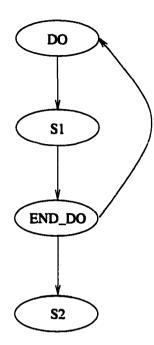


Figure 7.3: Control flow graph with a do - while loop

- 2. END\_WHILE occurs in iteration i of the loop, and
- 3. S1 occurs in iteration i + 1 or greater.

Next we need to examine the postcondition loop. Figure 7.3 shows a flow graph for a do loop. If the loop is executed only one time, the happens before relationships among the nodes are:

 $DO \rightarrow S1 \rightarrow END_DO \rightarrow S2.$ 

The happens before relationships for two executions of the loop are:

 $DO \rightarrow S1 \rightarrow END_DO \rightarrow DO \rightarrow S1 \rightarrow END_DO \rightarrow S2.$ 

The boundary nodes of an iteration for a postcondition loop are different than those of a precondition loop. The first execution of DO begins iteration 1 of the loop, and END\_DO

completes that iteration. If the loop is iterated i times, DO and END\_DO are executed i times, and the back edge is followed i - 1 times.

Consider the happens before relationship between S1 and END\_DO. A path exists from the END\_DO node to the S1 node, but the relationship END\_DO  $\rightarrow$  S1 is true only if

- 1. the loop is executed more than once,
- 2. END\_DO occurs in iteration i, and
- 3. S1 occurs in an iteration greater than i.

Property 6.1' subsumes property 6.1 to account for the occurrence of loops. The property is given in two parts for completeness, but only part 1 is modified. The variable l is used to denote a loop.

### Property 6.1'

PART 1. If a path exists from node a to node b in  $FG_i$ , then  $a \rightarrow b$  when

- 1. a and b are both executed and a back edge is not part of the path from node a to node b, or
- 2. a and b are both executed, the back edge of loop l is part of the path from node a to b, node a occurs in iteration i of loop l and node b occurs in iteration j, where j > i, of loop l, or
- 3. a and b are both executed, the back edge of loop l is part of the path from node a to b, loop l is a precondition loop, nodes a and b occur in the same iteration, and node b is the head of the loop.

PART 2. If  $a \rightarrow b$  when both a and b are executed, then a path exists from node a to node b in  $FG_i$ .

Condition (1) of part 1 is equivalent to property 6.1. Conditions (2) and (3) quantify which happen before relationships are possible with the addition of back edges. Condition (2) of part 1 allows the relationship END\_WHILE  $\rightarrow$  S1 of figure 7.2 when multiple iterations of the loop occur, and S1 occurs in a later iteration than END\_WHILE. Also notice that this condition allows the happens before relationship WHILE  $\rightarrow$  WHILE where the first WHILE occurs in an earlier iteration than the second. As for postcondition loops, the condition S1  $\rightarrow$  DO is allowed for figure 7.3 when two or more iterations occur. Condition (3) of part 1 allows S1  $\rightarrow$  WHILE when both occur in the same iteration.

## 7.2 H Graph

With the possibility of loops in the source code of each process of the distributed system. loops are also possible in H. In the algorithm for constructing H, additions are required for detecting the repeated execution of communication commands and representing these repetitions as cycles in H. Cycles occur in H if

- 1. a send command is in the body of a loop and the send is possible.
- 2. a send command is *possible*, the matching receive is *ready*, and both occur in the body of a loop, or
- 3. a combination of (1) and (2).

Cycles are created in H with back edges. The graph retains the properties of a tree; there exist a root node and leaf nodes. The terminology *ancestor*, *descendent*, *parent* and *child* will remain in use for the relationships defined by forward edges. The relationships between nodes defined by back edges will be discussed following the modified Crt\_H() algorithm.

Properties 6.5 through 6.8 and lemma 6.1 correspond to the H graph. The substantial changes to the H graph construction algorithm do not invalidate these properties and lemma. The node relationship *ancestor* is fundamental to properties 6.5 and 6.7, and these properties remain valid with the clarification of the *ancestor* relationship. Properties 6.6 and lemma 6.1 are not affected by loops. Property 6.8 is discussed following the modified Crt\_H() algorithm.

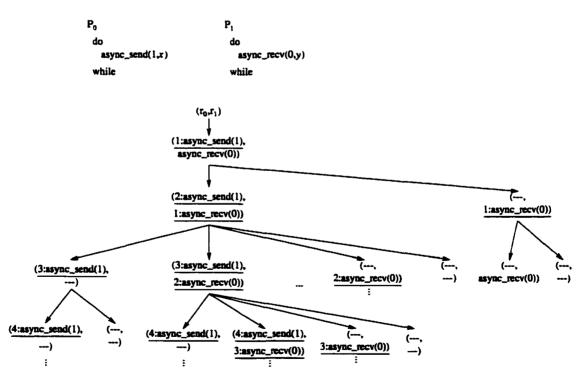


Figure 7.4: Example 1

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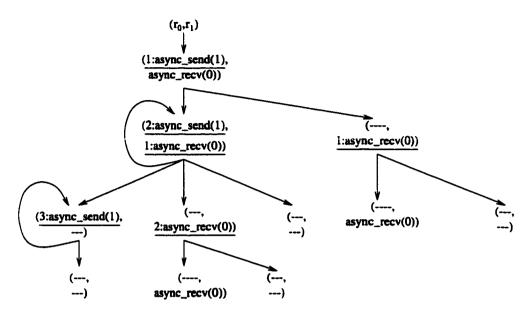


Figure 7.5: Example 1 with back edges

The detection of loops in H requires significant additions to the Crt\_H() algorithm. Two examples, useful for describing the additions to Crt\_H(), demonstrate the occurrence of loops in H. The first example is a two process distributed system. The source code of each process and the graph resulting from algorithm Crt\_H() in chapter 6 is shown in figure 7.4. The graph H can not accurately represent the execution of this distributed system without back edges. Communication commands are repeatedly executed, but the loops are not shown as cycles in H since this version of the algorithm does not detect loops. A pattern can be observed in H. The nodes (2:async\_send(1), 1:async\_recv(0)) and (3:async\_send(1), 2:async\_recv(0)) of figure 7.4 represent the same state of the system. Although the counters corresponding to the sends and receives differ, the send in each node represents the same command in  $P_0$ , and the receive in each node represents the same command in  $P_1$ . Another system state is represented by nodes (3:async\_send(1),---) and (4:async\_send(1),---) of figure 7.4. The complete H graph with the inclusion of back edges is shown in figure 7.5.

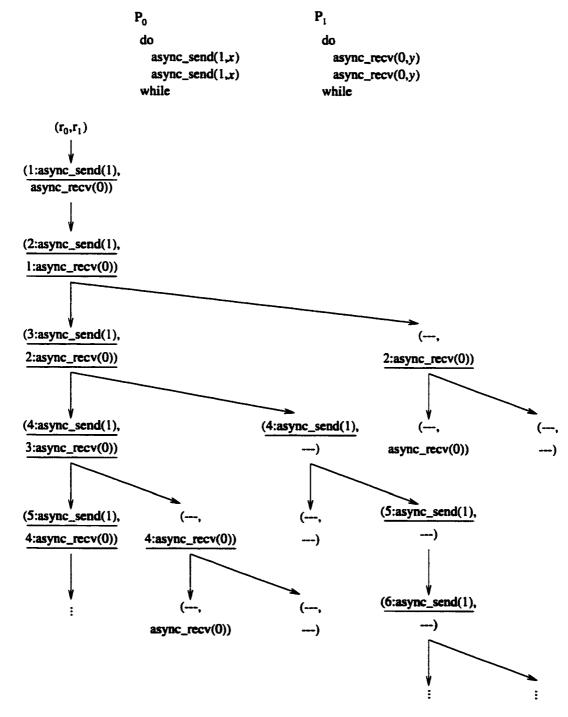


Figure 7.6: Example 2

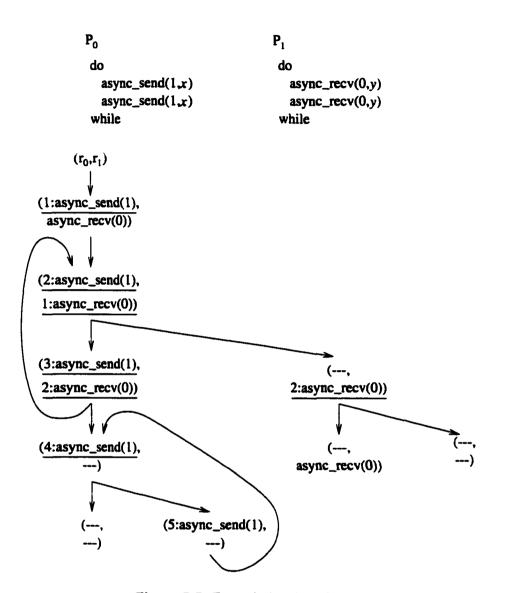


Figure 7.7: Example 2 with back edges

Loop detection is more difficult in the example of figure 7.6. The nodes (2:async\_send(1), 1:async\_recv(0)) and (3:async\_send(1), 2:async\_recv(0)) syntactically appear to represent the same state. but they do not. The node (2:async\_send(1), 1:async\_recv(0)) represents the first send of  $P_0$  and the first receive of  $P_1$ , whereas the node (3:async\_send(1), 2:async\_recv(0)) represents the second send in  $P_0$  and the second receive in  $P_1$ . Nodes (2:async\_send(1), 1:async\_recv(0)) and (4:async\_send(1),3:async\_recv(0)) represent the same state of the system, and nodes (3:async\_send(1),2:async\_recv(0)) and (5:async\_send(1),4: async\_recv(0)) represent another state of the system. The complete H graph representing the execution of the distributed system with back edges is given in figure 7.7

Additional information is required to detect and represent loops in H. For each node, n, of H the following information is needed.

- A temporary back edge, temp\_back, used by Crt\_H() is a field of n.
- An array of node pointers that are the children of *n*. *Kids[MAXEDGES]* is a field of *n*. Each entry represents a child that is the result of a forward or back edge. The forward edge children occur first in the array.
- An array of integers *Kid\_type[MAXEDGES]*, where *Kid\_type[i]* indicates the type of edge for *Kids[i]*, is a field of *n*. A zero entry indicates a forward edge, and a one entry indicates a back edge.
- An array of pointers to the parents nodes of n. Parents[2], is a field of n. Entry Parents[0] is the parent of n that is defined by a forward edge. Each node has a parent from a forward edge. If a node is pointed to by a back edge, then the node also has a parent that is defined by a back edge. The entry Parent[1] is the parent of n that is defined by a back edge or NULL if the n is not pointed to by a back edge. An example of a parent resulting from a back edge is node (3:async\_send(1), 2:async\_recv(0)) which is a parent of (2:async\_send(1), 1:async\_recv(0)) of figure 7.7.

When node n is added to H, a check is made to determine if the state represented by this node has already been represented by another node in n's execution path. This is done by comparing n with its ancestors. First n is compared with its parent. If the parent does not represent the same state, then the grandparent is compared against n. This continues until either a node that represents the same state of n is found or the root node is reached.

Two comparisons are required to determine if node n and its ancestor node, n'. represent the same state. The first comparison identifies syntactically identical nodes. Syntactically identical meaning that for each entry,  $v_i$ , in n, there exists  $v'_i$  in n' which is identical with the exception of the counter value. If nodes n and n' are syntactically identical, the second comparison is necessary to determine whether the nodes represent the same state. For each pair of entries,  $v_i$  and  $v'_i$ , where  $v_i$  and  $v'_i$  are not equal to the inactive marker, the test insures that FGnode[i] of n is equal to FGnode[i] of n'. If FGnode[i] of n is equal to FGnode[i] of n', both point to the same node of  $FG_i$ . Passing the test implies that  $v_i$  and  $v'_i$  represent the same command of  $P_i$ . If the test is true for each pair,  $(v_i, v'_i)$ , then the two nodes represent the same state.

If the ancestor node n' represents the same state as node n, then n' is possibly the entry point of a loop, and the parent of n is possibly the exit point of this loop. The next decision is whether to add a back edge from the parent of n to n' to form the loop. Two cases exist for the relative location of nodes n and n' in H.

- 1. The parent of node n is also node n'.
- 2. The parent of node n is not node n'. Node n' is an ancestor of the parent of node n.

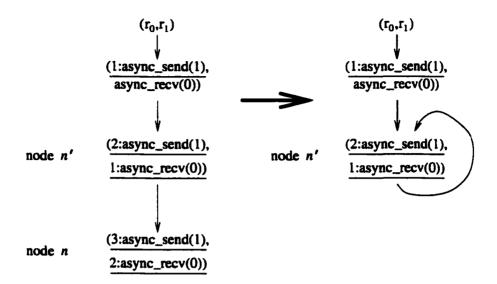


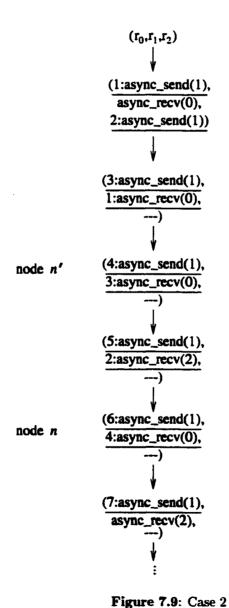
Figure 7.8: Case 1

If case 1 is true then a loop has been detected in H. A back edge is added from n' to itself, and node n is removed from H. Figure 7.8, the portion of figure 7.4 needed to demonstrate case 1, shows the transformation of H when the loop is detected. Case 2 requires more information to determine whether a loop has been found in H. Figure 7.9 is a distributed system that demonstrates case 2. Nodes n' and n represent the same state, but adding a back edge from the parent of n to n' would be incorrect. The state represented by node (5:async\_send(1), 2:async\_recv(2), —) does not recur after node n. Additionally, the state represented by nodes n and n' does not recur after node n.

Continuing to generate nodes of the execution path that includes n and n' is necessary to determine if a loop exists in H. If the nodes from n' to the parent of n are duplicated immediately after n, a loop exists in H. A back edge is added from the parent of n to n'creating a cycle. Node n and its descendants are removed from H. The algorithm Check\_Loops() checks for cases 1 and 2. Determining whether a back edge should be added for case 2 requires the use of field  $temp\_back$ . Whenever case 2 is true. Check\_Loops() sets the field  $temp\_back$  of n's parent to point to n'. Figures 7.10 and 7.11 demonstrate the use of  $temp\_back$ . The dashed edge represents the value of  $temp\_back$ . Figures 7.10 and 7.11 show the generation of H in figure 7.6 as each node is added. Only the portion of H relevant to the addition of a back edge is shown.

Step 3 of figure 7.10 shows the first occurrence case 2. Nodes n and n' represent the same state and a temporary back edge  $(temp\_back)$  is added from the parent of nto n'. A back edge can not be added until it is known that the state represented by node (3:async\\_send(1). 2:async\\_recv(0)) occurs again immediately after node n. The node added in step 4. (5:async\\_send(1), 4:async\\_recv(0)). represents the same state as node (3:async\\_send(1). 2:async\\_recv(0)). A temporary back edge is added from the parent of n (4:async\\_send(1). 3:async\\_recv(0)) to n' (3:async\\_send(1). 2:async\\_recv(0)). When this temporary back edge is added, n' also has a temporary back edge that points to node (2:async\\_send(1), 1:async\\_recv(0)). This indicates that the state of nodes (2:async\\_send(1), 1:async\\_recv(0)) and (3:async\\_send(1), 2:async\\_recv(0)) are repeated by (4:async\\_send(1), 3:async\\_recv(0)) and (5:async\\_send(1), 4:async\\_recv(0)) nodes. The temporary back edge of node n' becomes the back edge, and the nodes after n' are removed as shown in the resulting H.

| Po                    | <b>P</b> <sub>1</sub>      | P <sub>2</sub>  |
|-----------------------|----------------------------|-----------------|
| :                     | :                          | :               |
| async_send(1,x)       | async_recv(0,y)            | async_send(1,z) |
| do<br>async_send(1,x) | do<br>async_recv(0,y)      |                 |
| while()               | async_recv(2,y)<br>while() |                 |



rigure 1.9. Case 2

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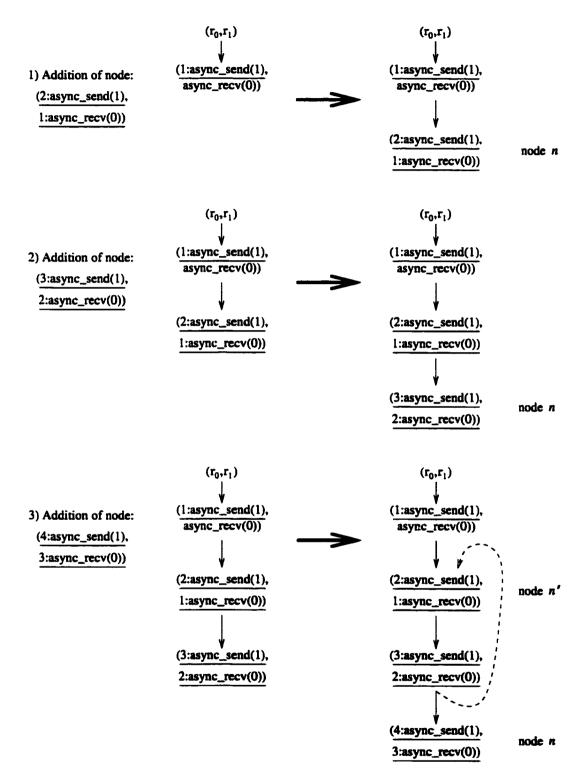


Figure 7.10: Detecting a loop

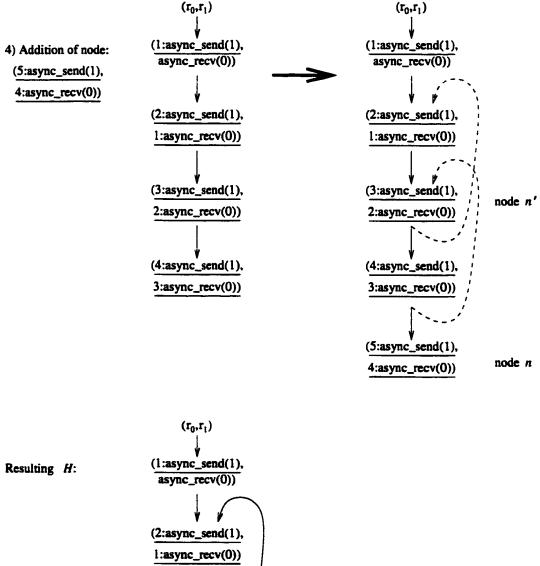


Figure 7.11: Detecting a loop

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(3:async\_send(1), 2:async\_recv(0))

When node n is added to H, algorithm Crt\_H() invokes algorithm Check\_Loops() to check for the existence of a loop with the additional node. Algorithm Check\_Loops() checks the ancestors of n for a node representing the same state as n. If one is found, the variable *Poss\_Head* is set to the matching node, and variable *Poss\_Tail* is set to the parent of n. If *Poss\_Head* and *Poss\_Tail* refer to the same node, an occurrence of case 1 is found, a back edge is added from *Poss\_Head* to itself, and node n is removed from H. If case 2 is verified, nodes from the parent of *Poss\_Tail* to *Poss\_Head* are traversed checking for values in *temp\_back*. If all nodes have values in *temp\_back*, then the loop has been repeated. In *Poss\_Head*, the value of *temp\_back* is replicated as the back edge. If any node has no value in *temp\_back*, the potential loop body has not been repeated.

When a loop is added to H, nodes require removal. If a back edge is added for case 1, then only node n needs to be removed. When a back edge is added for case 2, the nodes and their children that were created to duplicate the loop body must be removed. When traversing H from the parent of *Poss\_Tail* to *Poss\_Head*, the variable *prev\_traverse* is set to the previously checked node. If a back edge is added, node *prev\_traverse* and its children are removed by the **Remove\_Nodes()** function. Entries may remain in *CCS\_Q* for children of the removed node. When a node is removed from H, the queue *CCS\_Q* is scanned for entries whose parent is the removed node. If any are found, they are removed from *CCS\_Q* by the **RemoveQ()** function.

Crt\_H() Initialize queues  $Msg_Q_0, \ldots, Msg_Q_{N-1}, CCS_Q$  to empty Initialize array  $counter[0] \ldots counter[N-1]$  to 0 Create root node r  $r.CCS = CCS_0$ Determine\_SUCC( $r, CCS_0, Msg_Q_0, \ldots, Msg_Q_{N-1}, CCS_Q$ ) 147

while CCS\_Q is not empty  $item = behead(CCS_Q)$ /\* format of item is <node, list,  $Q_0, \ldots, Q_{N-1}$ , counter> \*/ Parent = item.nodeLL = item.list $Msg_Q_0,\ldots,Msg_Q_{N-1} = item.Q_0,\ldots,item.Q_{N-1}$ counter = item.counterfor each <CCS, FGnode> entry in LL Create a node n in Hn.CCS = CCSn.FGnode = FGnodeAddEdge(Parent, n)Determine\_SUCC( $n, CCS, Msg_Q_0, \dots, Msg_Q_{N-1}, counter, CCS_Q$ ) end for end while end algorithm

```
Determine_SUCC(n, CCS, Msg_Q_0, \ldots, Msg_Q_{N-1}, counter, CCS_Q)
   Msg_Q'_0,\ldots,Msg_Q'_{N-1} = Msg_Q_0,\ldots,Msg_Q_{N-1}
   counter' = counter
   Loop = false
   if (n = \text{root node})
       SUCC(CCS) = Generate_SUCC(n) /* < CSS, FG node> is entry in SUCC(CCS) */
       if (SUCC(CCS) \neq NULL)
           Add \langle n.SUCC(CCS), Msg_Q'_0, \dots, Msg_Q'_{N-1}, counter' \rangle to the tail of CCS_Q
       end if
   else
       for i = 0 to N - 1
           if (v_i \text{ of } CCS = \operatorname{async} \operatorname{recv}(j))
               if (Msg_Q'_i \text{ has entry } < counter, j >)
                    /* v_i is a ready receive */
                  item = behead first <counter, j > entry in Msg_{-}Q_{i}
                  append item.counter to v_i in CCS
                                                                 /* item.counter:async_recv(j) */
               end if
           end if
       end for
       for i = 0 to N - 1
           \underline{if}(v_i \text{ of } CCS = async\_send(j))
               counter/j]'++
               Add \langle counter/j \rangle, i > to Msg_Q'_i
               Append counter[j]' to v_i in CCS
           end if
       end for
       Loop = Check Loop(n)
                                                                  /* Changes for loop start here */
       if(Loop = false)
```

```
SUCC(CCS) = Generate_SUCC(n)
if (SUCC(CCS) \neq NULL)
Add < n, SUCC(CCS), Msg_Q'_0, \dots, Msg_Q'_{N-1}, counter'>
to the tail of CCS_Q
end if
end if
/* Changes for loop stop here */
end if
end if
```

```
Check Loop(n)
   Found_Match = false
   Poss_Head = n.parent(0)
                                /* Check if an ancestor of n represent the same state of n */
   while (Poss_Head \neq ROOT) AND (Found_Match = false)
      Found_Match = Check_Dup(n, Poss_Head)
      if (Found_Match = false)
         Poss_Head = Poss_Head.parent[0]
      endif
   endwhile
   if (Found_Match = true) /* Poss_Head represents the same state as n. Does loop exist? */
      Poss_Tail = n.parent[0]
      if (Poss_Head = Poss_Tail)
                                                                            /* Case 1 */
         Add_BackEdge(Poss_Head. Poss_Tail)
         RemoveNodes(n)
         return(true)
      else
                                                                            /* Case 2 */
         traverse_node = Poss_Tail.parent(0)
         while (traverse_node \neq Poss_Head) AND (traverse_node.temp_back \neq NULL)
             prev_traverse = traverse_node
             traverse_node = traverse_node.parent/0]
         end while
         if (traverse_node \neq Poss_Head) OR
                                                                /* a potential back edge */
             ((traverse_node = Poss_Head) AND (Poss_Head.temp_back = NULL))
             Poss_Tail.temp_back = Poss_Head
             return(false)
         else
                                                       /* a loop exists, add the back edge */
             Add_BackEdge(Poss_Head.temp_back, Poss_Head)
             RemoveNodes(prev_traverse)
             return(true)
         endif
      endif
   endif
end function
```

```
Check_Dup(node1, node2)
   CCS1 = node1.CCS
   CCS2 = node2.CCS
   i = 0
   Equal = true
   while (i < N) AND (Equal = true)
      if (v_i \in CCS1 = v_i \in CCS2) /* Do not compare counter that may be appended to v_i */
         if ( node1.FGnode[i] \neq node2.FGnode[i])
             Equal = false
         end if
      else
         Equal = false
      endif
      i++
   end while
   return(Equal)
end function
Remove_Nodes(n)
   index = 0
   while (n.Kids/index) \neq \text{NULL})
      Remove_Nodes(n.Kids/index/)
      index++
   end while
   Delete n
   RemoveQ(n)
end function
RemoveQ(CCS)
   item = head of CCS_Q
   while (item \neq NULL)
      if item.parent = CCS
         Remove item from CCS_Q
      end if
      item = next entry in CCS_Q
   end while
end function
```

AddEdge(parent, n) i = 0<u>while</u> (parent.Kids[i]  $\neq$  NULL) i++<u>end while</u> parent.Kids[i] = n n.Parents[0] = parent <u>end function</u>

```
Add_BackEdge(n, parent)

i = 0

while (parent.Kids[i] \neq NULL)

i++

end while

parent.Kids[i] = n

n.Parents[1] = parent

end function
```

The addition of back edges to H represents the repeated execution of a portion of the distributed system's execution. When following a possible execution path of H and a back edge occurs in the path, this back edge represents an iteration of the loop associated with the back edge. If, when considering only the forward edges of H.

- nodes a and b are in an execution path in H,
- nodes a and b are both nodes of the same loop, and
- node a is an ancestor of node b.

then, when considering forward and back edges,

- b is an ancestor of a when b occurs in iteration i of the loop and a occurs in an iteration greater than i, and
- a is an ancestor of b when a occurs in iteration i and b occurs in iteration i or greater.

Referring back to figure 7.7, node (2:async\_send(1), 1:async\_recv(0)) is an ancestor of node (3:async\_send(1), 2:async\_recv(0)), and node (3:async\_send(1), 2:async\_recv(0)) is an ancestor of (2:async\_send(1), 1:async\_recv(0)). The first ancestor relationship is inherent, but the second is only possible with the addition of the back edge. The second relationship is true only when node (3:async\_send(1), 2:async\_recv(0)) occurs in iteration i and node (2:async\_send(1), 1:async\_recv(0)) occurs in an iteration greater than i.

If node a is an ancestor of node b, then b is a descendant of a. The children of a are the descendants of a whose path length from a is equal to one. This path can be a forward or back edge. If b is a child of a, then a is the parent of b.

Property 6.8 states that tree H represents all the partial orders of the distributed system. Without back edges in H, the number of partial orders is finite. If H has back edges, the partial orders are known but the number of partial orders is potentially infinite. A bound is not known for the number of times a loop can be iterated. Each path from the root to a leaf node that includes a back edge represents a group of partial orders that have a repeating pattern. Graph H continues to represent all the partial orders.

### 7.3 POG

In chapter 6, the input to the algorithm  $Crt_POG()$  is the tree H and the output is the POG. With the possibility of back edges in H, the POG can also have back edges. Only the function EQUIV() of algorithm  $Crt_POG()$  is affected by the addition of back edges in H. Properties 6.9 through 6.13 and Lemmas 6.2 and 6.3 correspond to the POG. We

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demonstrate that these properties and lemmas are maintained with the addition of back edges.

Function EQUIV() serves the same function as described in chapter 6. However, the inclusion of back edges requires additional tests to determine equivalency of H nodes. Suppose CCS and CCS' are found to have equivalent communication commands, and the nodes that represent CCS and CCS' are n and n'. Function EQUIV() must check whether

1. n or n' is pointed to by a back edge, or

2. n or n' has a back edge.

Function EQUIV() calls function Check\_Back() to determine if either (1) or (2) are true. If neither (1) nor (2) occurs. n and n' are equivalent. Both cases require further tests to determine equivalence.

In case (1), if only one of the nodes is referenced by a back edge, then n and n' are not equivalent. When nodes n and n' are each pointed to by a back edge, both node n are entry points of loops in H. The next test determines whether the loop associated with node n is equivalent to the loop associated with node n'. The recursive function TreeCmp() of algorithm Crt\_POG() determines the equivalence of the two loops.

Node back is the node that has a back edge to node n, and node back' is the node that has a back edge to node n'. Nodes n and back define a subtree. Node n is the root node, and the nodes that are descendants of n but not the descendants of back comprise the nodes of the subtree. The variable subtree is the subtree defined by nodes n and back. Nodes n' and back' also define a subtree, subtree'. The two subtrees are traversed in lock step, starting at the root node, in depth first order. The current node of *subtree*, c, is compared against the current node of *subtree'*, c'. If

- 1. the CCS of node c is equivalent to the CCS of node c', and
- 2. the number of children of c is equal to the number of children of c'

then the traversal of the subtree continues. If either condition is false, the loops are not equivalent and the traversal stops. If both subtrees are completely traversed without falsifying either condition, then the loops are equivalent. If the loops are equivalent, then nodes n and n' are represented by a single node in the *POG*. The nodes of the equivalent loops, that are not the entry and exit points of the loop, will be united by the original EQUIV() algorithm.

If case 2 is found to be true, then the following two tests are required to determine the equivalence of n and n':

- 1. both n and n' have a back edge. and
- 2. the H node pointed to by the back edge of n is equivalent to the H node pointed to by the back edge of n'.

Function Check\_Node() is called by EQUIV() to determine if these two tests are true. If both tests are passed, both n and n' will be represented by a single node in the POG.

The equivalent H nodes described in test 2 will already be represented by one node of the POG as a result of the previous case. A single back edge will be added from the

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#### CHAPTER 7. LOOPS

POG node that represents n and n' to the POG node representing the equivalent H nodes pointed to by the back edges of n and n'.

One additional field is added to the H nodes to transform H into the POG. The field POGnode is added to point to the POG node representing this H node. More than one H node may have the same value of POGnode since one POG node represents equivalent H nodes. The POG nodes also require additional fields that are replicated from the H nodes:

- Kids[MAXEDGES]
- Kid\_type[MAXEDGES]
- Parents[MAXEDGES]

These POG node fields are functionally equivalent to their H node counterparts. Field Kids[MAXEDGES] is an array of pointers to the children of the POG node. Each entry represents either a forward or back edge. Field  $Kid_type[MAXEDGES]$  is an array of integers indicating the type of edge for each entry. Forward edge have a zero entry, while back edges have a one entry. Pointers to the parents of the POG node are maintained in the array Parents[MAXEDGES].

Algorithm Crt\_POG() and function EQUIV() are shown with required back edge additions. Supportive functions are also shown.

Crt\_POG()
Initialize queue VisitNodes to empty
Create root node S (labeled root)
Add <S, KidsOf(root node of H)> as the first entry in the queue VisitNodes

```
while (VisitNodes not empty)
      item = behead(VisitNodes)
                                               /* format of item is < node_ptr. node_set> */
      POG_ptr = item.node_ptr
      node_set = item.node_set
                                                /* node_set= {node1,...,nodem}, m > 1 */
      while ((EQUIV_set = EQUIV(node_set) \neq \emptyset))
         Commos = the sends and ready receives the CCSs of EQUIV_{set}
         Create POG node N and label with Commos
         AddEdge(POG_ptr, N)
         Node\_SuccSet = \emptyset
         for each node of EQUIV_set
             Node_SuccSet = Node_SuccSet \cup KidsOf(node)
         end for
         Add the entry \langle N, Node_SuccSet \rangle to the tail of VisitNodes
         node_set = node_set - EQUIV_set
      end while
      for each nodeofnode_set
         if ((Commos = sends and ready receives of the CCS of node) \neq NULL)
             Create POG node N and label with Commos
             AddEdge(POG_ptr. N)
             Add the entry \langle N. KidsOf(node)> to the tail of VisitNodes
         else
             Create POG node N and label as END node
             AddEdge(POG_ptr. N)
         endif
      endfor
   end while
end algorithm
EQUIV (node_set)
   node_set' = node_set
   EQUIV_{found} = false
   while (node_set' \neq \emptyset) AND (EQUIV_found = false)
      Node_1 = Select(node_set')
      EQUIV\_set = \{Node\_1\}
      Commos = the sends and ready receives of Node_1.CCS
      FGnode = Node_1.FGnode
      Back_Found1 = Check_Back(Node_1)
```

 $Commos_2 =$  the sends and ready receives of Node\_2.CCS

**if** (Commos = Commos\_2) AND (FGnode = FGnode2)

 $local\_set = node\_set'$ while (local\\_set  $\neq \emptyset$ )

 $Node_2 = Select(local_set)$ 

 $FGnode2 = Node_2.FGnode$ 

```
Back_Found2 = Check_Back(Node_2)
             if (Back_Found1 = Back_Found2)
                case Back_Found1
                0:
                    EQUIV_found = true
                    Add Node_2 to EQUIV_set
                1:
                   if (TreeCmp(Node_1, Node_2, Node_1.parent/1], Node_2.parent/1]))
                       EQUIV_found = true
                       Add Node_2 to EQUIV_set
                   end if
                2:
                   if (Check_Node(Node_1, Node_2))
                       EQUIV_found = true
                       Add Node_2 to EQUIV_set
                   end if
                end_case
             end if
         end if
      end_while
   end while
   if (EQUIV_found=true)
      return(EQUIV_set)
   else
      return(\emptyset)
end function
Check_Back(Node)
    /* Check 1: Is Node pointed to by a back edge? */
   <u>if</u> (Node.parent[1] \neq NULL)
      return(1)
    /* Check 2: Does Node have a back edge? */
   i = 0
   while (Node.Kids/i) \neq NULL)
      if (Node.Kid_Type/i) = 1)
          return(2)
      end if
      i++
```

```
end while

/* Neither check 1 nor check 2 is true */

return(0)

end function
```

```
Check_Node(Node_1, Node_2)
   i = 0
   while (Node_1.Kid_Type/i) = 0)
                                                                /* find back edge in Node_1 */
       i++
   end while
   BackNode1 = Node_1.Kid/i
   i = 0
   while (Node_2.Kid_Type/i) = 0)
                                                                /* find back edge in Node_2 */
       i++
   end while
   BackNode2 = Node_2.Kids[i]
   if (BackNode1.POGNode = BackNode2.POGNode)
       return(true)
   else
       return(false)
   end if
end function
TreeCmp(Root1. Root2, Term1. Term2)
   Kids1 = Root1.Kids
   Kids2 = Root2.Kids
   if ((Kids1 has no entries AND Kids2 has no entries) AND (Root1.CCS = Root2.CCS))
       return(true)
   end if
   if ((number of entries in Kids1 \neq number of entries in Kids2)
       OR (Root1.CCS \neq Root2.CCS))
          return(false)
   end if
   i = 0
   <u>while</u> (Kids1[i] \neq NULL)
       if ((Kids1[i] \neq Term1) \text{ AND } (Kids2[i] \neq Term2))
          \underline{if} (TreeCmp(Kids1[i], Kids2[i], Term1, Term2) = false)
              return(false)
          end if
       else
          if (((Kids1[i] = Term1) \text{ AND } (Kids2[i] \neq Term2))) \text{ OR}
              ((Kids1[i] \neq Term1) \text{ AND } (Kids2[i] = Term2)))
              return(false)
```

# <u>end if</u> <u>i++</u> <u>end while</u> return(true) <u>end function</u>

```
\begin{aligned} \text{KidsOf}(node) \\ kidset &= \text{NULL} \\ i &= 0 \\ \underline{\text{while}}(node.Kids[i] \neq \text{NULL}) \\ \underline{\text{if}} node.Kid\_type[i] &= 0 \\ & \text{Add} node.Kids[i] \text{ to } kidset \\ \underline{\text{end if}} \\ i++ \\ \underline{\text{end while}} \\ \text{return}(kidset) \\ \underline{\text{end function}} \end{aligned}
```

Properties 6.9. 6.10. 6.11. and 6.12 are derived directly from the properties of H and are affected by back edges as described in section 7.2. Lemmas 6.2 and 6.3 and property 6.13 remain true with the addition of loops in H and the *POG*. Modification of algorithm Crt\_POG() is limited to additional checks for equivalency of nodes of H. The construction of the *POG* continues to preserve the causal and concurrent relationships in H. Property 6.13 states that each path from the root node to a leaf node of the *POG* represents a unique partial order. If there exists a path from the root node to leaf node n that contains a loop, then a different path exists from the root to n when the nodes of the loop are repeated. The last modifications pertain to the algorithms Bound\_Assert() and Find\_LCPs() that determine the LCP and LCP' events. Lemmas 6.4 and 6.5 and properties 6.14 and 6.15 correspond to the identification of the LCP and LCP' events. These lemmas and properties are not affected by the possible occurrence of back edges in the POG. Two modifications are required for Bound\_Assert(). The first modification stops searching a path for the last LCP' event when the ASSERT node occurs in the body of a loop. Without back edges in flow graph  $FG_i$ , the search stopped when either a RECEIVE node or the root node was encountered. With back edges the search should also stop if the ASSERT node itself is encountered. When Bound\_Assert() searches for a RECEIVE node in the flow graph of figure 7.12 two paths are searched. One is the path including only the FOR node and the RECEIVE node. The search stops at the RECEIVE node. The other path starts at the FOR node. proceeds to the END\_FOR node by following the back edge. The next node in the path is the ASSERT node. The search terminates since a receive does not exist on the path from the ASSERT node back to itself. If a RECEIVE node exists between the END\_FOR node and the ASSERT node, as shown in figure 7.13, the RECEIVE is a last LCP' event and is added to the linked list Local\_LCPs. In this case, the search succeeds when the **RECEIVE** node is encountered.

The second modification is needed when a loop occurs in the path being searched, but the ASSERT node is not part of the loop body. Without modification, the nodes of a loop will be followed infinitely if the loop occurs prior to the ASSERT node and a RECEIVE node is not found. The flow graph in 7.14 demonstrates the problem. The path ASSIGN, FOR, END\_FOR, SEND, FOR, END\_FOR, SEND, ... is repeatedly traveled unless a modification is made. When searching a path for a RECEIVE node, each node is flagged as *visited* when it is encountered. Before following a parent of a node in a search path, the visited flag of that node is tested. If it has not been set, then this path is searched. If it has been previously visited, this path is not searched.

For completeness, we repeat algorithm Bound\_Assert() with modifications.

```
Bound_Assert()
                                                           /* input: FG_i and assert_node */
   current_list = the parent nodes of assert_node
   NextBranch = NULL
   Local_LCPs = NULL
   crnt_node = first entry in current_list
   Remove crnt_node from current_list
   receive_found = false
   do
      while ((receive_found=false) AND (crnt_node \neq root node of FG_i) AND
          (crnt_node \neq assert_node) AND (crnt_node has not been visited))
          if (current_list \neq NULL)
             Push current_list on the stack NextBranch
          endif
          Mark crnt_node as visited
          if crnt_node = receive
             Add crnt_node to Local_LCPs
             receive_found = true
          else
             current_list = parent nodes of crnt_node
             crnt_node = first entry in current_list
             Remove crnt_node from current list
          endif
      endwhile
      if (NextBranch \neq NULL)
          receive\_found = false
          current\_list = Pop(NextBranch)
          crnt_node = first entry in current_list
          Remove crnt_node from current_list
      endif
   while (NextBranch \neq NULL)
end algorithm
```

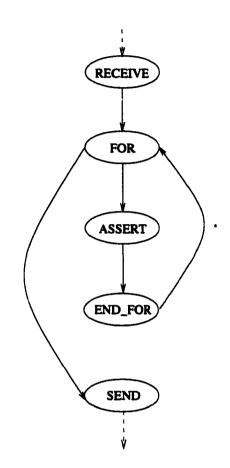


Figure 7.12: Assert in the loop body

Algorithm Bound\_Assert() constructs a linked list,  $Local_LCPs$ , that are the last LCP events of the assert. This list is used by algorithm Find\_LCPs() to determine the LCP and LCP' events of the POG. The search for LCP and LCP' requires Find\_LCPs() to visit the ancestors of each POG node represented by an LCP event in  $Local_LCPs$ . Changes are necessary to Find\_LCPs() to contend with back edges encountered during the search. Back edges in the POG define additional causal relationships as demonstrated by the portion of the POG shown in 7.15. Without considering the back edge, the causal relationships are

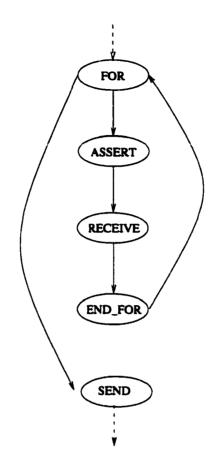


Figure 7.13: Assert and receive in the loop body

 $1: 0S1 \rightarrow 1: 1R0 \rightarrow 1: 2S0 \rightarrow 1: 0R2$ . The causal relationships  $1: 0R2 \rightarrow 1: 2S0 \rightarrow 1: 1R0 \rightarrow 1: 0S1$  exist with the back edge. When determining the *LCP* and *LCP'* events, all casual relationships, including those derived from back edges, must be considered.

A node with a back edge pointing to it has two parents. One parent is the result of a forward edge, and the other parent is the result of a back edge. In the original version of **Find\_LCPs()**, only parent nodes which result from forward edges are searched. To consider all the causal relationships in the POG, paths that include parent nodes that are the result of back edges are also searched.

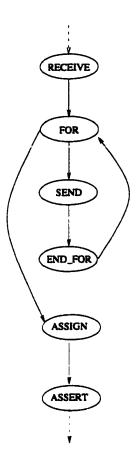


Figure 7.14: Assert not in the loop body

In the POG shown in figure 7.15, the assert occurs in  $P_1$ , and the receive of node *last* is the last LCP event of  $P_1$ . The search for LCP and LCP' events starts at node *last*. The send of node n, 1:0S1, is found to be an LCP' event. Node n has two parents, one resulting from a forward edge and one resulting from a back edge. At this point the search branches into two paths. The path that includes the parent of node n resulting from a forward edge is searched by the original Find\_LCPs(). The path that includes node n' and node n'' should also be searched by Find\_LCPs() since these nodes are ancestors of node n. The receive of node n'' is an LCP event and the send of node n' is an LCP' event.

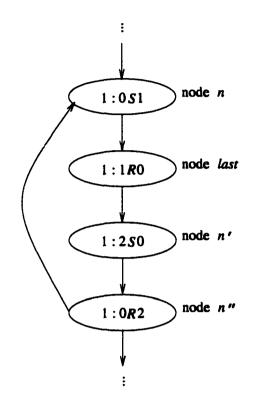


Figure 7.15: POG with a back edge

Notice in the POG of figure 7.15 that when the path follows the back edge parent of node *n*. the path *last*. *n*. *n''*. *n'* can repeat indefinitely. When a back edge is encountered, the back edge must be followed to consider all causal relationships. By following the back edge once, all additional causal relationships defined by this back edge are considered. Additional variables are required in algorithm Find\_LCPs() to follow paths that include parent nodes resulting from back edges and to not visit a parent that is the result of a back edge more than once in the same search path. A node is placed in the set *VisitOnce*if the node is a parent node resulting from a back edge, and the node is visited by the current search. Since the search can branch into two different paths, the state of the search prior to the branch is saved. The branch resulting from a forward edge is visited first. When the search of this branch has been completed, the other branch is searched by restoring the saved state and continuing the search at the branch point. An entry in the queue StateQ is the state of a search. The format of an entry in StateQ is  $<POGNode. RwoSQ, SendQ, RecvQ, FoundProcs, Sends, Rec_wo_Sends, VisitOnce>$ . The variable POGNode is the parent node resulting from the back edge. The remaining items are the values of variables before the branch. Algorithm Find\_LCPs() is repeated with the appropriate modifications.

Find\_LCPs()

/\* Input: Local\_LCPs Output: SendQ, RecvQ \*/

```
StateQ = NULL
for each entry in Local_LCPs where the event entry is c: iRj
   for each POG node that contains c: iRi
       Lastnode = POG node that contains c: iRj
       POGnode = Startnode
       FoundProcs = Sends = VisitOnce = \emptyset
       Rec_wo_Sends = \{i\}
       RwoSQ = NULL
       Insert \langle c, i, j, POGnode \rangle in RwoSQ
       POGnode = ParentOf(POGnode)
       while (POGnode \neq root node) AND (FoundProcs \neq ({ 0, ..., N-1 } - i))
          while (POGnode \neq root node) AND (FoundProcs \neq ({ 0, ..., N-1 } - i))
              for each receive, c: jRk, in POGnode
                 if ((j \in Sends) \text{ OR } (j = i)) \text{ AND } (k \notin FoundProcs)
                    Insert \langle c, j, k, POGnode \rangle in RwoSQ
                     Rec_wo_Sends = Rec_wo_Sends + j
                 endif
              endfor
              for each send, c: jSk, in POGnode
                 if (k \in \text{Rec.wo.Sends}) AND
                    ((Recv_POGnode = SearchQ(c, k, j)) \neq NULL)
                    if (RwoSQ does not have an entry with k as the receiver)
                        Rec_wo_Sends = Rec_wo_Sends - k
                     endif
                     Sends = Sends + j
                     FoundProcs = FoundProcs + j
                     Insert <c, j, POGnode> in SendQ
```

```
Insert \langle c, k, Recv_POGnode \rangle in RecvQ
               end if
            end for
            POGnode = ParentOf(POGnode)
         end while
         if (State Q \neq NULL)
            item = behead(StateQ)
            POGnode = item. POGnode
            RwoSO = item.RwoSO
            SendQ = item.SendQ
            RecvQ = item.RecvQ
            FoundProcs = item.FoundProcs
            Sends = item.Sends
            Rec_wo_Sends = item.Rec_wo_Sends
             VisitOnce = item. VisitOnce
         end if
      end while
   end for
end for
end algorithm
```

```
ParentOf (POGnode)

<u>if</u> (POGnode.Parent[1] ≠ NULL) /* if POGnode has two parents */

AND (POGnode.Parent[1] not in VisitOnce)

Add entry

<POGnode.Parent[1]. RwoSQ, SendQ, RecvQ, FoundProcs.

Sends, Rec_wo_Sends, VisitOnce>

to StateQ

<u>end if</u>

return(POGnode.Parent[0])

<u>end function</u>
```

The changes to algorithm Find\_LCPs() to facilitate searching paths including back edges for LCP and LCP' events do not affect lemmas 6.4 and 6.5 and properties 6.14 and 6.15. The entries in *SendQ* are the LCP events, and the entries in *RecvQ* are the LCP' events. No alterations to the method of adding entries into these queues results from the changes

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to Find\_LCPs(). We conclude that our technique for identifying LCP and LCP' events remains valid.

The next chapter analyzes the distributed programs of chapter 2. The resulting POG is shown for each program, and the LCP and LCP' are determined from the POG.

# Chapter 8

# Static Analysis of Distributed Programs

We presented five distributed programs in Chapter 2. In this chapter, we apply the algorithms of chapters 6 and 7 to determine the LCP and LCP' events for each distributed program.

## 8.1 Set Partition

SETPART, the set partition program, is reproduced from section 2.1 with the addition of an assert statement  $A_1$  in process  $P_1$ .

| P <sub>2</sub> |   | • |
|----------------|---|---|
| т 0            | ٠ | • |

1  $m\mathbf{x} = \max(S)$ 2  $async_send(1, mx)$  $S = S - \{mx\}$ 3 4  $async_recv(1, x)$ 5  $S = S \cup \{\mathbf{x}\}$ 6  $\mathrm{mx} = \mathrm{max}(S)$ 7 while (mx > x)8  $async_send(1, mx)$ 9  $S = S - \{ \mathrm{mx} \}$ 10  $async_recv(1, x)$ 11  $S = S \cup \{\mathbf{x}\}$ 12 mx = max(S)13 endwhile

P<sub>1</sub>:: 14 while(true) 15  $async_recv(0, y)$ 16  $T = T \cup \{\mathbf{y}\}$ 17 mn = min(T) $A_1$  $assert(y = max(S) \ge mn > x \land$  $|S| = |S_0| \land S \cap T = y$ 18  $async_send(0, mn)$ 19  $T = T - \{\mathrm{mn}\}$ 20 endwhile

An assert statement in either process is adequate for expressing expected system execution behavior. Placing the causal assert statement  $A_1$  between lines 17 and 18 is useful for detecting incorrect execution and for locating errors in both  $P_0$  and  $P_1$ . Assert statement  $A_1$  is evaluated on each exchange.

A false evaluation of  $A_1$  indicates erroneous execution of the program. SETPART's error is identified by the assert's falsifying clause. If y is not equal to  $\max(S)$ ;  $P_0$  did not send the correct value. If  $\max(S) \not\geq mn$ ; processing should have stopped on the last exchange, and a likely error is  $P_0$ 's exchange loop condition. If  $mn \neq x$ ; either a value other than the minimum of T was chosen, or  $P_0$  has erroneously altered the variable x since the last exchange. If the new size of S has changed,  $P_0$  has not correctly added or removed a value from S since the last exchange. If the intersection of S and T is not equal to y; either S or T has not been correctly updated since the last exchange, and the results of the other clauses help in identifying the incorrect set.

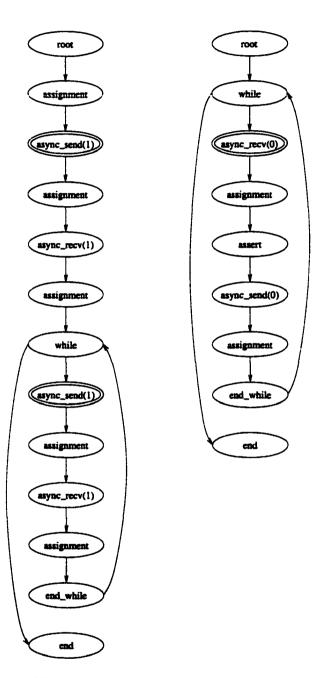


Figure 8.1: Flow Graphs for Set Partition

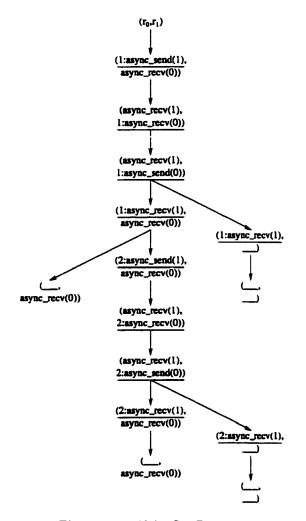


Figure 8.2: H for Set Partition

Suppose the programmer mistypes line 8 by sending x instead of mx to  $P_1$ . This mistake is detected by clause  $y = \max(S)$  of  $A_1$ . The negative evaluation of this clause identifies an erroneous value sent by  $P_0$ . Alternatively, suppose  $P_0$ 's condition to initiate another exchange is incorrectly  $a \ge$  instead of a >, then line 7 is

7 while  $(mx \ge x)$ .

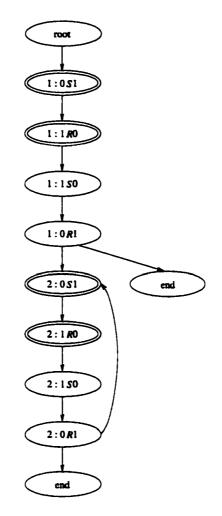


Figure 8.3: POG for Set Partition

This error prevents  $P_0$  from detecting the sets are partitioned, and causes SETPART to enter an infinite loop. The clause mn > x of  $A_1$  detects this error the first time an invalid exchange is attempted by  $P_0$  and eliminates the infinite loop problem.

Static analysis is performed by the algorithms of chapter 7 since loops are present in the program. First, algorithm  $Create_FG_i()$  constructs the control flow graphs. The resulting flow graphs are shown in figure 8.1.

Graph H is constructed by algorithm Crt\_H() from the flow graphs. The resulting graph H is shown in figure 8.2. The back edge represents the continuous exchange of data between the two processes until the set is partitioned. The *POG* is constructed from Hand is shown in figure 8.3.

Algorithm Bound\_Assert() determines the last LCP' event of the assert statement in  $P_1$ . Node async\_recv(0) of  $FG_1$  is returned by Bound\_Assert(). This node is shown in figure 8.1 with double circles. The event async\_recv(0) of  $P_1$  is represented by two POG nodes. One node has the entry 1:1R0, and the other node has the entry 2:1R0.

Starting with node 1:1R0 of the POG, we identify the LCP and LCP' events. The LCP' event is 1:1R0, and the LCP event is 1:0S1. For node 2:1R0, the LCP' event is 2:1R0, and the LCP event is 2:0S1. The nodes with double circles in figure 8.3 represent the LCP and LCP' events. Since the assert is in  $P_1$ , it is not necessary for  $P_1$  to propagate state information to  $P_0$ . Our static analysis allows us to not piggyback messages from  $P_0$  to  $P_1$ .

#### 8.2 Mutual Exclusion

Assume a three process distributed system implements mutual exclusion by embedding the circulating token protocol in its distributed application. Additional assumptions are that process  $P_0$  starts the token circulating, process  $P_1$  evaluates the the assert statement  $A_1$ , and each process  $P_i$  initializes variable  $in\_cs_i$  to false. Assertion  $A_1$  detects mutual exclusion violation. The distributed application may incorporate message passing, but we only analyze the mutual exclusion code. The messages of the application will not affect our analysis. Below is the portion of the code we analyze.

#### MUTEX

•

| MUU I            | EA.   |
|------------------|---|
| $P_0$ ::         |   |
| 1                | do  |
| 2                | async_send(1, token)  |
| 3                | async_recv(2, token, <i>waitsecs</i> )  |
| 4                | if message received   |
| 5                | if want_cs <sub>0</sub>   |
| 6                | $in_cs_0$ = true; $critsec_0$ ; $want_cs_0$ = false   |
| 7                | endif   |
| 8                | async_send(1, token)  |
| 9                | else /* async_recv timed out */   |
| 10               | do_other  |
| 11               | endif   |
| 12               | enddo   |
| . –              |   |
| $P_1::$          |   |
| 13               | do  |
| 14               | async_recv(0, token, <i>waitsecs</i> )  |
| 15               | if message received   |
| $A_1$            | <b>assert</b> $(in_cs_0 = t \land in_cs_1 = t \Rightarrow in_cs_0 \rightarrow in_cs_1 \lor in_cs_1 \rightarrow in_cs_0$ and |
| 1                | $in\_cs_1 = t \land in\_cs_2 = t \Rightarrow in\_cs_1 \rightarrow in\_cs_2 \lor in\_cs_1$ and                               |
|                  | $in\_cs_0 = t \land in\_cs_2 = t \Rightarrow in\_cs_0 \land in\_cs_2 \lor in\_cs_0)$  |
| 16               | if $want_{cs_1}$  |
| 17               | $in_{cs_1}$ =true; $critsec_1$ ; $want_{cs_1}$ =false   |
| 18               | endif   |
| 19               | async_send(2, token)  |
| 20               | else /* async_recv timed out */   |
| 21               | do_other <sub>1</sub>   |
| 22               | endif   |
| 23               | enddo   |
| 20               |   |
| $P_2::$          |   |
| 24               | do  |
| 25               | async_recv(1, token, <i>waitsecs</i> )  |
| 26               | if message received   |
| 20               | if want_cs <sub>2</sub>   |
| 28               | $in_{cs_2}$ =true; critsec <sub>2</sub> ; want_cs <sub>2</sub> =false   |
| 28<br>29         | endif   |
| 29<br>30         | async_send(0, token)  |
| 30<br>31         | else /* async_recv timed out */   |
| 31<br>32         | do_other <sub>2</sub>   |
| 32<br>33         | endif   |
| зз<br>34         | endido  |
| J <del>.</del> 7 | CHURA   |

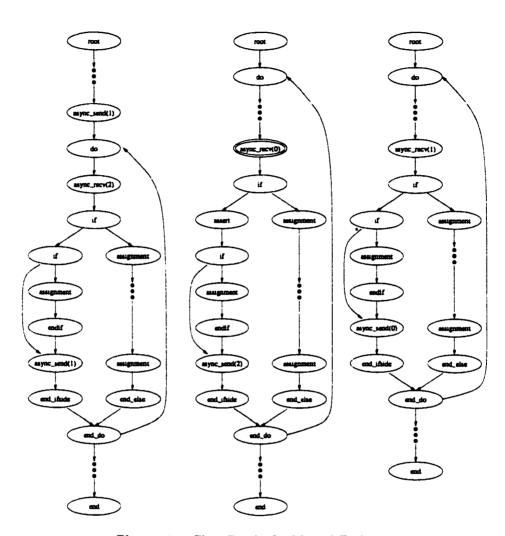


Figure 8.4: Flow Graphs for Mutual Exclusion

Assume line 26 of  $P_2$  is erroneously omitted, and then suppose the following occurs. Process  $P_0$  passes the token to  $P_1$ , and  $P_1$  enters its critical section. Process  $P_2$  wants to enter its critical section and has set want\_cs<sub>2</sub> to true. While  $P_1$  is in its critical section, the async\_recv on line 25 times out. The condition of line 27 is true, and  $P_2$  incorrectly enters its critical section while  $P_1$  is in its critical section.

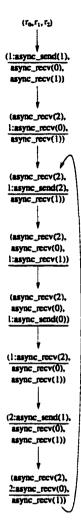


Figure 8.5: Graph H for Mutual Exclusion

This invalid critical section entry by  $P_2$  is detected by the assert statement  $A_1$  when the token circulates around to  $P_1$ . The clause  $(in\_cs_1 = t \land in\_cs_2 = t \Rightarrow in\_cs_1 \rightarrow$  $in\_cs_2 \lor in\_cs_2 \rightarrow in\_cs_1)$  evaluates to false detecting that  $P_1$  and  $P_2$  entered their critical sections concurrently. The combination of  $in\_cs_i$  being true and the timestamp of when  $in\_cs_i$  was last modified conveys the last time  $P_i$  entered its critical section. With this information, the assert statement detects any of the processes violating mutual exclusion.

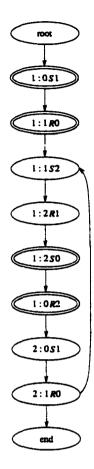


Figure 8.6: POG for Mutual Exclusion

The flow graphs for the circulating token protocol are shown in figure 8.4. The do\_other statements in the source code are represented as a series of assignment nodes in the flow graphs. The H graph generated is shown in figure 8.5, and the POG is shown in figure 8.6.

Algorithm Bound\_Assert() determines the last LCP' event of the assert statement in  $P_1$ , node async\_recv(0) of  $FG_1$ . This node is shown in figure 8.4 with double circles. The event async\_recv(0) of  $P_1$  is represented by two POG nodes. One node has the entry 1:1R0, and the other node has the entry 2:1R0. Starting with node 1:1R0 of the POG, we identify the LCP and LCP' events. The LCP' event is 1:1R0, and the LCP event is 1:0S1. For node 2:1R0, the LCP' events are 2:1R0, 1:0R2, and 1:2R1. The LCP events are 2:0S1, 1:2S0, and 1:1S2. The nodes with double circles in figure 8.6 represent the events that are the LCP and LCP' events. The messages that implement the circulating token are also the messages that piggyback state information for assert evaluation. The distributed program's application messages will not be tagged for piggybacking.

#### 8.3 Bubble Sort

We continue with the distributed bubble sort program from chapter 2 that consists of six processes. The time space diagram for the bubble sort's execution is repeated in figure 8.7. The hashes on  $P_2$ 's time line represent assertion evaluation. Two asserts in one of the six processes provides a thorough erroneous execution detection method. The assert statements can be in any one of the six processes and provide the same meaningful information. We have arbitrarily selected  $P_2$ . Process  $P_2$ 's source code is shown below with the two assert statements  $A_{2a}$  and  $A_{2b}$ . The clause  $P_i.list \leq P_i.recv_list$  in the assert statements tests whether every element in  $P_i.list$  is less than or equal to all elements of  $P_i.recv_list$ . and the clause  $P_i.list \geq P_i.recv_list$  in the assert statements tests whether every element in  $P_i.list$ is greater than or equal to all elements  $P_i.recv_list$ .

#### P<sub>2</sub>::

integer pid, phase; arrays list, recv\_list pid = 21 2 read q/6 elements into list 3 sort list 4 for phase = 0 to 5 5 if phase is even 7 async\_send(3, list) 8 async\_recv(3. recv\_list) 9  $list = merge\_sort(list, recv\_list, first)$  $A_{2a}$ **assert**( $P_2.list \leq P_2.recv\_list \land P_2.recv\_list = P_3.list \land$  $P_3.list \leq P_3.recv\_list \land P_3.recv\_list = P_4.list \land$  $P_4.list \leq P_4.recv\_list \land P_4.recv\_list = P_5.list \land$  $P_5.list \geq P_5.recv\_list$ ) 10 endif 11 if phase is odd && pid != 0 && pid != N-112 async\_send(1, list) 13 async\_recv(1. recv\_list) 14  $list = merge\_sort(list, recv\_list, last)$ **assert**( $P_2.list \ge P_2.recv\_list \land P_2.recv\_list = P_1.list \land$ A26  $P_1.list \ge P_0.recv\_list \land P_1.recv\_list = P_0.list \land$  $P_0.list \leq P_0.recv\_list$ ) 15 endif 16 endfor

| merg | e_sort(list.recv_list, half)::                 |
|------|--|
|      | array <i>merge_list</i>                        |
| 1    | $merge\_list = merging of recv\_list and list$ |
| 2    | sort merge_list                                |
| 3    | if $half = first$                              |
| -4   | return first half of elements in merge_list    |
| 5    | else   |
| 6    | return last half of elements in merge_list     |
| 7    | endif  |

7 endif

The clause  $P_i.recv_list = P_{i+1}.list$ , for i = 2...4, of assert  $A_{2a}$  determines whether process  $P_i$  received the correct list from its right neighbor  $P_{i+1}$ . The clause  $P_i.recv_list = P_{i-1}.list$ , for i = 1...2, of assert  $A_{2b}$  determines whether process  $P_i$  received the correct

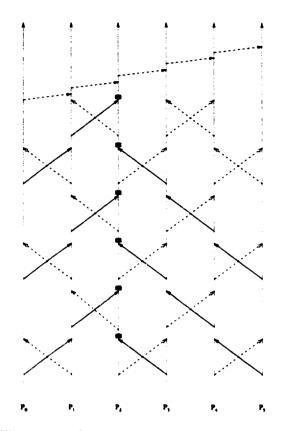
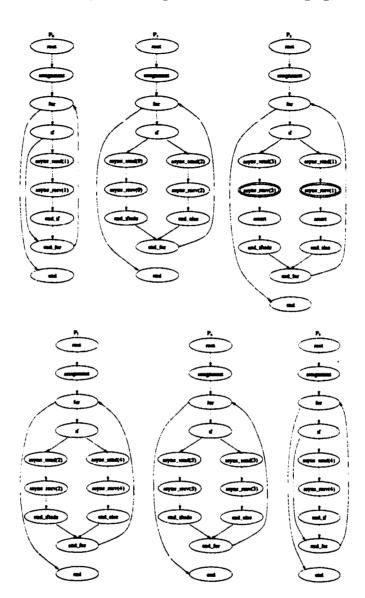


Figure 8.7: Time space diagram for Bubble Sort

list from its left neighbor  $P_{i-1}$ . The clauses  $P_i.list \leq P_i.recv \ list$  and  $P_i.list \geq P_i.recv \ list$ ensure that merge\_sort() correctly sorted and halved the merged list.

Assume line 9 of  $P_4$  is mistyped. The function merge\_sort() is passed *last* instead of *first*. Function merge\_sort() sorts and returns the last q/6 elements, and these elements are assigned to *list*. The correct execution should have assigned to *list* the first q/6 elements of the merged and sorted elements. In the next phase (odd), line 12 of  $P_4$  sends this incorrect *list* to  $P_3$ . Assume  $P_3$  is correct. In the following even phase when  $P_3$  sends its supposedly correct list to  $P_2$ , the clause  $P_4$ .*list*  $\leq P_4$ .*recv\_list* of assert  $A_{2a}$  evaluates to false detecting that  $P_4$  executed incorrectly. This false evaluation singles out the error to  $P_4$ 's execution



of merge\_sort() in an even phase. In general, errors in merging, sorting and halving

Figure 8.8: Flow Graphs for Bubble Sort

any of the process's list will be detected by the two assert statements. The comparisons  $P_2.list \leq P_2.recv\_list$ ,  $P_3.list \leq P_3.recv\_list$  and  $P_4.list \leq P_4.recv\_list$  of  $A_{2a}$  ensures the correct execution of  $P_2$  and its right neighbors. The comparisons  $P_2.list \geq P_2.recv\_list$  and  $P_1.list \geq P_0.recv\_list$  of  $A_{2b}$  ensures the correct execution of  $P_2$  and its left neighbors.

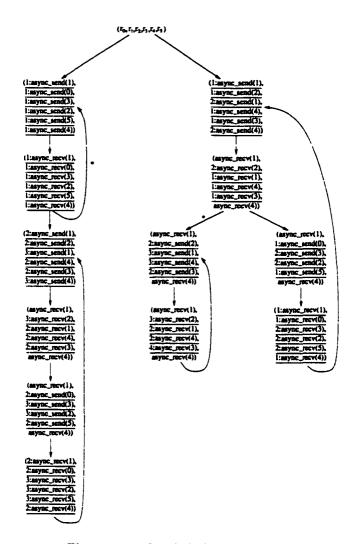


Figure 8.9: Graph H for Bubble Sort

In an even phase, process  $P_3$  should send list to  $P_2$ . But consider the case when  $P_3$  mistakenly sends recv\_list instead of list. Clause  $P_2.recv_list = P_3.list$  of  $A_{2a}$  evaluates to false and identifies  $P_2$  as sending the incorrect data. Assert  $A_{2a}$  ensures that  $P_2$ 's right neighbors have sent the correct data, and assert  $A_{2b}$  ensures that  $P_2$ 's left neighbors have sent the correct data.

The source code for the other five processes is not shown in this chapter, but the bubble sort algorithm in chapter 2 is sufficiently outlined for our static analysis. The flow graphs are shown in figure 8.8. The resulting H graph is shown in figure 8.9. Each process has an if/else branch in execution, and the combinations of different executions creates a large Hgraph. Only those branches that contribute to a path in the *POG* are shown in H. An edge with an asterisk denotes an incorrect decision made at the if/else branch of the processes. The resulting *POG* is shown in figure 8.10.

Since we have two assert statements in  $P_2$ . algorithm Bound\_Assert() is called twice to determine the last LCP' events. For assert  $A_{2a}$ , the last LCP' event is  $async_recv(3)$ of  $FG_2$ . The event  $async_recv(3)$  is represented by three POG nodes. The POG node entries that represent this receive are 1:2R3. 3:2R3. and 2:2R3. For assert  $A_{2b}$ , the last LCP' event is  $async_recv(1)$  of  $FG_2$ . The event  $async_recv(1)$  is also represented by three POG nodes. The POG node entries that represents this receive are 2:2R1. 1:2R1, and 2:2R1. All six POG node representatives of these last LCP' events are underlined in figure 8.10.

For each of the last LCP' events, the LCP and LCP' events are determined by algorithm Find\_LCPs(). The LCP and LCP' events are underlined in figure 8.11. The messages that piggyback state information are shown in the time space diagram of figure 8.7 as solid directional lines. The LCP and LCP' events for assert  $A_{2a}$  are identical to the LCP and LCP' events for assert  $A_{2b}$ . In this example, the additional assert statement did not increase the number of messages piggybacking state information.

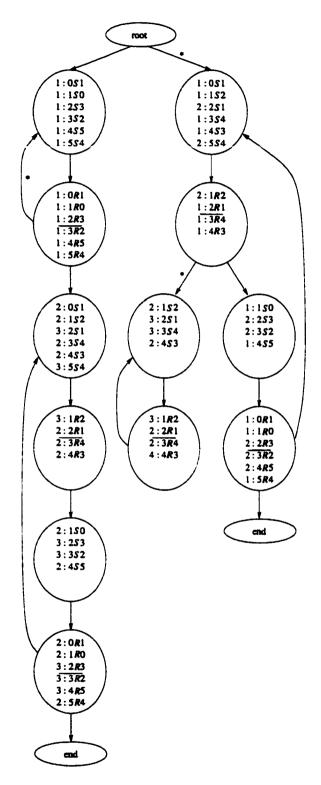


Figure 8.10: POG for Bubble Sort

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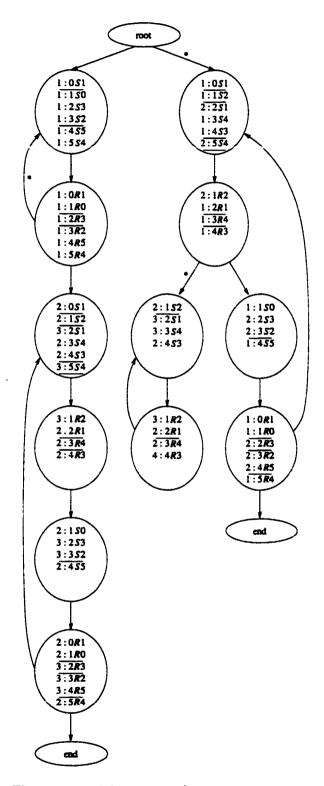


Figure 8.11: LCP and LCP' events for Bubble Sort

#### 8.4 Tree Sort

Referring back to figure 2.5, we see that the distributed tree sort program of chapter 2 consists of 15 processes. We have selected  $P_1$  to evaluate assert statement  $A_1$ . This assertion ensures that processes  $P_1, P_3, P_4, P_7, P_8, P_9$  and  $P_{10}$  have correctly split, merged, and sorted the list  $P_0$  sent to  $P_1$ . Since the left side and the right side of the tree are symmetric, a similar assert statement would be placed in  $P_2$  to ensure processes  $P_2, P_5, P_6, P_{11}, P_{12}, P_{13}$  and  $P_{14}$  correctly split, merge, and sort the list  $P_0$  sent to  $P_2$ .

```
P_1:: (parent node)
          integer child<sub>1</sub>, child<sub>2</sub>, parent
          arrays list. list<sub>1</sub>. list<sub>2</sub>
          async_recv(0, list);
    1
   2
          split list into two halves: list_1. list_2
   3
          async_send(3, list_1)
    4
          async_send(4, list_2)
   5
          async_recv(3, list_1)
   6
          async_recv(4, list_2)
    A_1: assert(P_7.list is sorted \land P_8.list is sorted \land P_9.list is sorted \land
                     P_{10}.list is sorted \wedge P_3.list is sorted \wedge P_4.list is sorted \wedge
                     ((P_7.list \cup P_8.list \cup P_9.list \cup P_{10}.list) = P_1.list) \land
                     (P_7.list = P_3.list_1) \land (P_8.list = P_3.list_2) \land
                     ((P_3.list_1 \cup P_3.list_2) = P_3.list = P_1.list_1) \land
                     (P_9.list = P_4.list_1) \land (P_{10}.list = P_4.list_2) \land
                     (P_4.list_1 \cup P_4.list_2 = P_4.list = P_1.list_2) \land
          (P_1.list_1 \cup P_1.list_2 = P_1.list))
    7
          merge list_1 and list_2 into list
    8
          async_send(0, list)
```

In the correct implementation of tree sort,  $P_3$  receives a list from  $P_1$ , and then  $P_3$  is responsible for sorting this list and sending the sorted list to  $P_1$ . Assume  $P_3$  erroneously sends the wrong list to  $P_1$ . Following is the incorrect implementation of  $P_3$ :

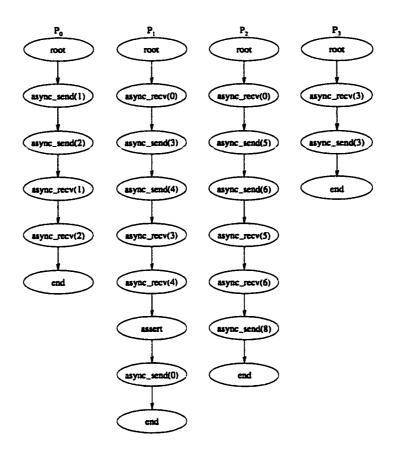
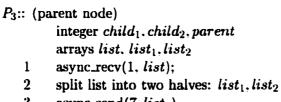


Figure 8.12: Flow Graphs for Tree Sort



- 3  $async_send(7, list_1)$
- 4  $async_send(8, list_2)$
- 5  $async_recv(7, list_1)$
- 6  $async_recv(8, list_2)$
- 7 merge  $list_1$  and  $list_2$  into list
- 8  $async_send(1, list_1)$

Line 8 is incorrect,  $P_3$  should send list to  $P_1$ . Assert  $A_1$  detects the error by two clauses evaluating to false. These clauses are  $(P_3.list_1 \cup P_3.list_2 = P_3.list = P_1.list_1)$  and  $(P_1.list_1 \cup P_1.list_2 = P_1.list)$ . The combination of these clauses identifies that  $P_1.list_1$  is incorrect. Since none of the other clauses involving  $P_3.list_1$  and  $P_3.list_2$  evaluated to false, the false evaluation of  $(P_3.list_1 \cup P_3.list_2 = P_3.list = P_1.list_1)$  conveys that  $P_1.list_1$  is not equal to  $P_3.list$ . With this information, the source of the error is easily found.

As another example of an incorrect implementation, suppose leaf process  $P_8$  does not correctly sort its list. This error causes clause ( $P_8.list$  is sorted) of  $A_1$  to evaluate to false. None of the other clauses evaluate to false, and the source of the error is directly identified.

The flow graphs for  $P_0$ ,  $P_1$ ,  $P_2$ , and  $P_7$  are shown in figure 8.12. The flow graphs for  $P_3$ ,  $P_4$ ,  $P_5$  and  $P_6$  are identical to  $P_2$ 's flow graph with the exception of the destination and source of messages. Also, the flow graphs for  $P_8$ ,  $P_9$ ,  $P_{10}$ ,  $P_{11}$ ,  $P_{12}$ ,  $P_{13}$ ,  $P_{14}$  are identical to  $P_7$ 's flow graph with the exception of the destination and source of the message. The destinations and originations of the messages for the communication events are given in chapter 2.

The H graph for the tree sort program is shown in 8.13. There exists only one execution path since none of the processes have a possible branch in execution. The resulting POGis shown in figure 8.14. Algorithm **Bound\_Assert()** returns the event **async\_recv(4)** of  $P_2$  as the last LCP' event. This event is identified in  $P_1$ 's flow graph with double circles. One POG node represents this receive event, and that node's entry is 3:1R4. This event, as well as the LCP and LCP' events determined by algorithm Find\_LCPs(), is underlined in figure 8.14. Figure 8.15 is the time space diagram of tree sort's execution with the six messages that piggyback state information shown as solid lines.

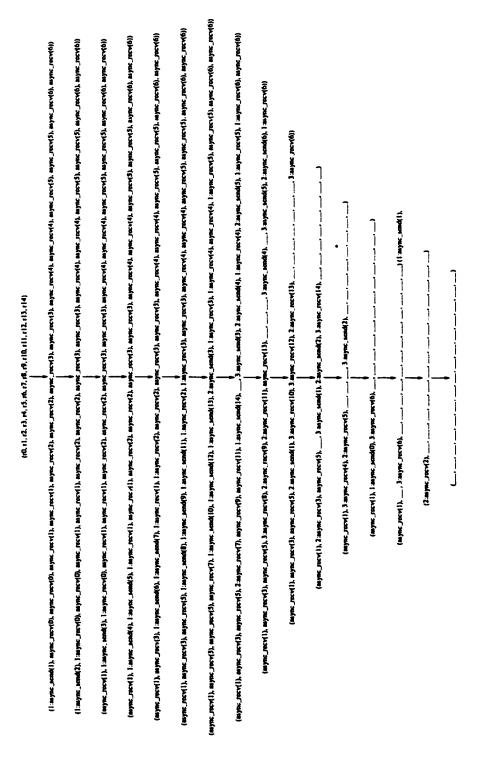


Figure 8.13: Graph H for Tree Sort

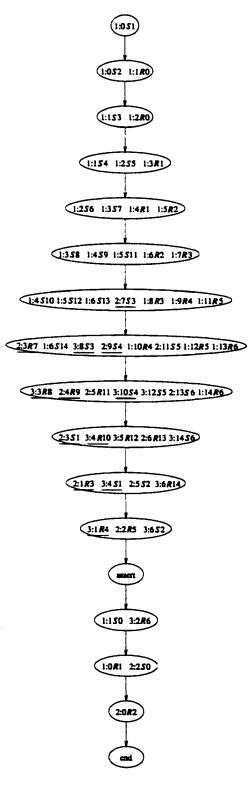


Figure 8.14: POG for Tree Sort

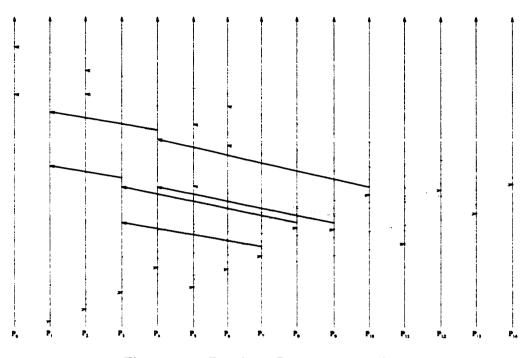


Figure 8.15: Time Space Diagram for Tree Sort

### 8.5 Positive Acknowledgement/Retransmission

The two process distributed program implementing positive acknowledgement and retransmission is repeated from chapter 2 with the addition of assert statement  $A_0$ . Process  $P_0$ sends a message to  $P_1$ , and  $P_1$  acknowledges receipt of that message. Process  $P_0$  retransmits the message until an acknowledgement for the message is received.

| $P_0$ :: |  |  |
|----------|--|--|
|          | <i>MsgBitSend</i> : bit                | /* alternating bit */                  |
|          | sbuffer: message                       | /* buffer for outgoing data message */ |
|          | event: (MsgArrival, CksumErr, TimeOut) | /* different interrupt events */       |
| 1        | MsgBitSend = 0                         | /* initialize alternating bit */       |
| 2        | FromHost(sbuffer)                      | /* get the data message from host */   |
| 3        | repeat                                 |  |

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| 4     | async_send(1,sbuffer, MsgBitS                   | end)  |
|-------|---|---|
| 5     | StartTimer;                                     | /* time to wait for acknowledgement */                    |
| 6     | wait(event)                                     | /* possibilities MsgArrival, CksumErr, TimeOut */         |
| 7     | if $event = MsgArrival$                         |   |
| 8     | $async_recv(1, ack)$                            | <pre>/* receive the acknowledgement */</pre>              |
| $A_0$ | $: \mathbf{assert}(P_1.IncomingBit = P_0.MsgBi$ | $tSend \land P_0.MsgBitSend \neq P_1.MsgBitReceive \land$ |
|       | $P_0.sbuffer = P_1.rbuffer \land P_1.event =$   | MsgArrival)   |
| 9     | FromHost( <i>sbuffer</i> )                      | /* an acknowledgment has arrived intact */                |
| 10    | inc( <i>MsgBitSend</i> )                        | /* increment by 1 then mod 2 */                           |
| 11    | endif   |   |
| 12    | until doomsday                                  |   |

 $P_1::$ 

| 4 1 |                                     |                                       |    |
|-----|-------------------------------------|---------------------------------------|----|
|     | MsgBitReceive : bit                 | /* alternating bit                    | */ |
|     | IncomingBit : bit                   | /* incoming message's bit             | */ |
|     | rbuffer: message                    | /* buffer for incoming data message   | */ |
|     | event: (MsgArrival. CksumErr)       | /* different interrupt events         |    |
| 13  | MsgBitReceive = 0                   | /* initialize alternating bit         | */ |
| 14  | repeat                              |                                       |    |
| 15  | wait( <i>event</i> )                | /* possibilities MsgArrival, CksumErr | */ |
| 16  | if $event = MsgArrival$             | /* a valid message has arrived        | */ |
| 17  | async_recv(0, rbuffer, IncomingBit) | /* accept the message                 | */ |
| 18  | if IncomingBit = MsgBitReceive      |                                       |    |
| 19  | ToHost( <i>rbuffer</i> )            | /* pass the data to the host          | */ |
| 20  | inc( <i>MsgBitReceive</i> )         | /* increment by 1 then mod 2          | */ |
| 21  | endif                               |                                       |    |
| 22  | async_send(0, acknowledgement)      |                                       |    |
| 23  | endif                               |                                       |    |
| 24  | until doomsday                      |                                       |    |
|     |                                     |                                       |    |

Assert  $A_0$  first determines if *IncomingBit* was correctly received at  $P_1$  and was not erroneously changed by  $P_1$ . The second clause of the assert,  $P_0.MsgBitSend \neq P_1.MsgBitReceive$ , ensures that MsgBitSend and MsgBitRecv are correctly updated. The third clause,  $P_0.sbuffer$  $= P_1.rbuffer$ , determines whether  $P_1$  received the correct message, and the last clause,  $P_1.event = MsgArrival$ , ensures that  $P_1$  sent the acknowledgement only after it received a message from  $P_0$ .

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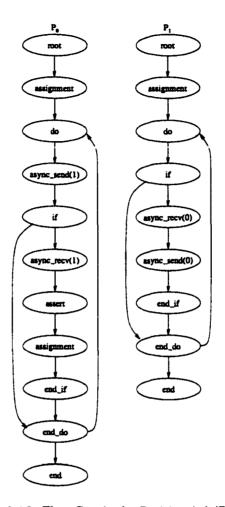


Figure 8.16: Flow Graphs for Positive Ack/Retrans

In the correct implementation of this distributed program, process  $P_1$  increments *Ms-gBitReceive* when a new message is received. Suppose  $P_1$  increments *MsgBitReceive* when it receives any valid message. This error occurs if either line 18 is omitted or if line 20 is placed after line 21.

Assume line 18 is omitted. Suppose the following events occur.  $P_0$  sends a message to  $P_1$ .  $P_1$  receives the message and correctly passes the message to the host and increments *MsgBitReceive*. Process  $P_1$  then sends an acknowledgement, but the acknowledgement is

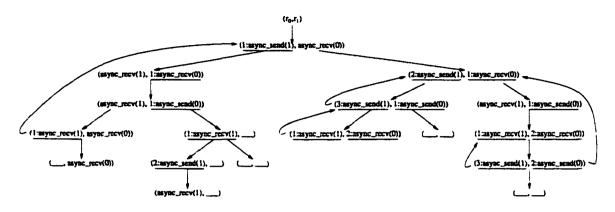


Figure 8.17: Graph H for Positive Ack/Retrans

lost. Process  $P_0$  times out and retransmits the same messages. Process  $P_1$  receives a duplicate message. Since line 18 is missing,  $P_1$  erroneously passes the message to the host and increments MsgBitReceive. Process  $P_1$  then sends an acknowledgement to  $P_0$ , and the acknowledgement is received by  $P_0$ . The assert statement is evaluated. The second clause of  $A_0$ .  $P_0.MsgBitSend \neq P_1.MsgBitReceive$ , evaluates to false and identifies the error.

As another example of an incorrect implementation, assume  $P_1$  sends an acknowledgement for any event. This error occurs if line 22 is placed after line 23. Suppose the following events occur. Process  $P_0$  sends a message to  $P_1$ . The message is corrupted in transit. Process  $P_1$  is interrupted and procedure wait returns a CKsumErr event. Line 16 evaluates to false, but then  $P_1$  incorrectly sends an acknowledgement to  $P_0$ . Process  $P_0$  receives the acknowledgement. The assert statement is then evaluated, and clause  $P_1$ .event = MsgArrival evaluates to false. This clause identifies that  $P_1$  sent an invalid acknowledgement.

The flow graphs are shown in figure 8.16, and graph H in shown in figure 8.17. Although the two processes' source code is short, the execution behavior of the distributed program

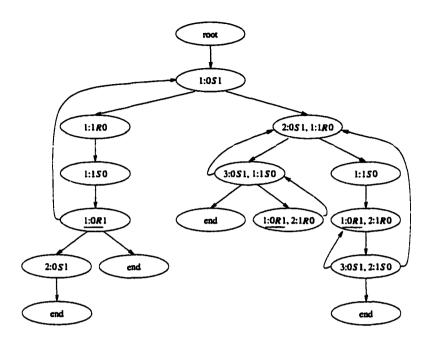


Figure 8.18: POG for Positive Ack/Retrans

is complex. The main reason for this is the  $async_recv(1, ack)$  of line 8. Process  $P_1$  will continue execution regardless of whether  $P_0$  receives  $P_1$ 's acknowledgement. The result, as shown in figure 8.17. is multiple branches of execution. The resulting *POG* is shown in figure 8.18.

The assert statement is evaluated when the if condition of  $P_0$  evaluates to true. Algorithm Bound\_Assert() identifies statement  $async\_recv(1)$  of  $P_0$  as the last LCP' event. This event is represented by three POG nodes which are underlined in figure 8.18. Only the messages sent from  $P_0$  to  $P_1$  need to piggyback state information. Algorithm Find\_LCPs() identifies the POG node entries that represent the send event of  $P_1$  as the LCP event. Both LCP and LCP' events are underlined in the POG of figure 8.19.

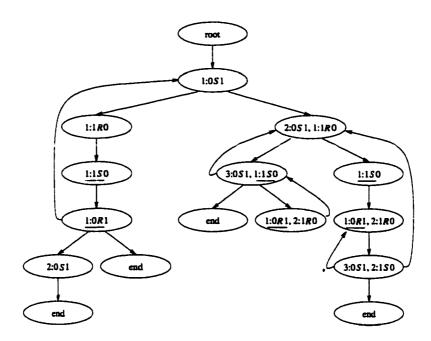


Figure 8.19: LCP and LCP' events for Positive Ack/Retrans

The five examples analyzed in this chapter are diverse in their communication behavior. Together they demonstrate the robustness of our static analysis technique. For each example, the analysis identifies the latest causally preceding communication events. The assert is evaluated with the causal global state obtained by piggybacking state information on the messages of the LCP and LCP' events.

#### 8.6 Prototype

A prototype system has been written to demonstrate the feasibility of analyzing distributed programs for evaluating distributed asserts. Our prototype is a two-pass compiler. The grammar for our compiler is shown in appendix A. The C source files for the distributed processes are the input of the compiler. For assert statement evaluation, code is added to the processes' source files to create and maintain a causal global state, and the *LCP* messages are identified and altered to piggyback this causal global state. The remainder of the distributed program is not altered.

We will use the distributed program SETPART as our running example in the following explanation of our system. The source code for SETPART appears below.

 $P_0$ :

```
#include <stdio.h>
#include <async.h>
#include <sys/time.h>
int S[16];
int x;
main(argc,argv)
     int argc;
     char *argv[];
{
  int count;
  int numcount;
 int len;
  int i;
  int mx;
  if (argc < 2)
     {
      fprintf ( stderr, "USAGE: %s <st size>\n", argv[0]);
       exit(1);
     }
  init_async (121, 0, 2, 0, 0.0, 0, 0);
  count = atoi(argv[1]);
  Init_List ( S, &numcount, count, 0);
 printf("Initial set in PO\n\t");
  for ( i=0; i<numcount; i++ )</pre>
       printf("%6d ", S[i]);
 printf("\n\n");
 mx = max(S);
 x = -999999;
 while (mx > x)
```

1**9**8

```
£
       async_send ( 1, &mx, sizeof(mx) );
       Remove ( S, &numcount, mx );
       len = sizeof(int);
       async_recv ( 1, &x, &len, 60 );
       Add (S, &numcount, x);
       mx = max(S);
      }
  printf("Final set in PO\n\t");
  for ( i=0; i< numcount; i++ )</pre>
       printf("%6d ", S[i]);
  printf("\n\n");
  close_async();
7
P_1
#include <stdio.h>
#include <async.h>
#include <sys/time.h>
int mn:
int T[16];
int y;
main(argc,argv)
      int argc;
      char *argv[];
{
   int count;
   int numcount;
   int len;
   int i;
   int devdata;
   devdata = 1;
   if (argc < 2)
      {
       fprintf ( stderr, "USAGE: %s <set size>\n", argv[0]);
        exit(1);
      ŀ
   init_async ( 121, 1, 2, 0, 0.0, 0, 0 );
   count = atoi(argv[1]);
   numcount = Init_List ( T, &numcount, count, 1);
   printf("Initial set in P1\n\t");
   for ( i=0; i<numcount; i++ )</pre>
       printf("%6d ", T[i]);
   printf("\n\n");
```

```
while (devdata > 0)
     £
       len = sizeof(int);
       devdata = async_recv ( 0, ky, &len, 60 );
       if (devdata > 0)
     £
       Add ( T, &numcount, y );
       mn = min(T);
       assert((max(CG._PO_S.S) == y) &&
        (max(CG._PO_S.S) >= mn) &&
                    (mn > CG._PO_x.x)
                                             ŁŁ
                    (intersect(CG._PO_S.S, T) == y) );
       async_send ( 0, &mn, sizeof(mn) );
       Remove ( T, &numcount, mn );
     }
     }
 printf("Final set in P1\n\t");
 for ( i=0; i<numcount; i++ )</pre>
       printf("%6d ", T[i]);
 printf("\n\n");
 close_async();
}
```

The first pass of our compiler consists of four phases. The initial phase parses the source code in each of the process input files and creates a control flow graph for each process as described in chapter 7. A declaration table. VarMap. is created. Each variable in a process has an entry in the table consisting of variable type, identifier and amount of memory required.

When an assert statement is detected by the parser, an entry containing only the variable identifier is added to the list **assert\_vars** for each non-local variable that occurs in the assert. Since processes can have identical variable identifiers, a notation has been developed to distinguish the process in which a variable resides. Non-local variables of the assert must be specified in the following format:

CG. Pi\_id.id

The process number is indicated by i, and the ids indicate the variable identifier. For example, set partition's assert is

```
assert((max(CG._PO_S.S) == y) &&
(max(CG._PO_S.S) >= mn) &&
(mn > CG._PO_x.x) &&
(intersect(CG._PO_S.S, T) == y) );
```

The list assert\_vars will have two entries, CG.\_PO\_S.S and CG.\_PO\_x.x, after parsing this assert.

The second phase creates three files for each process: asserti.h. pigRecvi.c., and pigSendi.c where *i* is the process number. Each asserti.h file defines a data structure for the causal global state and will be included in  $P_i$ . A structure exists in the included file for each entry of  $assert_vars$ . The type and size of each item of  $assert_vars$  are found in the table VarMap. The singular difference between asserti.h and assertj.h is the initialization of vector time. The files assert0.h and assert1.h created for SETPART are shown below.

```
assert0.h:
#define MAXPS 2
struct
 {
   struct
   Ł
     int S[16];
     int vtime;
   } _PO_S;
   struct
   Ł
     int x;
     int vtime;
   } _PO_x;
 } CG, tmpCG;
 int _vector_t[MAXPS] = {1, 0 };
```

```
assert1.h:
 #define MAXPS 2
 struct
 £
   struct
   £
     int S[16];
     int vtime;
   } _PO_S;
   struct
   Ł
     int x;
     int vtime;
   } _PO_x;
 } CG, tmpCG;
 int _vector_t[MAXPS] = {0,1 };
```

The symbol MAXPS indicates the number of processes in the distributed program. As shown in procedure Update() of chapter 4. the integer vtime is used for updating the causal global state. The variable CG is the causal global state. and the variable tmpCG is for temporarily holding a received causal global state. Vector time is maintained in the array \_vector\_t[].

The file **pigSend***i*.c is included by process  $P_i$ . This file contains the source code for function **Piggy\_Send()** which piggybacks the causal global state onto an outgoing message. This function is also responsible for updating the causal global state prior to piggybacking state information. The **Piggy\_Send()** functions differ for each process. **Piggy\_Send()** for process  $P_i$  is only responsible for updating CG with the variables that reside locally in  $P_i$ . The files **pigSend0.c** and **pigSend1.c** for SETPART are shown below.

PigSend0.c

#include <stdio.h>
#include <async.h>
Piggy\_send(i, data, sizedata)

```
int i:
   char *data:
   int sizedata;
£
   char *dataptr;
   dataptr=(char *)malloc(sizeof(CG)+sizedata);
   memcpy(dataptr, data, sizedata);
  memcpy(CG._P0_S.S, S, (sizeof(int) * 16));
   CG._PO_S.vtime = _vector_t[0];
   CG._PO_x.x = x;
   CG._PO_x.vtime = _vector_t[0];
  memcpy((dataptr+sizedata), &CG, sizeof(CG));
  return(async_send(i, dataptr, sizeof(CG)+sizedata));
}
PigSend1.c
 #include <stdio.h>
 #include <async.h>
Piggy_send(i, data, sizedata)
   int i;
   char *data;
   int sizedata;
 £
   char *dataptr;
   dataptr=(char *)malloc(sizeof(CG)+sizedata);
   memcpy(dataptr, data, sizedata);
   memcpy((dataptr+sizedata), &CG, sizeof(CG));
   return(async_send(i, dataptr, sizeof(CG)+sizedata));
 }
```

The file pigRecvi.c is included by process  $P_i$ . This file contains the source code for function Piggy\_Recv() which receives an incoming message that has been piggybacked with a causal global state. The newly received causal global state is copied into the variable tmpCG. The Piggy\_recv() of  $P_i$  updates  $P_i$ 's causal global state with the latest state information by comparing the vtime of corresponding entries in CG and tmpCG. The entry with the largest vtime has the latest state information. This is consistent with the causal state propagation protocol described in chapter 4. Piggy\_recv() of  $P_i$  only updates the components of the causal global state that do not correspond to it's own variables. The files pigRecv0.c and

pigRecv1.c for SETPART are shown below.

```
pigRecv0.c:
 #include <stdio.h>
 #include <async.h>
 Piggy_recv(i, data, sizedata, time)
   int i;
   char *data;
   int *sizedata;
   int time;
 {
   char *dataptr;
   int CGsize;
   CGsize = sizeof(CG) + *sizedata;
   dataptr=(char *)malloc(CGsize);
   if (async_recv(i, dataptr, &CGsize, time) < 0)
     return(-1);
   *sizedata = CGsize - sizeof(CG);
   memcpy(data, dataptr, *sizedata);
   memcpy(&tmpCG, (dataptr + *sizedata), sizeof(CG));
   return(#sizedata);
 }
pigRecv1.c:
 #include <stdio.h>
 #include <async.h>
 Piggy_recv(i, data, sizedata, time)
   int i;
   char *data;
   int *sizedata;
   int time;
 £
   char *dataptr;
   int CGsize;
   CGsize = sizeof(CG) + *sizedata;
   dataptr=(char *)malloc(CGsize);
   if (async_recv(i, dataptr, &CGsize, time) < 0)</pre>
     return(-1);
   *sizedata = CGsize - sizeof(CG);
   memcpy(data, dataptr, *sizedata);
   memcpy(&tmpCG, (dataptr + *sizedata), sizeof(CG));
```

```
if (CG._PO_S.vtime < tmpCG._PO_S.vtime)
{ memcpy(CG._PO_S.S, tmpCG._PO_S.S, (sizeof(int) * 16));
    CG._PO_S.vtime = tmpCG._PO_S.vtime;
}
if (CG._PO_x.vtime < tmpCG._PO_x.vtime)
{ memcpy(&CG._PO_x.x, &tmpCG._PO_x.x, sizeof(CG._PO_x.x));
    CG._PO_x.vtime = tmpCG._PO_x.vtime;
}
return(*sizedata);
}</pre>
```

The third phase determines the LCP and LCP' events. The H graph and the POG are constructed according to the algorithms  $Crt_H$  and  $Crt_POG$  given in chapter 7. From the POG, the LCP and LCP' events are determined. These events are found according to the algorithms  $Bound_Assert$  and  $Find_LCPs$  also of chapter 7. This phase produces the same results for SETPART that where given in section 8.1.

The last phase of pass one forks a child process that is the second pass of the compiler and establishes a pipe from the first pass process to the second pass process. Through this pipe the identification of the *LCP* and *LCP'* events are sent to the second pass. The identification of each event consists of two numbers: process identifier and communication node identifier. As the nodes of the control flow graph are created in phase one, a counter **commoNodeID** is assigned to each communication node. The counter **commoNodeID** is initialized to one each time a new control flow graph is built and incremented each time an **async\_recv** or **async\_send** node is added.

The second pass of the compiler reads the LCP and LCP' event identifications and stores this information in the table IDMap. The distributed processes are parsed again by pass two, and a new source file is created for each process. The name of each file is N.file.c, where *file* is the name of the original source file. If the names of SETPART's original source files are proc0.c and proc1.c, then N.proc0.c and N.proc1.c are the two new source files created by pass two. These new source files are the result of altering the original files to incorporate piggybacking of data on the *LCP* and *LCP'* events.

The first line written in process  $P_i$ 's new file is **#include "assert***i*.**h**". When a line of source code is read by the parser that is not an **async\_send()** or **async\_recv()** function call that corresponds to an *LCP* or *LCP'* event, the line is written to the new source file. The parsing of pass two does not create internal data structures, only a **commoNodeID** counter is maintained as in pass one. When a send or receive command is detected during parsing, the **commoNodeID** is incremented and the table **IDMap** is checked to determine if the command is an *LCP* or *LCP'* event. If the command is an *LCP* or *LCP'* event and is an **async\_send()** function call, the function name is replaced with Piggy\_send. The parameters of the function are not altered. A line is also added after the function call to update vector time. If the command is an *LCP* or *LCP'* event and is an **async\_recv()** function call, the function name is replaced with Piggy\_recv. Again the parameters of the function name is replaced with Piggy\_recv again the parameters of the function name is replaced with Piggy\_recv.

After the source file for  $P_i$  has been parsed, two lines are added to the end of the new source file to include the **pigRecvi.c** file and the **pigSendi.c** file, thus completing the creation of the new file. Once all new source file are created, our two pass compiler is finished. The new files for SETPART are shown below.

```
N.proc0.c:
#include "assert0.h"
#include <stdio.h>
```

```
#include <async.h>
#include <sys/time.h>
int S[16];
int x;
main(argc,argv)
     int argc;
     char *argv[];
Ł
  int count;
  int numcount;
  int len;
  int i;
  int mx;
  if (argc < 2)
     Ł
       fprintf ( stderr, "USAGE: %s <st size>\n", argv[0]);
       exit(1);
     }
  init_async (121, 0, 2, 0, 0.0, 0, 0);
  count = atoi(argv[1]);
  Init_List ( S, &numcount, count, 0);
  printf("Initial set in PO\n\t");
  for ( i=0; i<numcount; i++ )</pre>
       printf("%6d ", S[i]);
  printf("\n\n");
  mx = max(S);
  x = -999999;
  while (mx > x)
     ſ
       Piggy_send(1, &mx, sizeof(mx));
       _vector_t[0]++;
       Remove (S, &numcount, mx);
       len = sizeof(int);
       async_recv(1, &x, &len, 60);
       _vector_t[0]++;
       Add (S, knumcount, x);
       mx = max(S);
     }
  printf("Final set in PO\n\t");
  for ( i=0; i< numcount; i++ )</pre>
```

```
printf("%6d ", S[i]);
   printf("\n\n");
   close_async();
 }
 #include "pigRecv0.c"
 #include "pigSend0.c"
N.procl.c:
 #include "assert1.h"
 #include <stdio.h>
 #include <async.h>
 #include <sys/time.h>
 int mn;
 int T[16];
 int y;
 main(argc,argv)
      int argc;
      char *argv[];
 {
   int count;
   int numcount:
   int len;
   int i;
   int devdata;
   devdata = 1;
   if (argc < 2)
      {
        fprintf ( stderr, "USAGE: %s <set size>\n", argv[0]);
        exit(1);
      }
   init_async (121, 1, 2, 0, 0.0, 0, 0);
   count = atoi(argv[1]);
   numcount = Init_List ( T, &numcount, count, 1);
   printf("Initial set in P1\n\t");
   for ( i=0; i<numcount; i++ )</pre>
        printf("%6d ", T[i]);
   printf("\n\n");
   while (devdata > 0)
      {
        len = sizeof(int);
        devdata = Piggy_recv(0, ky, klen, 60);
```

```
_vector_t[1]++;
       if (devdata > 0)
   £
      Add ( T, &numcount, y );
     \cdot mn = min(T);
      assert((max(CG._PO_S.S) == y) kk
       (max(CG._PO_S.S) >= mn) kk
                   (mn > CG._PO_x.x)
                                            ŁŁ
                   (intersect(CG._PO_S.S, T) == y) );
      async_send(0, &mn, sizeof(mn));
            _vector_t[1]++;
     Remove ( T, &numcount, mn );
   }
    }
 printf("Final set in P1\n\t");
 for ( i=0; i<numcount; i++ )</pre>
       printf("%6d ", T[i]);
 printf("\n\n");
 close_async();
#include "pigRecv1.c"
#include "pigSend1.c"
```

}

The new files are ready for compilation and execution. After compilation, the executing programs create and maintain a causal global state for the assert statements. The assert statement is evaluated using the causal global state transmitted via the identified LCP messages. Despite the potential disturbance to the timing of the distributed program's execution by increasing message sizes, the timing changes of our technique are minor compared to other existing techniques. We do not add messages to the distributed execution and execution is not suspended to gather state information. By preserving the causal relationships, the distributed program maintains the same functionality of the original.

# Chapter 9

# Conclusions

Our research addresses the difficult issue of monitoring the execution of a distributed system. We have developed a runtime method for monitoring both stable and unstable properties that does not disrupt the computation of the distributed system. We used the sequential assert statement as the basis for our development of the distributed assert statement. A distributed assert statement is evaluated with that statement's causal global state. The causal global state incorporates the state of the system as a whole as it may have causal impact upon the assert statement.

We have developed a runtime protocol that constructs the causal global state and evaluates the assert statement where no additional synchronization or message passing is imposed on the distributed application. The causal global state is immediately available providing real-time feedback.

The protocol increases the size of only the messages corresponding to the LCP and LCP' events. We refined our protocol by statically analyzing the distributed program in order to reduce the amount of piggybacked data. Our techniques are able to analyze complex

distributed programs where each process has branches in execution and nested loops. The POG is able to represent all concurrent and causal relationships and all possible paths of the system's execution. By having this information condensed into the POG, we are able to determine the assert's LCP and LCP' events.

In conclusion, our work provides a practical solution for monitoring a distributed system's execution that is not only theoretically sound, but also implementable. Our solution provides a powerful monitoring tool that can be used throughout the system's life cycle, and the only responsibility left to the distributed program developer is to assert predicates as needed. The developer must understand causality to create informative predicates since they will be evaluated with a causal global state.

## 9.1 Communication Systems

Two message passing systems are commonly used for writing distributed programs. These systems are PVM (Parallel Virtual Machine) and MPI(Message Passing Interface). Both can run on a variety of architecture platforms and provide a library of communication commands. Our work has not been ported to these systems, but we will address what would be involved.

PVM is the forerunner of MPI. PVM provides asynchronous reliable FIFO point-to-point communication on a heterogeneous network of machines running Unix. A process sends a message to another process with the command pvm\_send(). The pvm\_send() has the same functionality as our async\_send(). A process receives a message with one of the following commands: pvm\_recv(), pvm\_trecv(), or pvm\_nrecv(). The command pvm\_recv() is a

blocking receive and is equivalent to our  $async_recv()$ . As with our  $async_recv()$ , there is an option to receive from any process instead of a specific process. This is achieved with a -1 in the process identification field. We have not addressed this issue in our analysis, although only minor modifications are necessary to handle the -1 option. Consider a four process system with the following line in process  $P_0$ .

In terms of flow of execution, this is equivalent to the nested if/else statements shown below. Since all paths of executable are assumed possible in our analysis, boolean expressions are not necessary and the textual order of the receiving processes is irrelevant in the nested if/else statements.

```
if ()
    async_recv(1, y)
else if ()
    async_recv(2, y)
    else if ()
        async_recv(3, y)
```

We are able to analyze communication commands embedded in nested if/else statements. The only modification required to our analysis is to recognize the -1 option and treat this as nested if/else statements.

The command pvm\_trecv() is a blocking receive with the ability to timeout after a specified length of time. The command pvm\_nrecv() is non-blocking receive. If a message has not arrived when pvm\_nrecv() is executed, it returns immediately. Our async\_recv() has an option of specifying a length of time to wait for a message. Setting this field to zero is equivalent to a nonblocking receive. We did not explicitly address nonblocking and timeout

receives, but they can be analyzed with minor modifications. Consider a four process system with the following line in process  $P_0$ .

 $async_recv(1, y, \theta)$ 

The zero is the timeout. In terms of execution flow, this is equivalent to the if statement shown below.

if () async\_recv(1. y)

The only change to our analysis is to recognize the use of the timeout field and to analyze in the same manner as an if statement and a receive command.

Multicasting is also possible in PVM. The command  $pvm_mcast()$  is executed by the sender of the multicast message. The sender of the multicast messages may send to all processes except itself. An array of process identifiers is provided to the command  $pvm_mcast()$  specifying which processes should be sent the message. We do not have an equivalent command in our asynchronous library. If the array contains the values 1 and 2, this is equivalent to two asynchronous send commands, one sending to  $P_1$  and one sending to  $P_2$ . Our analysis is able to handle a sequential series of send commands. The modifications necessary to analyze a multicast command are to read the pids from the array and treat each entry as a separate send command.

MPI provides reliable FIFO communication which can be either asynchronous or synchronous indicated by the send command. Communication can also be either blocking or

#### CHAPTER 9. CONCLUSIONS

nonblocking. Both the send and receive commands indicate whether blocking is desired. MPI's and PVM's blocking have different semantics. MPI attempts to improve system performance by overlapping communication and computation. Nonblocking communication is one way to achieve this overlap. A nonblocking send is initiated with a command that copies the message to a buffer and immediately returns. While computation is preceding, the message is copied out of the send buffer. The send is completed with a command to verify that the message has been transferred. Similarly, a receive command initiates the receive operation and immediately returns. While computation continues, data is transfered into the receive buffer. A separate command completes the receive operation.

MPI's library of communication commands is large, and it is not necessary to discuss each command. We will describe how each type of communication can be achieved with a subset of the commands. Asynchronous communication can be achieved with the communication pair MPI\_BSend() and MPI\_Recv(). The B preceding Send indicates that message buffering is to be used. The send blocks by default, meaning the send will wait until the message is copied out of the sender's buffer before it returns control to the caller. The receive also blocks by default, meaning it returns only after the receive buffer contains the message. MPI's blocking asynchronous communication can be analyzed as we currently analyze our async\_send() and async\_recv().

Nonblocking communication is indicated with an I in the communication commands: MPI\_IBSend() and MPI\_IRecv(). The command MPI\_IBSend() places the message in the buffer. The command MPI\_Test() verifies that the send has completed. We only need to analyze the MPI\_IBSend(), and it can be analyzed in the same manner as async\_send().

The contents of the send buffer reflect the causal information of the sending process. The computation that occurs between the MPI\_IBSend() and MPI\_Test() do not affect the causal global state and can be considered as occurring after the send. The command MPI\_IRecv() only initiates the receiving of the message. The command MPI\_WAIT() is one of several commands that can complete the receive. The command MPI\_WAIT() waits for the receive to complete. The commands that complete the receipt of the message should be analyzed in the same manner as async\_recv() since this is when the message is received by the process.

The commands for synchronous communication are MPL\_SSend() and MPL\_Recv(). Our work will require modifications to analyze synchronous communication. Synchronous message passing means that the sending process blocks until the message is received by the destination process. We discussed synchronous communication when describing Taylor's work in chapter 6. Since the rendezvous of a send/receive pair in the synchronous domain can be considered a single event on the sending and receiving processes, the algorithms for constructing the POG and the H will require modification to correctly represent the happens before relationships. The algorithms for finding the LCP and LCP' events will also require minor modifications.

MPI's communication commands have the same options that are available with PVM's commands. We discussed the analysis of these options when describing PVM. For example, the MPI receive command also has a wild card to indicate it will accept a message from any process. MPI also provides commands for broadcasting. The analysis of these broadcast commands can be handle in the same manner as with PVM multicast commands. In conclusion, the major work for analysis programs written in either of these two message passing systems is for synchronous communication. As described, the remaining work will require minor modifications for recognizing the particular system's asynchronous communication commands.

### 9.2 Complexity issues of static analysis

The worst case performance of our static analysis is exponential in the number of possible concurrency states. For the worst case, assume every node of a flow graph can occur in the same concurrency state with every node from the other processes' flow graphs. If we let T be the number of nodes of all the processes' flow graphs, then an upper bound on the number of nodes of one flow graph is O(T). The worst case bound on the number of concurrency states is  $O(T^N)$ , where N is the number of processes in the distributed application.

Although static analysis can have exponential performance, the time spent analyzing does not affect the execution of the distributed system. The analysis is done prior to execution, and provides insight into the application's behavior.

Performance improving refinements to the analysis algorithms have been considered. Localized portions of the POG can be constructed based on the location of the assert statement. Only the events that occur before the execution of the assert statement need to be represented in the POG. Representation of communication events that occur after the last LCP' events is not necessary to determine the remaining LCP and LCP' events. Our algorithms can be modified to determine the last LCP' events before constructing H and POG graphs. When a last LCP' event is represented in H, construction of that branch of execution can stop. This can result in a smaller H and POG, depending on the location of the assert statement.

Space conservation is possible by not generating the complete H graph prior to generating the POG. As a portion of the H graph is generated, the corresponding portion of the POG can be generated. This portion of H is no longer needed and can be discarded. The space required to store the entire H graph would not be necessary.

### 9.3 Future Work

Our work can be extended in several directions. Three major areas are described.

### 9.3.1 Data Analysis

To minimize the amount of piggybacked data, we statically analyze a distributed program and identify the *LCP* and *LCP'* events. This can greatly reduce the number of messages piggybacking data. Additional reductions can be obtained by performing data analysis with regard to the assert statement. In the simplest case, processes only send state information regarding variables used in the asserted predicate. The amount of data piggybacked, and the sizes of the causal state buffers are reduced to include only relevant variables. The maximum size of a process's causal state buffer is one tuple for each variable in the assert. Since a process only piggybacks the contents of its causal state buffer, this maximum also applies to the increased size of messages. Consider a distributed program where a process's LCP event is executed more than one time (e.g., it occurs in the body of a loop), as demonstrated in the distributed program SETPART where process  $P_0$ 's LCP event occurs in a while loop. If  $P_0$ 's state information changes every time the LCP event is executed, then this state information should be piggybacked to correctly propagate the state of the process. If, however, the state information does not change, piggybacking duplicate state information is not necessary.

Sophisticated static analysis, such as data flow analysis [1], can provide the information required to determine whether the state of the process has changed since the last piggy-backing of state information. This type of static analysis, in combination with determining the LCP and LCP', can provide additional reductions in the amount of piggybacked data.

### 9.3.2 Modifications to the Distributed Program

If we change the location of an assert statement or add assert statements to the distributed application, the affects to our static analysis are minor. The POG does not require modification since a different assert location does not affect the concurrency and causal relationships of the distributed program. When an assert is added or relocated in process  $P_i$ ,  $P_i$ 's flow graph can be updated with the appropriate location of the assert node. As with all assert statements, algorithm Bound\_Assert() is called to determine the *last LCP'* events, and algorithm Find\_LCPs() is called to determine the *LCP* and *LCP'* events of the assert statement.

If the assert's predicate is changed, this will only affect data analysis. Although we have not developed these algorithms, we suspect that additional variables will not invalidate the prior data analysis. If variables are removed, the corresponding portion of the data analysis should also be removed.

If the distributed program is altered, the effects to the already existing flow graphs and POG are dependent on the type of changes. Changes to assignment statements will not affect the POG but may alter the data analysis. Additions or deletion of control constructs which do not alter communication events will not affect the POG. If control constructs are added or deleted that affect communication events, or if communication events are added or deleted. the POG is affected. The effects may be incremental, meaning that only a portion of the communication analysis requires reevaluation.

Since distributed assert statements are initially intended as a tool for debugging, altering the distributed program is expected. Incremental static analysis may provide a feasible and efficient solution for updating the flow graphs and the *POG*.

#### 9.3.3 Global Assert Statement

We have demonstrated the usefulness of evaluating assert statements with causal global states. but distributed systems may remain which require their execution to be monitored with global states. In chapter 3, algorithms that capture global states of the distributed system's execution, problems capturing global states, and the lack of meaningful predicate evaluation with these states were described. Two of our conclusions about global state reasoning were (1) the consideration of all global states of the system is required for a meaningful evaluation of the predicate, and (2) obtaining global states should not invalidate other global states. Our work can be extended by developing a meaningful run-time evaluation of

a global assert statement, i.e., evaluation against all consistent cuts that include the assert statement.

The POG is useful for evaluating a global assert statement. It provides the information needed to determine the consistent cuts of the distributed system's computation that include the assert statement. By examining a partial order of a distributed program, we can determine a lower and upper bound communication event in each process that define the region of execution that is concurrent to an assert statement. If  $P_j$ 's lower and upper bound events are *lower<sub>j</sub>* and *upper<sub>j</sub>*, then all events in  $P_j$  that happen between *lower<sub>j</sub>* and *upper<sub>j</sub>* are concurrent to the assert statement. A process's *LCP* message is the lower bound message of the process's concurrent region. The upper bounds can be determined from the *POG* by a similar method to *LCP* determination with node traversal occurring downward instead of upward. Once the lower and upper bounds are found in each process, all valid consistent cuts of the assert can be constructed from the concurrent regions' events.

A run-time method of gathering the information of the consistent cuts is required for global assert statement evaluation. One possibility is to send each local state and corresponding vector time that results from the execution of an event concurrent to the assert to a monitor process. The monitor process can glue together, using vector time stamps, the received local states to form global states for assert statement evaluation. The monitor process will have all the state information necessary for a meaningful evaluation of the assert statement. An evaluation method based on gathering state information concurrent to the assert is meaningful since evaluation is done with all global states that result from a consistent cut including the assert statement. Admittedly, this is only a starting point for developing a global evaluation method, but the majority of the static analysis exists in the *POG*.

## 9.4 Concluding Remarks

A meaningful and reliable technique for examining the execution of distributed programs has been our goal. By developing both causal distributed assert statements and a static analysis technique for determining the LCP and LCP' events for piggybacking state information, we have achieved our goal with minimal interference to the execution of a distributed program. Existing run time debugging techniques are not reliable for detecting buggy programs since they capture only one of many global states. The one captured global state may or may not provide meaningful information. To capture a global state, these techniques add messages to the distributed execution which alter the causal relationships among events.

Our results provide a practical tool for the distributed system engineer. As demonstrated with our analyzed programs, the examination of an execution is easily achieved by inserting assert statements that express the expected behavior of the program. Our prototype evaluates the assert without requiring the programmer to alter the distributed program or to log state information. The programmer will need to rethink his debugging strategy. Instead of thinking globally, a causal view of the execution is necessary. Once this is achieved, causal assert statements convey meaningful insight into the program's behavior.

# Appendix A

# Grammar

The italicized variables are nonterminals, and the all capitalized nonterminals are tokens in the lexer. Terminals appear in monospaced font.

| translation_unit | <b>→</b>      | external_decl                                      |
|------------------|---------------|--|
|                  | I             | translation_unit external_decl                     |
| external_decl    | <b>→</b>      | function_defn                                      |
|                  | ł             | declaration  |
| function_defn    | $\rightarrow$ | decl_specifiers declarator decl_list compound_stmt |
|                  | ł             | decl_specifiers declarator compound_stmt           |
|                  | i             | declarator decl_list compound_stmt                 |
|                  | I             | declarator compound_stmt                           |
|                  | I             | POUND < postfix_expr >                             |
|                  | l             | POUND < postfix_expr / postfix_expr >              |
|                  | ł             | POUND " postfix_expr "                             |
|                  | I             | POUND " postfiz_expr / postfix_expr "              |

| decl_specifiers        | $\rightarrow$   | storage_class_specifier                 |
|------------------------|-----------------|---|
|                        | 8               | storage_class_specifier decl_specifiers |
|                        | I               | type_specifier                          |
|                        |                 | type_specifier decl_specifiers          |
|                        | I               | type_qualifier                          |
|                        |                 | type_qualifier decl_specifiers          |
| init_declarator_list   | $\rightarrow$   | init_declarator                         |
|                        | I               | init_declarator_list , init_declarator  |
| init_declarator        | $\rightarrow$   | declarator                              |
|                        |                 | declarator = initializer                |
| storage_class_specifie | $r \rightarrow$ | TYPEDEF                                 |
|                        | ļ               | EXTERN                                  |
|                        | 1               | STATIC                                  |
|                        | ł               | AUTO                                    |
|                        |                 | REGISTER                                |
| type_specifier         | $\rightarrow$   | VOID                                    |
|                        | 1               | CHAR                                    |
|                        | 1               | SHORT                                   |
|                        | I               | INT                                     |
|                        | I               | LONG                                    |
|                        | ł               | FLOAT                                   |
|                        | I               | DOUBLE                                  |

| l | SIGNED                    |
|---|---------------------------|
| 1 | UNSIGNED                  |
| l | struct_or_union_specifier |
| 1 | enum_specifier            |
| Ι | TYPE_NAME                 |

#### struct\_or\_union\_specifier

٠

|                          | $\rightarrow$ | struct_or_union IDENTIFIER struct_decl_list       |
|--------------------------|---------------|---|
|                          | l             | struct_or_union struct_decl_list                  |
|                          | ł             | struct_or_union IDENTIFIER                        |
| struct_or_union          | $\rightarrow$ | STRUCT  |
|                          | I             | UNION   |
| struct_decl_list         | <b>→</b>      | struct_decl                                       |
|                          | ł             | struct_decl_list struct_decl                      |
| struct_decl              | $\rightarrow$ | specifier_qualifier_list struct_declarator_list ; |
| specifier_qualifier_list | $\rightarrow$ | type_specifier specifier_qualifier_list           |
|                          | F             | type_specifier                                    |
|                          | I             | type_qualifier specifier_qualifier_list           |
|                          | I             | type_qualifier                                    |
| struct_declarator_list   | $\rightarrow$ | struct_declarator                                 |
|                          | I             | struct_declarator_list , struct_declarator        |

| struct_declarator | $\rightarrow$ | declarator                                |
|-------------------|---------------|---|
|                   | 1             | : constant_expr                           |
|                   |               | declarator : constant_expr                |
| enum_specifier    | $\rightarrow$ | ENUM enumerator_list                      |
|                   |               | ENUM IDENTIFIER enumerator_list           |
|                   | I             | ENUM IDENTIFIER                           |
| enumerator_list   | $\rightarrow$ | enumerator .                              |
|                   | l             | enumerator_list, enumerator               |
| enumerator        | $\rightarrow$ | IDENTIFIER                                |
|                   |               | IDENTIFIER = constant_expr                |
| type_qualifier    | <b>→</b>      | CONST                                     |
|                   |               | VOLATILE                                  |
| declarator        | $\rightarrow$ | pointer direct_declarator                 |
|                   | I             | direct_declarator                         |
| direct_declarator | $\rightarrow$ | IDENTIFIER                                |
|                   | I             | ( declarator )                            |
|                   | I             | direct_declarator [ CONSTANT ]            |
|                   | I             | direct_declarator []                      |
|                   | I             | direct_declarator ( parameter_type_list ) |
|                   | I             | direct_declarator ( identifier_list )     |
|                   | I             | direct_declarator ()                      |

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| pointer             | $\rightarrow$ | •  |
|---------------------|---------------|--|
|                     | I             | <pre>* type_qualifier_list</pre>             |
|                     | 1             | * pointer                                    |
|                     | I             | <pre>* type_qualifier_list pointer</pre>     |
| type_qualifier_list | $\rightarrow$ | type_qualifier                               |
|                     | I             | type_qualifier_list type_qualifier           |
| parameter_type_list | $\rightarrow$ | parameter_list                               |
|                     | I             | parameter_list, ELIPSIS                      |
| parameter_list      | $\rightarrow$ | parameter_decl                               |
|                     | ł             | parameter_list , parameter_decl              |
| parameter_decl      | $\rightarrow$ | decl_specifiers declarator                   |
|                     | I             | decl_specifiers abstract_declarator          |
|                     | t             | decl_specifiers                              |
| identifier_list     | $\rightarrow$ | IDENTIFIER                                   |
|                     | l             | identifier_list, IDENTIFIER                  |
| type_name           | $\rightarrow$ | specifier_qualifier_list                     |
|                     | l             | specifier_qualifier_list abstract_declarator |
| abstract_declarator | <b>→</b>      | pointer                                      |
|                     | l             | direct_abstract_declarator                   |
|                     | I             | pointer direct_abstract_declarator           |

 $direct\_abstract\_declarator$ 

|                  | $\rightarrow$ | ( abstract_declarator )                            |
|------------------|---------------|--|
|                  | 1             | []   |
|                  | ļ             | [ constant_expr ]                                  |
|                  | 1             | direct_abstract_declarator [ ]                     |
|                  | 1             | direct_abstract_declarator [ constant_expr ]       |
|                  | 1             | ()   |
|                  | l             | ( parameter_type_list )                            |
|                  |               | direct_abstract_declarator ( )                     |
|                  | l             | direct_abstract_declarator ( parameter_type_list ) |
| initializer      | $\rightarrow$ | assignment_expr                                    |
|                  | ļ             | initializer_list                                   |
|                  | I             | initializer_list ,                                 |
| initializer_list | $\rightarrow$ | initializer  |
|                  |               | initializer_list, initializer                      |
| stmt             | $\rightarrow$ | labeled_stmt                                       |
|                  |               | compound_stmt                                      |
|                  | I             | expr_stmt  |
|                  | I             | selection_stmt                                     |
|                  | I             | iteration_stmt                                     |
|                  | t             | jump_stmt  |

•

| labeled_stmt   | $\rightarrow$ | IDENTIFIER : stmt                              |
|----------------|---------------|--|
|                |               | CASE constant_expr : stmt                      |
|                |               | DEFAULT : stmt                                 |
| compound_stmt  | $\rightarrow$ |  |
|                | I             | stmt_list                                      |
|                | l             | decl_list                                      |
|                | I             | decl_list stmt_list                            |
| decl_list      | $\rightarrow$ | declaration                                    |
|                | I             | decl_list declaration                          |
| stmt_list      | <b>→</b>      | stmt   |
|                |               | stmt_list stmt                                 |
| expr_stmt      | $\rightarrow$ | ;  |
|                |               | expr ;   |
| selection_stmt | $\rightarrow$ | IF ( expr ) stmt                               |
|                | I             | IF (expr) stmt ELSE stmt                       |
|                | I             | SWITCH (expr) stmt                             |
| iteration_stmt | $\rightarrow$ | WHILE whileprod (expr) stmt                    |
|                |               | DO doprod stmt UNTIL ( expr );                 |
|                | Ι             | FOR tempprod ( expr_stmt expr_stmt ) stmt      |
|                | I             | FOR tempprod ( expr_stmt expr_stmt expr ) stmt |
| whileprod      | $\rightarrow$ | {}   |
| doprod         | $\rightarrow$ | {}   |

.

| tempprod            | $\rightarrow$ | {}                                  |
|---------------------|---------------|-------------------------------------|
| jump_stmt           | $\rightarrow$ | CONTINUE ;                          |
|                     | I             | BREAK ;                             |
|                     |               | RETURN ;                            |
|                     | l             | RETURN expr ;                       |
| relational_expr     | $\rightarrow$ | shift_expr                          |
|                     | 1             | relational_expr < shift_expr        |
|                     | l             | relational_expr > shift_expr        |
|                     |               | relational_expr LE_OP shift_expr    |
|                     | ļ             | relational_expr GE_OP shift_expr    |
| shift_expr          | $\rightarrow$ | additive_expr                       |
|                     | l             | shift_expr LEFT_OP additive_expr    |
|                     | 1             | shift_expr RIGHT_OP additive_expr   |
| additive_expr       | $\rightarrow$ | multiplicative_expr                 |
|                     | 1             | additive_expr + multiplicative_expr |
|                     |               | additive_expr - multiplicative_expr |
| multiplicative_expr | $\rightarrow$ | cast_expr                           |
|                     |               | multiplicative_expr + cast_expr     |
|                     | I             | multiplicative_expr / cast_expr     |
|                     | 1             | multiplicative_expr % cast_expr     |
| cast_expr           | $\rightarrow$ | unary_expr                          |
|                     |               | ( type_name ) cast_expr             |

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| unary_ezpr         | $\rightarrow$  | postfix_expr   |
|--------------------|----------------|--|
|                    |                | INC_OP unary_expr                                      |
|                    |                | DEC_OP unary_expr                                      |
|                    | l              | unary_operator cast_expr                               |
|                    |                | SIZEOF unary_expr                                      |
|                    |                | SIZEOF ( type_name )                                   |
| argument_expr_list | $\rightarrow$  | assignment_expr  |
|                    |                | argument_expr_list, assignment_expr                    |
| postfix_expr       | $\rightarrow$  | primary_expr   |
|                    |                | postfix_expr [ expr ]                                  |
|                    | l              | postfix_expr ( )                                       |
|                    | ł              | postfix_expr ( argument_expr_list )                    |
|                    | ł              | postfix_expr . IDENTIFIER                              |
|                    | l              | postfix_expr PTR_OP IDENTIFIER                         |
|                    | 1              | postfix_expr INC_OP                                    |
|                    | 1              | postfix_expr DEC_OP                                    |
|                    | I              | SEND ( cast_expr , cast_expr , cast_expr )             |
|                    | T              | RECV ( cast_expr , cast_expr , cast_expr , cast_expr ) |
|                    | 1              | ASSERT ( expr )  |
| primary_expr       | <del>-</del> > | IDENTIFIER   |
|                    | I              | CONSTANT   |
|                    | I              | STRING_LITERAL   |

|                   | ł             | (expr)                                    |
|-------------------|---------------|---|
| unary_operator    | $\rightarrow$ | لع<br>ا                                   |
|                   | ł             | *   |
|                   | 1             | +   |
|                   | 1             | -   |
|                   | ļ             | -   |
|                   |               | !   |
| equality_expr     | $\rightarrow$ | relational_expr                           |
|                   | 1             | equality_expr EQ_OP relational_expr       |
|                   | ļ             | equality_expr NE_OP relational_expr       |
| and_expr          | $\rightarrow$ | equality_expr                             |
|                   |               | and_expr & equality_expr                  |
| exclusive_or_expr | $\rightarrow$ | and_expr                                  |
|                   | I             | exclusive_or_expr ^ and_expr              |
| inclusive_or_expr | $\rightarrow$ | exclusive_or_expr                         |
|                   | l             | inclusive_or_expr   exclusive_or_expr     |
| logical_and_expr  | $\rightarrow$ | inclusive_or_expr                         |
|                   | ļ             | logical_and_expr AND_OP inclusive_or_expr |
| logical_or_expr   | $\rightarrow$ | logical_and_expr                          |
|                   | I             | logical_or_expr OR_OP logical_and_expr    |
| conditional_expr  | $\rightarrow$ | logical_or_expr                           |
|                   | I             | logical_or_expr ? expr : conditional_expr |

| assignment_expr     | $\rightarrow$ | conditional_expr                               |
|---------------------|---------------|--|
|                     | I             | unary_expr assignment_operator assignment_expr |
| assignment_operator | $\rightarrow$ | =  |
|                     | I             | MUL_ASSIGN                                     |
|                     |               | DIV_ASSIGN                                     |
|                     | I             | MOD_ASSIGN                                     |
|                     | I             | ADD_ASSIGN                                     |
|                     | 1             | SUB_ASSIGN .                                   |
|                     |               | LEFT_ASSIGN                                    |
|                     | I             | RIGHT_ASSIGN                                   |
|                     | I             | AND_ASSIGN                                     |
|                     | I             | XOR_ASSIGN                                     |
|                     | I             | OR_ASSIGN                                      |
| expr                | $\rightarrow$ | assignment_expr                                |
|                     | ١             | expr, assignment_expr                          |
| constant_expr       | $\rightarrow$ | conditional_expr                               |
| declaration         | $\rightarrow$ | decl_specifiers;                               |
|                     | 1             | decl_specifiers init_declarator_list ;         |
| D                   | $\rightarrow$ | [0-9]  |
| L                   | $\rightarrow$ | [a-xA-Z_]                                      |
| H                   | $\rightarrow$ | [a-fA-F0-9]                                    |
| E                   | $\rightarrow$ | [Ee][+-]? <b>D</b> +                           |

| FS       | $\rightarrow$ | (f F 1 L)  |
|----------|---------------|------------|
| IS       | $\rightarrow$ | (u U 1 L)* |
| AUTO     | $\rightarrow$ | auto       |
| BREAK    | $\rightarrow$ | break      |
| CASE     | $\rightarrow$ | case       |
| CHAR     | $\rightarrow$ | char       |
| CONST    | $\rightarrow$ | const      |
| CONTINUE | <b>→</b>      | continue   |
| DEFA ULT | $\rightarrow$ | default    |
| DO       | $\rightarrow$ | do         |
| DOUBLE   | $\rightarrow$ | double     |
| ELSE     | $\rightarrow$ | else       |
| ENUM     | $\rightarrow$ | enum       |
| EXTERN   | $\rightarrow$ | extern     |
| FLOAT    | $\rightarrow$ | float      |
| FOR      | $\rightarrow$ | for        |
| IF       | $\rightarrow$ | if         |
| INT      |               | int        |
| INT      | $\rightarrow$ | FILE       |
| LONG     | $\rightarrow$ | long       |
| REGISTER | $\rightarrow$ | register   |
| RETURN   | $\rightarrow$ | return     |

| SHORT      | $\rightarrow$ | short  |
|------------|---------------|--|
| SIGNED     | $\rightarrow$ | signed   |
| SIZEOF     | $\rightarrow$ | sizeof   |
| STATIC     | $\rightarrow$ | static   |
| STRUCT     | $\rightarrow$ | struct   |
| SWITCH     | $\rightarrow$ | switch   |
| TYPEDEF    | $\rightarrow$ | typedef  |
| UNION      | $\rightarrow$ | union  |
| UNSIGNED   | $\rightarrow$ | unsigned   |
| UNTIL      | $\rightarrow$ | until  |
| VOID       | <b>→</b>      | void   |
| VOLATILE   | $\rightarrow$ | volatile   |
| WHILE      | $\rightarrow$ | while  |
| SEND       | $\rightarrow$ | async_send                                       |
| RECV       | $\rightarrow$ | async_recv                                       |
| ASSERT     | $\rightarrow$ | assert   |
| POUND      | $\rightarrow$ | <pre>#include</pre>                              |
| IDENTIFIER | <b>→</b>      | $L(L D)^*$                                       |
| CONSTANT   | $\rightarrow$ | 0[ <b>x</b> X] <i>H</i> <sup>+</sup> <i>IS</i> ? |
|            |               | 0 <b>D+IS</b> ?                                  |
|            |               | <b>D</b> + <b>IS</b> ?                           |
|            |               | <b>D+EFS</b> ?                                   |

 $| D^*.D^+(E)?FS?$ 

 $| D^+.D^*(E)?FS?$ 

- $STRING_LITERAL \rightarrow$ "(\.[^\"])\*"
- RIGHT\_ASSIGN  $\rightarrow$ >>=
- LEFT\_ASSIGN  $\rightarrow$ <<=
- ADD\_ASSIGN  $\rightarrow$ +=
- SUB\_ASSIGN  $\rightarrow$ -==
- MUL\_ASSIGN  $\rightarrow$ \*=
- DIV\_ASSIGN  $\rightarrow$ /≖
- MOD\_ASSIGN %=  $\rightarrow$
- AND\_ASSIGN  $\rightarrow$ **&=**
- XOR\_ASSIGN ^=  $\rightarrow$
- OR\_ASSIGN  $\rightarrow$ =
- RIGHT\_OP  $\rightarrow$ >>
- LEFT\_OP <<  $\rightarrow$
- INC\_OP  $\rightarrow$ ++
- DEC\_OP  $\rightarrow$
- PTR\_OP  $\rightarrow$ ->
- $\rightarrow$ AND\_OP ŁŁ
- OR\_OP  $\rightarrow$
- LE\_OP  $\rightarrow$ <≖ GE\_OP  $\rightarrow$ >=

--

| EQ_OP | $\rightarrow$ | **         |
|-------|---------------|------------|
| NE_OP | $\rightarrow$ | [ <b>=</b> |
| ;     | $\rightarrow$ | ;          |
| {     | $\rightarrow$ | {          |
| }     | $\rightarrow$ | }          |

Appendix B

# **Asynchronous Library Functions**

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init\_async - initialize the asynchronous message transmittion facility

#### SYNOPSIS

#include <async.h>

int init\_async(group, procid, numprocs. vtflag, simlost, nonfifo, traceflag) short group; short procid: short numprocs: short vtflag; double simlost; short nonfifo; short traceflag;

#### PARAMETERS

- group a positive short integer identifying the process group to which this process is a member.
- <u>procid</u> a short integer between 0 and <u>numprocs-1</u> identifying the process number of this member of the process group.
- numprocs a short integer indicating the number of processes in this process group.
- vtflag a flag indicating whether or not vector clocks should be used during this execution. The difference in execution speeds and message sizes for most process groups is insignificant.
- <u>simlost</u> a double floating point number representing the probability of messages sent from this process being lost during transmittion. A value of 0.0 indicates that messages transmittion is reliable and a value of 1.0 will cause **all** messages sent from this process to be lost.
- <u>nonfifo</u> a flag indicating whether or not messages can be delivered out of order. Message order is simulated using the Miller-Park random number generator.
- traceflag a flag indicating whether or not traces of the execution should be constructed. If traceflag is true, then a file named progname.trace will be created. Refer to the async.h header file for the exact layout of the trace records.

## DESCRIPTION

init\_async initializes the asynchronous communication facilities provided by the libasync library. The first parameter identifies the group to which this process belongs. The group id is a short integer that identifies the set of processes within the distributed system. Processes are only allowed to communicate with other processes within their group. In addition, processes are only allowed to begin execution after all processes in the group have been started.

Each process in the system calls <u>init\_async</u> to register with the process server and obtain the list of addresses for the other members of the group. Only after all members have registered are the processes allowed to proceed. If all processes have not registered within a specified timeout period. failure responses are sent to those processes that have registered and the group is removed from the registry. Later attempts to register within the same group are considered requests from a new group.

#### **RETURN VALUES**

- 0 Initialization failed. An indication of why should be printed to stderr.
- 1 Initialization was successful.

#### NOTES

The library containing this and other asynchronous communication related functions, along with the C header files are located in dennis/public. To use them with gcc. the following command should be used.

gcc source -Idennis/public/include -Ldennis/public/lib -lasync -lm -ll

#### **EXAMPLE PROGRAMS**

Here are two programs that use asynchronous communication to send a simple "Hello World" string from process 0 to process 1. The receiving process then prints the number of bytes received and the received message. Notice that the message length is increased by 1 to insure the received message contains the '\0' string terminating character.

## **Process** 0

#include <stdio.h>
#include <async.h>
main ()

```
{
    char message[32];
    /* group: 101, process: P0, 2 processes in group */
    init_async(101, 0, 2, 0, 0.0, 0);
    sprintf(message,"Hello World");
    /* send message to P1 */
    async_send(1, message. strlen(message)+1);
    /* finished */
    close_async();
}
```

#### Process 1

```
#include <stdio.h>
#include <stdio.h>
#include <async.h>
main ()
{
    char message[32];
    int msglen:
    /* group: 101. process: P1. 2 processes in group */
    init_async(101. 1. 2. 0. 0.0. 0):
    msglen = 32:
    /* receive message from P0 */
    async_recv(0, message. &msglen. 0);
    printf("received %d bytes [%s]0. msglen. message):
    /* finished */
    close_async():
}
```

## **SEE ALSO**

| $\operatorname{async\_send}(2),$ | $\operatorname{async}\operatorname{recv}(2).$ | $close_async(2),$ | recv_qinfo(2). | <pre>inc_vtime(2),</pre> |
|----------------------------------|---|-------------------|----------------|--------------------------|
| get_vtime(2)                     |   |                   |                |                          |

async\_send - send an asynchronous message to another process

## SYNOPSIS

#include <async.h>

int async\_send( procid. msg, len ) short procid; void \*msg; int len;

#### PARAMETERS

- msg a pointer to the begining address of a message to be sent.
- <u>len</u> the length in bytes of the message. (Currently restricted to (<u>MAXMSGSIZE</u>) 10240 bytes.)

## DESCRIPTION

If vector time is in use, the local component is incremented to indicate the occurrence of an event. The message pointed to by  $\underline{\mathrm{msg}}$  length  $\underline{\mathrm{len}}$  is then sent to process procid. If <u>procid</u> is -1, then the message is broadcast to all other processes in the process group. (See init\_async(2) for a description of process groups.)

## **RETURN VALUES**

- 0 The message was lost during the send process.
- 1 The message was successfully sent to the other process and awaits delivery.

## SEE ALSO

init\_async(2), async\_recv(2), close\_async(2), recv\_qinfo(2), inc\_vtime(2),
get\_vtime(2)

async\_recv - receive an asynchronous message from another process

#### SYNOPSIS

#include <async.h>

#### PARAMETERS

- $\frac{\text{procid}}{\text{fier. the message is accepted from and process in the process group.} \quad \text{identifying the transmitting} \\ \text{fier. the message is accepted from and process in the process group.} \quad \text{identifying the transmitting} \\ \text{fier. the message is accepted from and process in the process group.} \quad \text{identifying the transmitting} \\ \text{fier. the message is accepted from and process in the process group.} \quad \text{identifying the transmitting} \\ \text{fier. the message is accepted from and process in the process group.} \quad \text{identifying the transmitting} \\ \text{fier. the message is accepted from and process in the process group.} \quad \text{identifying the transmitting} \\ \text{fier. the message is accepted from and process in the process group.} \quad \text{identifying the transmitting} \\ \text{fier. the message is accepted from and process in the process group.} \quad \text{identifying the transmitting} \\ \text{fier. the message is accepted from and process in the process group.} \quad \text{identifying the transmitting} \\ \text{fier. the message is accepted from and process in the process group.} \quad \text{identifying the transmitting} \\ \text{fier. the message is accepted from and process in the process group.} \quad \text{identifying the transmitting} \\ \text{fier. the message is accepted from and process in the process group.} \quad \text{identifying the transmitting} \\ \text{fier. the message is accepted from and process in the process group.} \quad \text{identifying the transmitting} \\ \text{fier. the message is accepted from and process in the process group.} \quad \text{identifying the transmitting} \\ \text{fier. the message is accepted from and process in the process group.} \quad \text{identifying the transmitting} \\ \text{fier. the message is accepted from and process in the process group.} \quad \text{identifying the transmitting} \\ \text{fier.} \quad \text{fier$
- msg a pointer to the begining address of a message to be sent.
- <u>len</u> a pointer to an integer to contain the length of the message in bytes. It is initialized to the length of the message buffer. (Currently restricted to (MAXMSGSIZE) 10240 bytes.)
- <u>waitsecs</u> an integer number of seconds to wait for the arrival of a message. If no message has arrived within <u>waitsecs</u> seconds, the function returns a -1. A value of  $\underline{0}$  indicates that the timer should not be used and the function will wait forever.

#### DESCRIPTION

If vector time is in use, the local component is incremented to indicate the occurrence of an event. A message from process procid is copied to the address stored in <u>msg</u>. The length of the message is stored in <u>len</u>. If procid is -1, then the message is accepted from any process in the process group. (See init\_async(2) for a description of process groups.) This option will return the next message in the order of arrival. If no message is available, the function will hang, waiting for an arrival. If no message arrives within <u>waitsecs</u> seconds, then the function returns with a value of -1.

## **RETURN VALUES**

-1 No message was available for delivery within the time specified by the <u>waitsecs</u> parameter.

message length

The message was successfully received from the indicated process. Side effects are to store the message in the memory area pointed to by  $\underline{\text{msg}}$  and to store the size of the received message in the integer pointed to by  $\underline{\text{len}}$ .

## SEE ALSO

```
init_async(2). async_send(2), close_async(2), recv_qinfo(2). inc_vtime(2),
get_vtime(2)
```

close\_async - terminate the asynchronous message transmittion facility

## SYNOPSIS

#include <async.h>

int close\_async()

#### DESCRIPTION

close\_async terminates the asynchronous communication facilities initialized by a call to init\_async. This function should always be called by the program using the async library. Failure to do so could leave zombie children wandering about.

## **RETURN VALUES**

- 1
- Termination was successful. Does not return until termination has been completed.

## SEE ALSO

init\_async(2). async\_send(2). async\_recv(2). recv\_qinfo(2), inc\_vtime(2),
get\_vtime(2)

recv\_qinfo - check the status of the asynchronous message wait queues

## SYNOPSIS

#include <async.h>

int recv\_qinfo( procid ) short procid;

## PARAMETERS

procid a short integer identifying the sending process from which messages should be checked. A value of -1 indicates that messages from **all** processes should be reported.

#### DESCRIPTION

recv\_qinfo checks to see if any messages are waiting to be delivered to this process from process procid.

#### **RETURN VALUES**

- 0 No messages are waiting to be delivered from the indicated process.
- 1 Messages are waiting to be delivered from the indicated process.

## **SEE ALSO**

init\_async(2). async\_send(2), async\_recv(2), close\_async(2), inc\_vtime(2),
get\_vtime(2)

inc\_vtime - increment the local component of the vector clock

## **SYNOPSIS**

#include <async.h>

int inc\_vtime()

#### DESCRIPTION

If vector clocks are being used in the asynchronous communication facilities, this function increments the local component to indicate the occurrence of a significant local event.

## **RETURN VALUES**

0 Vector clocks are not being used in this execution. See init\_async(2).

local vector clock component

The value of the local component of the vector clock is returned after it has been incremented to indicate success.

## SEE ALSO

init\_async(2), async\_send(2), async\_recv(2), close\_async(2), recv\_qinfo(2),
get\_vtime(2)

get\_vtime - return the current vector clock values

#### SYNOPSIS

#include <async.h>

int get\_vtime( vt ) unsigned int \*vt;

#### PARAMETERS

<u>vt</u>

a pointer to an array of unsigned integers where the values in the vector clock should be placed.

#### DESCRIPTION

If vector clocks are being used in the asynchronous communication facilities, this function stores the current value of the vector clock in the array of unsigned integers pointed to by  $\underline{vt}$ .

#### **RETURN VALUES**

An error has occurred preventing the completion of the operation.
Vector clocks are not being used in this execution. See init\_async(2).
The current values of the vector clock have been successfully placed in the <u>vt</u> array.

## SEE ALSO

init\_async(2), async\_send(2), async\_recv(2), close\_async(2), recv\_qinfo(2), inc\_vtime(2)

trace - Add a local event record to a process' trace file

#### **SYNOPSIS**

#include <async.h>

int trace()

### DESCRIPTION

<u>trace</u> is used with the asynchronous communication library event tracing facility. It creates an event record of type <u>TRACE\_LOCAL</u> with the current vector time and adds that record to the trace information. See init\_async(2) for information on initializing the tracing facilities.

#### **RETURN VALUES**

none No values are returned from this function.

### SEE ALSO

```
init_async(2), async_send(2), async_recv(2), recv_qinfo(2), inc_vtime(2),
get_vtime(2), close_async(2)
```

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